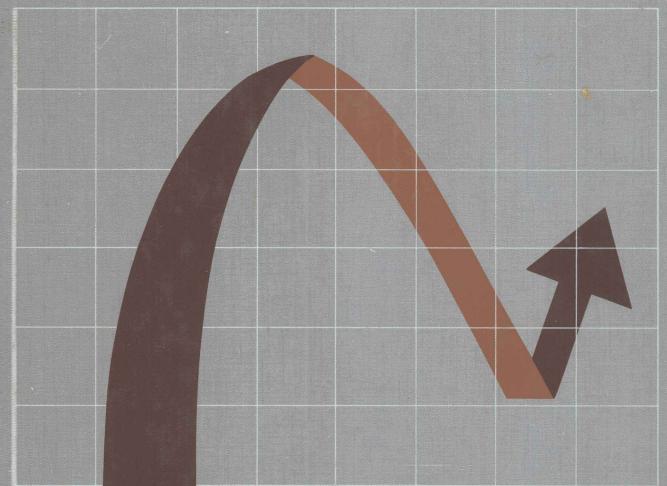
# **Business Statistics**

Methods and Applications

Philip G. Enns



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## Philip G. Enns

School of Business and Administration Saint Louis University

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## Preface

This book is intended to serve as the text for an introductory noncalculus business statistics course. I have tried to present the subject in a "user friendly" style, employing methods developed in teaching the subject over the past dozen years. I believe the book achieves a good balance between the technical precision of formal statistical science and the often vaguely defined conditions of real business and economic applications. Of equal importance, I have attempted to motivate the discussion of statistics by appealing to the reader's common sense and experience. We routinely encounter the use of statistics in our daily lives. Recognizing these situations is a useful starting point for understanding how statistics can help in business decision making.

#### Organization

Business Statistics is organized in four parts designed to take advantage of the logical structure of statistics. Part I presents an overview of the subject, followed by the topic of descriptive statistics. Chapter 1 is not a short throwaway but instead contains terms and discussion that are important to what follows. Chapters 2 and 3 are also somewhat longer than normal. This is a measure of my belief that there is much to be learned by lingering over data before racing off to the conclusions of statistical inference. The inclusion of some exploratory data analysis techniques also reflects the growing interest of the statistics profession in EDA and related descriptive methods. In these and later chapters, sections containing optional or review topics are denoted by an asterisk (\*).

Part II is devoted to probability and random variables. I try to accomplish several things in these chapters. First, I emphasize how probability links the description of past data observations with the uncertainty

of future data. Second, I explore the use of probability in decision making. Finally, avoiding card game and dice rolling examples, I try to relate the elegance of probability theory to the reader's understanding and experience with the worlds of business and economics.

Part III presents an introduction to sampling and statistical inference. The discussion is very basic; it is at once formal and informal. I try to convince the reader of the need for discipline and precision in reaching decisions based on sample data. At the same time, it is acknowledged that the art of applying the tools of inference often forces us to blink at strict rules and definitions.

Part IV contains eight chapters that deal with a range of topics used in business applications of statistics. With the exception of 12 (Multiple Regression), these are meant to be "stand alone" chapters. While they all rely in varying degrees on the first three parts, there is little cross-referencing among these chapters. This is intended to give the instructor maximum flexibility in planning a course. It should also help the reader in using the book for later reference.

Each chapter contains a set of learning aids. Each opens with an outline and objectives corresponding to the chapter sections. At the end of each chapter is a list of suggested readings that provide the interested student with different views of statistics and additional depth in specific topics. A list of terms introduced or emphasized in the chapter is included for the reader's review. The exercises all appear at the end of the chapter. They are grouped according to sections, followed by additional exercises for which the related section(s) is not explicitly identified. Finally, each chapter contains a series of questions concerning one or both sets of real data that appear in Appendix B.

