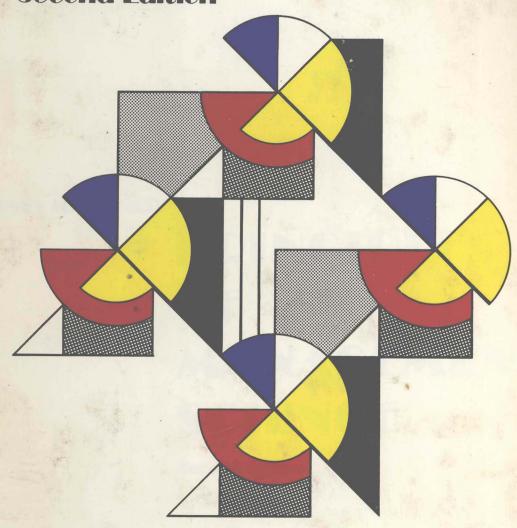
DRINCIPLES OF MANAGEMENT SCIENCE

Second Edition



HARVEY M. WAGNER

PRINCIPLES OF MANAGEMENT SCIENCE

With Applications to Executive Decisions

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Preface

This book is written primarily for college students who have no previous background in management science and who intend careers as administrators, executives, managers, or consultants in business, nonprofit enterprises, or government. The book is used in half-year or full-year introductory courses for undergraduates or graduates in business, economics, engineering, liberal arts, and public administration curricula.

The central goal of the book is to answer the question, "What are the fundamental ideas of management science?" The text does not presuppose any advanced training in business administration, industrial engineering, mathematics, statistics, probability theory, or economics. Therefore, the main ideas do not rely on the reader's being expert in these areas. The text does assume, however, that the reader is not entirely naive about such subjects.

PRINCIPAL OBJECTIVES

Beginning students frequently ask, "What must I learn about management science if I intend to become an executive rather than a specialist?" and "What must I learn about management science given that I want to apply it to real problems?" Regrettably, a single introductory management science course cannot completely answer either question. But such a course can better answer the first rather than the second question.

In the context of these two questions, the book's principal objectives are

- To introduce the important ideas in management science which are both fundamental and long lasting.
- To provide those students not going beyond a single introductory course with enough understanding and confidence to appreciate the strengths and inherent limitations of the management science approach.
- To prepare and motivate future specialists to continue in their study by having an insightful overview of management science.
- To demonstrate the cohesiveness of management science methodology.

Students who have been assigned this book as a text have increased their skills in formulating and building formal models of complex decision environments, in perceiving the critical issues to be resolved, and in isolating the basic phenomena that comprise the key elements of real situations. When faced with actual managerial problems, these students have learned from their grasp of the analytic fundamentals how to achieve sound and incisive evaluations of the important alternatives and how to attain the crucial insights.

COVERAGE AND EMPHASIS

Successful practitioners of management science are quick to point out that characterizing the subject by means of its component mathematical techniques can be highly misleading. Their reason is that real-life decisions do not arise with technical labels attached, such as *linear programming* or *risk analysis simulation*. A manager must be able to recognize what existing methods, if any, can yield worthwhile insights for taking appropriate courses of action. Granting the truth of these observations, we comment on why we organized the text by standard mathematical techniques rather than by various management problems.

Accumulated teaching experience of hundreds of instructors indicates that beginning students with only limited time for this subject better understand the model-building approach when they can *readily* discern the formal structure of the decision problem. Although realism is sacrificed in the classroom by adopting this pedagogic view, students so trained effectively bridge the gap between the techniques and their applications.

To warn students, however, of the trap of thinking that management science is synonymous with a collection of mathematical formulas, we take pains to *verbalize* the contribution that each model and technique make to decision-making. Students previously trained in science, engineering, or mathematics sometimes are surprised and even impatient that the text material is not written in a succinct mathematical style. But we suggest that thinking beyond the details of the formulas to the deeper significance of each approach, over the long pull, better prepares future managers and analysts to make successful applications.

Obviously, we had to exercise considerable judgment in selecting topics and in choosing the depth of treatment. In this regard, we were influenced considerably by more than 20 years of first-hand experience in applying management science to actual situations in business and government. The examples in the text often are scaled-down versions of real problems that we have encountered. The specific models that we chose, their complexity, and sequential development all reflect our observations of how most students come to appreciate and understand the pivotal concepts in management science.