Appendix A contains statistical tables needed for various calculations throughout the book. Appendix B describes and lists two sets of real data: a cross-section of bank loan data and quarterly time series of a corporation's revenues together with several economic measures. These sets are small enough to permit useful analysis by hand calculations but can also be used as input to computer-supported decision making.

Answers to the odd-numbered exercises are provided, followed by a glossary of terms that includes the chapter in which each term first appears.

#### Some Goals and Objectives

Instructors will see that my exposition of probability and statistics follows a traditional path. I have always found special pleasure in

the logic and consistency of mathematical statistics; trying to hide this would only weaken the book. But for this reason, I have made an extra effort to provide illustrations of statistics that are interesting and relevant to the reader's experience and business training. In choosing examples and exercises, one quickly tires of fabricating situations that perfectly illustrate a specific definition or rule and nothing else. As much as possible, I have drawn on the use of real data and, especially, the statistical applications of researchers in business, economics, and related fields. This was often quite a challenge, since real-world applications of statistics are rarely as simple and tidy as introductory textbooks would have us think. I believe I have succeeded in adapting these real examples to this beginning book in a way that is both interesting and unintimidating. I certainly learned a lot about the variety of business applications of statistics along the way.

The exercises range in difficulty from very simple to reasonably challenging. Some require a fair amount of data entry effort. Students and their instructors are encouraged to utilize whatever computing equipment is available; I see no special virtue in doing more arithmetic than is absolutely necessary. Beware that the precision of your calculations will sometimes produce substantial differences between your solutions and those provided in the book.

Some statistics-related cartoons from *The New Yorker* magazine are reprinted at various points in the book. I hope the reader enjoys these. I hope also that the cartoons help express what, to me, is important in teaching statistics in a school of business. We use data to support decisions that relate to all aspects of our lives. Most people don't really care very much about the technical side of statistics. When they filter the subject through their own experience and intelligence, it comes out looking quite different from the tight, logical discipline of the academic statistician. Theirs is not an invalid view. In teaching statistics, I have the most success when I am able to see the subject from a nonstatistician's angle. The cartoons offer some very perceptive nonstatistical views of statistics.

#### Supplements to the Text

A study guide, prepared by Professor Carol Diminnie and myself, is available as a supplement to *Business Statistics*. This book contains a variety of study suggestions and self-examination tools. It also displays detailed solutions to exercises selected from the text and additional exercises prepared for the study guide.

An instructor's manual is available from the publisher. This book

includes chapter teaching suggestions, solutions to the text exercises, discussion of the Appendix B data set questions, and overhead transparency masters based on figures found in the text.

A separate test bank contains objective true-false and multiple choice questions and problems with solutions provided. Special effort is made to coordinate these examination materials with the style of the text to help the instructor construct tests that are compatible with the student's learning.

The data sets described in Appendix B are available from the publisher.

#### Acknowledgments

I wish to thank a number of people whose contributions made possible the completion of this project. The following reviewers provided many valuable comments and suggestions that helped shape the final book:

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Professor Carol Diminnie of Saint Bonaventure University was my coauthor on the Study Guide, and she assisted with proofreading. I am deeply indebted to her for a heroic and timely effort.

On a personal note, I wish to thank my economist friends Gerry and Pat Welch for demonstrating that it is indeed possible to finish a textbook. I am especially grateful to my parents, who have always stressed the value of education, both as a career and for one's personal fulfillment.

This book would not have been written without the encouragement of my wife Paula. Her love was my greatest joy, and her memory will guide and sustain me always.