Throughout, the book puts into focus the value of information derived from a management science solution and attempts to give an accurate representation of how a hypothetical example would be applied in a real situation. The text develops the student's skill in formulating and building models and, specifically, in

translating a verbal description of a decision problem into an equivalent mathematical model. The book also explains the importance and the degree of severity of a model's assumptions, the connection between the starting assumptions and the derived results, and the seriousness of the assumptions for practical purposes. Finally, the text demonstrates by means of important examples the process and usefulness of constructing analogies, finding multiple interpretations of models, and deriving significant special cases from general models.

MATHEMATICS PREREQUISITES

The calculus is employed only in Chap. 15. Nevertheless, much of the text assumes a mathematical sophistication comparable to that acquired in standard college-level introductory calculus or a no-nonsense finite mathematics course. Elementary probability theory is first needed in Chap. 12.

SUGGESTIONS TO STUDENTS

If you have taken courses in both the calculus and elementary statistics or probability theory, you will recall that you could understand much of the calculus text without much help from the instructor whereas you needed the guidance of the instructor to fully understand the statistics or probability theory text. This is a very common occurrence among students. You will find management science to be more like statistics and probability theory than the calculus in that you can expect, as a matter of course, to rely on your instructor to amplify the ideas and techniques in this book. Since the concepts can be intricate, you may have to study several pages before comprehending the full idea. So be prepared for patient reading and some rereading. We have tried to avoid giving numerical examples that are so misleadingly simple that you are not sufficiently prepared for the exercises at the end of each chapter. As a result, you will find it advantageous to examine carefully the numerical illustrations in the chapters.

If your instructor assigns the exercises at the back of the chapters, do not wait until the last minute to begin the problems. The numerical exercises, although straightforward, can be fatiguing if attempted in a single evening session. Most students find that formulation problems require a "gestation period," so allow yourself a few days to ponder such exercises.

Surprisingly, it is difficult to write a *verbal* description of a management science problem that is completely unambiguous. More than once, thoughtful students have discovered vague wording in problems that we had assigned previously to other classes that experienced no difficulty in obtaining the intended solutions. Consequently, if you believe that an exercise displays a troublesome ambiguity, try to resolve it in a sensible way and make explicit on your paper the specific assumption that you adopted. The purpose of the exercises (namely, to give you practice in mathematical formulation) is well served by this procedure.

SUGGESTIONS TO INSTRUCTORS

The topic coverage has been purposely designed to give you considerable flexibility in choosing the subjects that you want to stress. The logical organization of the chapters is shown in Exhibit A.

In a one-term introductory course on mathematical programming models, you can include Chaps. 1 through 8, 10, 11, and 17, skipping all the starred (*) sections and optional material in smaller print. In a one-term introductory course on probabilistic models, you can include Chaps. 1, 12 through 17, also skipping optional and advanced material.

To assist you in selecting other combinations, the "Immediate Predecessors" of each chapter are shown in Exhibit B. In general, the chapters become progressively more difficult. Thus, although you could cover dynamic programming (Chaps. 8, 9, and 10) prior to linear programming, the reverse sequence ordinarily would be preferable, because the dynamic programming chapters assume the student already is somewhat familiar with multivariate constrained optimization models and solution techniques. Any material designated by an asterisk or appearing between the symbols \blacktriangleright and \blacktriangleleft and set in smaller print may be skipped without loss of continuity.

The second edition has been written to make certain topics more accessible to beginning students and to update the coverage where a subject's fundamental ideas have changed. Specifically, the *major* revisions occur in Chaps. 6, 7, 10, 11, 12, and 16. The material on networks in Chaps. 6 and 7 is now organized so that each algorithm is presented in conjunction with the model's description and application. A slower-paced exposition of dynamic programming models is given in Chap. 10 the new material includes worked out numerical examples to clarify the approach. The explanation of models and methods for integer programming in Chap. 11 is extensively rewritten to reflect computational experience of recent years; approaches that have not worked well in practice are omitted. The material on stochastic programming in Chap. 12 is revised to be more suitable for assignment in an introductory course. Finally, the exposition of computer simulation in Chap. 16 is expanded and reorganized to give greater prominence to the model-building aspects of the approach.

The book contains more than 600 exercises, many of which have multiple parts. New exercises are added to most chapters in the second edition. The problems are grouped into three categories. The Review Exercises are keyed closely to the text and determine whether the student has understood the conceptual developments. The Formulation Exercises consist of "word problems" and test whether the student can translate a verbal statement into a precise mathematical model. The Computational Exercises provide practice problems for applying algorithms. There is "redundancy" in the multiple parts of many exercises, and consequently, you should examine the parts to ascertain which ones you want to assign.