Philip G. Enns

## Contents

Par	t I I	Introduction and Descriptive Statistics 1
1.	Data	and Decision Making 2
		Introduction 2
		Populations and Samples 4
	1–2	The Information in Data 7
		Types of Data 8
		Representing Data with Variables 11
	1–3	An Overview of Statistics 12
		Describing and Inferring 13
		The Role of Probability 16
		A Brief History 16
		Exploring and Confirming 17
		The Business of Statistics 18
	1–5	Sources of Business Data* 19
		Finding Secondary Data 20
	1-6	
	1-7	Summing Variables: The Sigma Notation* 25
		Sigma Notation Rules 26
2.	Desci	riptive Statistics: Classifying and Displaying Data 40
	<b>2</b> –1	The Frequency Distribution 41
	2–2	Classifying Quantitative Data 45
		The Data Array 46
		The Frequency Distribution: Choosing the
		Classes 48
		The Frequency Distribution: Class Frequencies 51
		What Does the Frequency Distribution Show? 52
		Modifying the Guidelines 53

<sup>\*</sup> Denotes optional section. This symbol is used throughout when it occurs.

	2–3 2–4	
	2–5	Relative Frequencies and Percentages 63 Comparing Data Sets 65 Relative Frequency and Probability 68
	2–6	
	2–7	
		A Full Solution: The Density Scale 82 When Not to Use Equal Classes 84 Other Graphic Displays 85
3.	Descr	riptive Statistics: Arithmetic Measurements 104
	3–1	
	<i>3</i> – <i>2</i>	Measures of Location: Mean, Median, and
		Mode 106
		The Mean 106
		The Median 107
		Choosing a Measure of Location 108
		The Mode 109
	0.0	The Graphic View 111
	3–3	Measuring Dispersion—The Standard
		Deviation 112
		Population Data 114 Computational Alternatives 114
	3–4	Interpreting the Standard Deviation 116
	0-1	The Bell-Shaped Curve 116
		An Illustration 118
		Standardized Data 120
		The Coefficient of Variation 121
	<i>3</i> – <i>5</i>	Arithmetic Measures in Grouped Data 121
		The Mean of Grouped Data 122
		The Median and Mode for Grouped Data 123
		Graphical View 124
		The Standard Deviation for Grouped Data 124
	9.0	Need for Approximations 126
	3–6	Quantiles* 127 Ountile Magazine of Digneration 120
	3–7	Quantile Measures of Dispersion 129 Some Exploratory Data Techniques* 130

Part II	Probability and Random Variables 149
4. Prob 4-1 4-2	
4-3	Events 155
4-4	Combining Events 163
4–5	
4-6	The Market Control of the Control of
4.7	Tree Diagrams 178 Independent Events 180
4–7	Independence and Cause and Effect 182  Joint Probability of Independent Events 183
4-8	Bayes Rule 184
	200
	rete Random Variables 200
5–1	Random Variable Defined 200 Random Variables and Data 202 Discrete versus Continuous Random Variables 202
<i>5–2</i>	Probability Distributions 204
	Determining a Probability Distribution 206
<i>5–3</i>	Expected Value 207
	The Mean of a Probability Distribution The Standard Deviation of $P(X)$ 209
	The Graphic View 210
5–4	
5–5	015
<i>9–9</i>	How the Binomial Distribution Is Derived 220
	Computing Binomial Probabilities 220
5-6	
	Bernoulli Trials and Sampling 223
	Binomial Distribution Graphs and Expected
	Value <b>224</b>
	The Sample Proportion 227
5–7	• 1 0
<i>5–8</i>	
	A Queuing Example 231

<i>6</i> –1	Introduction 244 The Mean and Standard Deviation 248
<i>6</i> –2	The Mean and Standard Deviation 248 The Normal Distribution 249
	The Standard Normal Transformation 251
6–3	Using the Normal Distribution Table Percentiles for the Normal Distribution 259
<i>6</i> –4	Is the Normal Distribution Really Normal? 264
6–5	Normal Approximation to the Binomial  Distribution 265  Judging the Approximation 268
6–6	The Exponential Distribution* 270 The Forgetful Process 273
Part III	Sampling and Statistical Inference 283
_	oling and Sampling Distributions 284
7–1 7–2	Why Sample? 284 The Random Sample 286
7-2	The Random Sample 286 Sampling with and without Replacement 288 Obtaining a Random Sample 288 The Literary Digest Fiasco 290 Beyond Random Sampling 291
7–3	Parameters and Statistics 293 The Statistic as a Random Variable 295
7–4	The Sampling Distribution of the Mean The Central Limit Theorem 297 A Simulation Example 300 Sampling without Replacement: Finite Populations 303
7–5	Sampling Distributions: Some Extensions       304         Computing Probabilities       304         Sampling When σ Is Unknown       307         Other Sampling Distributions       308
7–6	
	stical Inference: Estimation 322
8–1 8–2	The Purpose of Inference 322 Estimation of Population Parameters 324 Choosing an Estimator 324 Sampling and Nonsampling Error 326