This text does not treat the topics of deterministic and stochastic dynamic programming over an unbounded horizon, continuous nonlinear programming, transform methods and imbedded Markov chains for queuing models, and gives only a brief discussion of stochastic programming and network algorithms. An

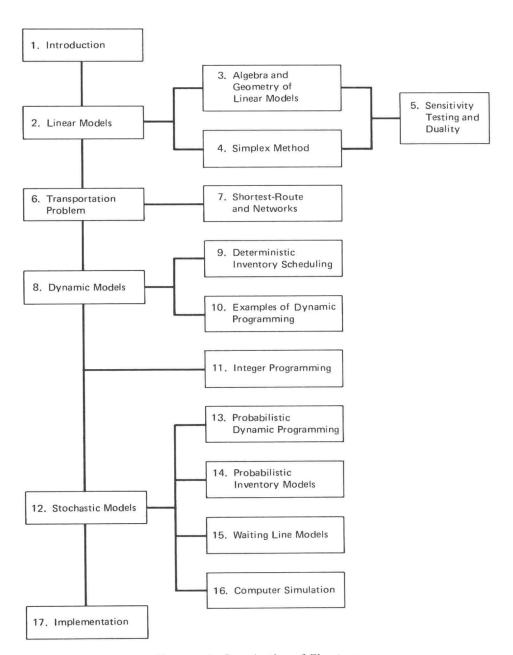


EXHIBIT A. Organization of Chapters.

	CHAPTER	11.151.	nediate ecessors
2	Linear Models		1 2
4	Simplex Method		2
5	Sensitivity Testing and Duality		3, 4
6	Transportation Problem		2, 5
7	Shortest-Route and Other Network Models		6
8	Dynamic Models		1, (7)
9	Deterministic Inventory Schedule		8
10	Examples of Dynamic Programming		8
11	Integer Programming		7
12	Stochastic Models		5
13	Probabilistic Dynamic Programming		10, 12
14	Probabilistic Inventory Models		(9), 12
15	Waiting Line Models		12
16	Computer Simulation		12
17	Implementation		1
NOTE: Chaps. 12 through 16 require probability theory. Chap. 15 requires differential and integral calculus. () indicates desirable but not essential.			

Ехнівіт В

extensive coverage of these topics at an introductory level can be found in my *Principles of Operations Research*, Prentice-Hall, 1975. Important replacement models are included in the dynamic programming chapters. Game theory has been omitted. In practicing operations research, we have found that game theory does not contribute any *managerial insights* to real competitive and cooperative decision-making behavior that are not *already* familiar to church-going poker players who regularly read the Wall Street Journal. (This is not to say, however, that the intricacies of real competitive economic behavior, such as price wars, advertising campaigns, mergers, and acquisitions, have yet become phenomena fully understood by management scientists.)

ACKNOWLEDGMENTS

Over the years since the first draft of this text was written, I have received many helpful suggestions from students and their instructors who have used the book. The list of persons who have provided sage counsel is now far too long to record here, but I must offer special thanks at least to Richard W. Cottle (Stanford), Eric V. Denardo (Yale), Hamilton Emmons (Case Western Reserve), Donald Erlenkotter (University of California, Los Angeles), Charles H. Falkner (University of Wisconsin), Arthur M. Geoffrion (University of California, Los Angeles), Richard B. Hoffman (Arthur Young & Co., Washington, D.C.), Charles L. Hubbard (Georgia State), Charles H. Kriebel (Carnegie Mellon), Rudolph P. Lamone (University of Maryland), Richard P. O'Neill (Louisiana State), Alan J. Rolfe (IDA, Arlington, VA), and Matthew J. Sobel (Yale). I am deeply indebted to Professor Robert E. Machol (Northwestern) whose friendly advice prompted many of the revisions in this new edition. And I again want to acknowledge Professor Arthur F. Veinott, Jr. (Stanford) who has continued to deeply influence my own thinking about the principles of management science.

In great measure, the managerial relevance of the book has been enhanced through my association since 1960 with McKinsey & Co., as a Consultant to the Firm, and particularly through the personal guidance of Dr. David B. Hertz, Douglas Watson, Warren M. Cannon, and D. Ronald Daniel.

A fine Instructor's Manual for the second edition was patiently prepared by Arthur S. Estey and Richard A. Ehrhardt (both of Yale), and a debt of gratitude remains to John Chamberlin, John M. Harrison, and Michael Saunders who wrote the previous Manual.

The secretarial skill and encouraging dispositions of Ms. Sheila Hill (Stanford) and Ms. Marcia Wheeler (Yale) triumphed admirably over the seemingly neverending strain of typing redrafts and meeting deadlines for the first edition. The limited pleasures of struggling over rewrites for the second edition were shared by Ms. Wilma Golden, Ms. Sara Martin, and Ms. Ellen Mester (all of Yale), at last count. And we all can be thankful for the unsparingly, but deftly, employed red pencils of editors Mr. Will Harriss (RAND) and Mr. Kenneth Cashman (Prentice-Hall).

PRINCIPLES OF MANAGEMENT SCIENCE

With Applications to Executive Decisions

CONTENTS

1.1	Once Upon a Time
1.2	By Any Other Name
1.3	Boundaries of Quantitative Analysis
1.4	IMPORTANCE OF MODEL-BUILDING
1.5	Process of Quantitative Analysis8
	Management Science, Lilliputian Style
1.7	At the End of the Rainbow
1.8	In the Beginning
	Review Exercises

Contents

	PREFACE	xv
1	THE ART AND SCIENCE OF EXECUTIVE DECISIONS	1
	 1.1. Once Upon a Time 1 1.2. By Any Other Name 1 1.3. Boundaries of Quantitative Analysis 4 1.4. Importance of Model-Building 6 1.5. Process of Quantitative Analysis 8 1.6. Management Science, Lilliputian Style 10 1.7. At the End of the Rainbow 21 1.8. In the Beginning 24 Review Exercises 24 	
2	FORMULATION OF LINEAR OPTIMIZATION MODELS	29
	 2.1. Introduction 29 2.2. Product-Mix Selection 33 2.3. Feed-Mix Selection 35 2.4. Fluid-Blending Schedule 37 2.5. Dynamic Planning—Integrated Production Planning Example 38 2.6. Product Allocation Through a Transportation Network 42 2.7. Industrial Importance of Linear Optimization Models 47 Review Exercises 50 Formulation Exercises 52 	
3	ALGEBRAIC AND GEOMETRIC REPRESENTATIONS OF LINEAR OPTIMIZATION MODELS 3.1. Introduction 65 3.2. General Algebraic Formulation 65	65

	CONTENTS
v	CONTENTS

3.3. Canonical Forms for Linear Optimization

	Models 69 3.4. Geometric Interpretation 70 Review and Computational Exercises 73 Formulation Exercises 77	
4	4.1. Theory in Perspective 79 4.2. Assessment of the Objective 80 *4.3. The Algorithmic Method 83 4.4. Introduction to the Simplex Algorithm 85 *4.5. Tabular Representation 95 4.6. Completeness and Domain of Applicability 96 4.7. Important Property of an Optimal Solution 100 *4.8. Convergence Properties 100 *4.9. Computational Requirements 103 Review Exercises 103 Computational Exercises 106	79
5	5.1. Postoptimality Analysis 111 5.2. Objective Function 112 5.3. Right-Hand-Side Constants 114 5.4. Duality 114 5.5. Solution to the Dual Problem 121 5.6. More Postoptimality Analysis 123 5.7. Summary 126 Review Exercises 126 Computational Exercises 130	111
6	6.1. Significance of Network Models 135 6.2. Classical Transportation Problem 135 6.3. Transshipment Model 142 6.4. Assignment Model 148 6.5. Duality in the Transportation Problem 149 6.6. Simplex Technique for Transportation 152 6.7. Further Comments on the Simplex Method 161 6.8. Sensitivity Testing 167 Review Exercises 171 Formulation Exercises 177 Computational Exercises 182	135