244

6. Continuous Random Variables

Contents	xix
----------	-----

	Describing the Uncertainty: Point and Interval
0.0	Estimation 326
8–3 8–4	Estimation of a Population Mean $327$ Estimating the Mean When $\sigma$ Is Unknown $331$
<i>6</i> –4	Small Samples: $n \le 30$ 332
	Large Samples: $n \ge 30$ 335
8–5	Estimating a Binomial Proportion 336
8-6	Interpreting and Controlling Estimates 337
0 0	Precision, Confidence, and Sample Size 337
	Planning the Sample Size to Estimate $\mu$ 338
	Planning the Sample to Estimate $\pi$ 340
	7
9. Statis	stical Inference: Hypothesis Testing 350
9. Statis	Introduction 350
<i>3</i> –1	The Analogy of the Legal Process 352
9–2	Developing a Strategy 353
	The Rejection Region 355
	Making the Decision 357
	Type I versus Type II Error 358
9–3	
	Relation to Interval Estimation 361
	The <i>P</i> Value of a Test 362
9–4	Tests of a Population Mean: $\sigma$ Unknown 363
	Small Samples: $n \leq 30$ 364
	Large Samples: $n > 30$ 365
	Finite Populations 366
9–5	Tests of a Binomial Proportion 367
9–6	Type II Error and the Power of a Test 370
	The Power of a Test 370
*	
Part IV	Topics in Business Statistics 383
10. Infere	ence Involving Two Populations 384
10-1	Comparing Two Means: Large Independent
	Samples 385
	Testing Hypotheses about $\mu_1 - \mu_2$ 386
	Estimating the Difference $\mu_1 - \mu_2$ 388
10–2	Comparing Two Means: Small Independent
	Samples 389
10–3	Comparing Two Means: Dependent Samples 392
10–4	Comparing Two Proportions 394

	11–1	Multivariate Data 406	
	11–2	Describing Linear Relations 409	
		The Linear Function 411	
		Fitting the Line 414	
	11–3		
		Features of the Least Squares Regression Line 4	21
		Some Cautions 423	
		Exploring the Data 425	
		Uses of Regression Analysis 427	
	11–4		
		Interpreting $s_e$ 429	
	11–5	The commercials of Botter minution and	
		Correlation 430	
		The Coefficient of Determination 431	
		The Coefficient of Correlation 434	
		Relation to Other Descriptive Measures 437	
		Interpreting $r$ and $r^2$ 438	
	<i>11–6</i>	110 1111041 110401 100	
		Point Estimation of the Linear Model 441	
	11–7		
		Interval Estimation of $\beta$ 445	
		Hypothesis Testing of $\beta$ 446	
		Testing Correlation 449	
	11-8		<b>50</b>
		Inference about a Mean Response 450	
		Inference about a Predicted Response 451	
10	N/L145	:-1 D	
12.	Multi	iple Regression 470 Introduction 470	
	12-1		
		The Linear Model 471	
		What Makes the Model Linear? 471	
	10 0	An Illustration 472 Estimation and Prediction 473	
	12-2		
		Least Squares Estimation 473 Interpreting the Multiple Regression	
		Equation 475	
		Multicollinearity 478	
	12-3		
	12-0	SPSS Applied to Real Estate Data 480	
	12-4		
		30 404	

406

11. Regression and Correlation Analysis

		Testing Model Validity: The F Test 485
	12–5 12–6	The F Distribution 486 F Test of Model Significance 487 Predicting Y 488 Examining Individual Coefficients 489 Applied Multiple Regression 491 Sales Forecasting 491 Modeling Consumer Behavior 497
13.	The A	Analysis of Variance 528
	13-1	
	13–2	One-Factor ANOVA 529 Statistical Inference 532
		The $F$ Test 534
	<i>13–3</i>	Randomized Block Design 538 Sums of Squares 538
		Block Inferences 542
	13–4	
14.	14-1 14-2 14-3	The Multinomial Distribution 562 Goodness-of-Fit Tests 567 Fitting a Normal Distribution 567 Contingency Tables 571 A Test of Independence 571 Comparing Multinomial Populations 574
15.	Nonp	parametric Statistics 590
	<i>15–1</i>	Introduction 590
		Advantages and Disadvantages of Nonparametric Methods 591
	<i>15–2</i>	
	15–3	Matched Samples 591 A One-Sample Median Test 595 Large Samples 596 The Sign Test 597 Matched Samples 597
		Hypotheses of the Test 597
		Large Samples 599

	10-4	Test comparing 1 wo
		Independent Samples 600
		Hypotheses of the Test 601
		Large Samples 603
	<i>15–5</i>	Rank Correlation 603
		Interpreting $r_{\rm S}$ 605
		Inferences Using $r_S$ 606
		Large Samples 607
	15 6	
	10-0	Other Nonparametric Methods 607 The Kruskal-Wallis Test 607
		The Friedman Test 608
		Kolmogorov-Smirnov Tests 608
		Runs Tests 608
	15–7	Relative Efficiency of Nonparametric Tests 609
16.		ness and Economic Time Series 622
	<i>16–1</i>	
		Uses of Time Series Analysis 625
	<i>16</i> –2	
		Time Series Components 626
		Classical Time Series Models 630
	<i>16–3</i>	
		Choosing a Trend Equation: The Method of Least
		Squares 632
		Trend Model Performance 636
		Forecasting Trend 639
	16-4	
	10 1	Couldn't Oto
		Computing Seasonal Effects $640$ Estimating $Y_T \cdot C$ $641$
		Eliminating $Y_T \cdot C$ 644
		Eliminating $I_T$ 645
		Adjusting the Seasonals 645
	16 5	Using Seasonal Indexes 647
	10-3	Business Cycles 650
		Business Cycle Indicators 652
		••
17.		Numbers 664
	17–1	Types and Uses of Index Numbers 664
		Types of Index Comparisons 665
	<i>17–2</i>	The Price Index 666
		The Price Relative 666

The Weighted-Aggregates Price Index 667 Comparing Index Numbers 17-3 Using Index Numbers 671 Measuring Change Deflating a Time Series 671 672 Monetary Purchasing Power 17-4 The Consumer Price Index 673 673 Background of the CPI Uses of the CPI 677 Problems with the CPI Solutions to Odd-Numbered Exercises 688 Glossary of Terms 734 Appendix A: Statistical Tables Table A-1 Individual Probabilities of the Binomial Distribution  $P(X) = \binom{n}{x} \pi^{X} (1 - \pi)^{n-X}$ 744 Table A-2 Poisson Probability Distribution  $P(X) = \frac{\mu^X e^{-\mu}}{X!}$ 747 Table of Areas from Mean to Distances Table A-3Z from Mean for Normal Probability Distribution 753 Values of  $e^{-\mu}$ 754 Table A-4 Table A-5 The t Distribution 755 Critical Values of the F Distribution Table A-6 at a 5 Percent Level of Significance,  $\alpha = 0.05$ 756 Critical Values of the F Distribution at a 1 Percent Level of Significance,  $\alpha = 0.01$ 757 Percentiles for the Chi-Square Table A-7 Distribution 758 Table A-8 Critical Values of the Wilcoxon Signed Rank Test Statistic 759