7	SHORTEST ROUTE AND OTHER NETWORK MODELS	189
	7.1. Topics in Focus 189 7.2 Shortest-Route Model 189 7.3 Shortest-Route Algorithm in a General Network 193 7.4 Shortest-Route Algorithm in an Acyclic Network 198 *7.5 Critical Path Scheduling 199 *7.6 Employment Scheduling 202 Review Exercises 205 Formulation Exercises 208 Computational Exercises 214	
8	INTRODUCTION TO DYNAMIC OPTIMIZATION MODELS	219
	 8.1. Analysis of Dynamic Phenomena 219 8.2. Stagecoach Problem: An Allegory 221 8.3. Elementary Inventory Model 227 8.4. Numerical Solution 232 8.5. Sensitivity Analysis 238 Review Exercises 242 Computational Exercises 248 Formulation Exercises 250 	
9	DYNAMIC OPTIMIZATION OF INVENTORY SCHEDULING	253
	 9.1. Exploiting Special Structure 253 9.2. Convex and Concave Cost Functions 254 9.3. Inventory Model with Convex Costs 257 9.4. Planning Horizon Analysis for Convex Cost Model 262 9.5. Lot-Size Inventory Model with Concave Costs 263 9.6. Algorithm for Concave Cost Model 265 9.7. Planning Horizon Analysis for Concave Cost Model 268 Review Exercises 270 Computational Exercises 273 Formulation Exercises 278 	
10	OTHER EXAMPLES OF DYNAMIC PROGRAMMING	281
	 10.1. Reminder 281 10.2. Distribution of Effort—One Constraint 282 10.3. Capital Budgeting Problem 286 10.4. Knapsack Problem 291 	

10.5. Equipment Replacement Model 295

	*10.6. Inventory Model with Production Smoothing 298 10.7. Distribution of Effort—Two Constraints 303 *10.8. Distribution of Effort—Nested Problem 304 10.9. Structure of Multistage Analysis 306 10.10. Insights to Dynamic Phenomena 307 10.11. Computational Feasibility 308 10.12. Applicability of Dynamic Programming 308 Review Exercises 309 Formulation and Computational Exercises 312	
11	INTEGER PROGRAMMING AND COMBINATORIAL MODELS	323
	 11.1. Quest for a Philosopher's Stone 323 11.2. Integer Programming Formulations 328 11.3. Branch-and-Bound Algorithm 338 11.4. Knapsack Problem 344 *11.5. Extensions of Branch-and-Bound 346 Review Exercises 348 Computational Exercises 355 Formulation Exercises 356 	
12	INTRODUCTION TO STOCHASTIC PROGRAMMING MODELS	367
	 12.1. Impact of Uncertainty 367 12.2. Decision-Making in an Uncertain Environment 371 12.3. Fallacy of Averages 379 12.4. Two-Stage Linear Model 382 12.5. Chance-Constrained Model 388 Review Exercises 391 Formulation and Computational Exercises 396 	
13	PROBABILISTIC DYNAMIC PROGRAMMING MODELS	401
	 13.1. Introduction 401 13.2. Distribution of Effort Example 401 13.3. New Product Introduction—A Decision Tree 404 13.4. Elementary Inventory Model 407 13.5. Optimal Batch Size Model 410 13.6. Stochastic Regeneration Model-Equipment Replacement 415 *13.7. Sales Forecasting Problem 418 	

	Formulation and Computational Exercises 426	
14	PROBABILISTIC INVENTORY MODELS	443
	 14.1. New Orientation 443 14.2. Scientific Approach to Inventory Management 444 14.3. Ground Work for Inventory Analysis 446 14.4. Static (Single Decision) Model 449 14.5. Economic-Order-Quantity Models 454 14.6. Stochastic Dynamic Continuous Review Model 462 *14.7. Stochastic Dynamic Periodic Review Model 472 14.8. Concluding Remarks on Implementation 476 Review Exercises 479 Formulation and Computational Exercises 485 	
15	WAITING LINE MODELS	491
	 15.1. Introduction 491 15.2. Taxonomy of Waiting Line Models 493 15.3. Probability Distributions of Interarrival Times 496 15.4. Probability Distributions of Service Times 501 15.5. Single-Server Model with Poisson Input and Exponential Service (M/M/1) 506 15.6. Multiple-Server Model with Poisson Input and Exponential Service (M/M/5) 517 *15.7. Birth-and-Death Process 522 *15.8. Other Queuing Models 528 Review Exercises 528 Formulation and Computational Exercises 534 	
16	COMPUTER SIMULATION OF MANAGEMENT SYSTEMS	541
	16.1. When All Else Fails 541 16.2. Simulation in Perspective 545 16.3. Stock Market Simulation Example 548 16.4. Building a Simulation Model 551 16.5. How to Mark Time 553 16.6. Computer Languages 557 *16.7. Design of Simulation Experiments 559 *16.8. Generating Random Phenomena 565 *16.9. Deus Ex Machina 573 Review Exercises 574 Formulation Exercises 578	

13.8. Applicability and Computational Feasibility 420

Review Exercises 421