

海外优秀数学类教材系列丛书

THOMSON

影印版

Calculus (Fifth Edition)

微积分 (第5版)

(上册)

□ James Stewart



高等教育出版社
Higher Education Press

0172
Y41D=2

影印版

Calculus

(Fifth Edition)

微积分 (第5版)(上册)

James Stewart

McMaster University



高等教育出版社
Higher Education Press

图字 01-2003-6454 号

James Stewart

Calculus: Early Transcendentals, fifth Edition.

ISBN:0-534-39321-7

Copyright©2003 by Brooks/Cole, a division of Thomson Learning

Original language published by Thomson Learning (a division of Thomson Learning Asia Pte Ltd).

All Rights reserved. 本书原版由汤姆森学习出版集团出版。版权所有,盗印必究。

Higher Education Press is authorized by Thomson Learning to publish and distribute exclusively this English language reprint edition. This edition is authorized for sale in the People's Republic of China only (excluding Hong Kong, Macao SAR and Taiwan).

Unauthorized export of this edition is a violation of the Copyright Act. No part of this publication may be reproduced or distributed by any means, or stored in a database or retrieval system, without the prior written permission of the publisher.

本书英文影印版由汤姆森学习出版集团授权高等教育出版社独家出版发行。此版本仅限在中华人民共和国境内(不包括中国香港、澳门特别行政区及中国台湾)销售。未经授权的本书出口将被视为违反版权法的行为。未经出版者预先书面许可,不得以任何方式复制或发行本书的任何部分。

981-254-456-9

图书在版编目(CIP)数据

微积分.上册=Calculus:第5版/(加)史迪沃特
(Stewart,J.)编著.一影印本.一北京:高等教育出版社,2004.7

(海外优秀数学类教材系列丛书)

ISBN 7-04-014003-9

I.微... II.史... III.微积分-高等学校-教材
-英文 IV.0172

中国版本图书馆CIP数据核字(2004)第036386号

出版发行 高等教育出版社
社 址 北京市西城区德外大街4号
邮政编码 100011
总 机 010-82028899

购书热线 010-64054588
免费咨询 800-810-0598
网 址 <http://www.hep.edu.cn>
<http://www.hep.com.cn>

经 销 新华书店北京发行所
印 刷 北京中科印刷有限公司

开 本 889×1194 1/16
印 张 45.5
字 数 960 000

版 次 2004年7月第1版
印 次 2004年7月第1次印刷
定 价 60.00元(含光盘2张)

本书如有缺页、倒页、脱页等质量问题,请到所购图书销售部门联系调换。

版权所有 侵权必究

PREFACE

A great discovery solves a great problem but there is a grain of discovery in the solution of any problem. Your problem may be modest; but if it challenges your curiosity and brings into play your inventive faculties, and if you solve it by your own means, you may experience the tension and enjoy the triumph of discovery.

GEORGE POLYA

The art of teaching, Mark Van Doren said, is the art of assisting discovery. I have tried to write a book that assists students in discovering calculus—both for its practical power and its surprising beauty. In this edition, as in the first four editions, I aim to convey to the student a sense of the utility of calculus and develop technical competence, but I also strive to give some appreciation for the intrinsic beauty of the subject. Newton undoubtedly experienced a sense of triumph when he made his great discoveries. I want students to share some of that excitement.

The emphasis is on understanding concepts. I think that nearly everybody agrees that this should be the primary goal of calculus instruction. In fact, the impetus for the current calculus reform movement came from the Tulane Conference in 1986, which formulated as their first recommendation:

Focus on conceptual understanding.

I have tried to implement this goal through the *Rule of Three*: “Topics should be presented geometrically, numerically, and algebraically.” Visualization, numerical and graphical experimentation, and other approaches have changed how we teach conceptual reasoning in fundamental ways. More recently, the Rule of Three has been expanded to become the *Rule of Four* by emphasizing the verbal, or descriptive, point of view as well.

In writing the fifth edition my premise has been that it is possible to achieve conceptual understanding and still retain the best traditions of traditional calculus. The book contains elements of reform, but within the context of a traditional curriculum. (Instructors who prefer a more streamlined curriculum should look at my book *Calculus: Concepts and Contexts, Second Edition*.)

|||| What's New in the Fifth Edition

By way of preparing to write the fifth edition of this text, I spent a year teaching calculus from the fourth edition at the University of Toronto. I listened carefully to my students' questions and my colleagues' suggestions. And as I prepared each lecture I sometimes realized that an additional example was needed, or a sentence could be clarified, or a section could use a few more exercises of a certain type. In addition, I paid attention to the suggestions sent to me by many users and to the comments of the reviewers.

An unusual source of new problems was a phone call I received from a friend of mine, Richard Armstrong. Richard is a partner in an engineering consulting firm and advises

clients who build hospitals and hotels. He told me that, in certain parts of the world, sprinkler systems for large buildings are supplied with water by tanks located on the roofs of the buildings. Of course he knew that the water pressure decreases as the water level decreases, but he needed to be able to quantify this effect so his clients could guarantee a certain pressure for a certain period of time. I told him how he could solve his problem by solving a separable differential equation, but it occurred to me that his problem could be developed into a rather nice project when combined with other ideas. (See the project on page 609).

The structure of *Calculus, Early Transcendentals, Fifth Edition*, remains largely unchanged, but there are hundreds of improvements, small and large:

- The review of inverse trigonometric functions has been moved from an appendix to Section 1.6.
- Two sections in Chapter 10 have been combined.
- I have rewritten Section 12.2 to give more prominence to the geometric description of vectors.
- New phrases and margin notes have been added to clarify the exposition.
- A number of pieces of art have been redrawn.
- The data in examples and exercises have been updated to be more timely.
- Examples have been added. For instance, I added the new Example 1 in Section 5.3 (page 394) because students have a tough time grasping the idea of a function defined by an integral with a variable limit of integration. I think it helps to look at Example 1 before considering the Fundamental Theorem of Calculus.
- Extra steps have been provided in some of the existing examples.
- More than 25% of the exercises in each chapter are new. Here are a few of my favorites:

Exercise	Page	Exercise	Page	Exercise	Page
2.8.34	164	3.9.55	256	4.4.74	315
5.4.52	412	7.7.36	529	9.1.11–12	592
10.3.47–48	678	11.9.40	760	11.12.35	784
13.3.32–34	869	14.3.5–6	920	14.5.15–16	938

I've also added new problems to the Problems Plus sections. See, for instance, Problems 20 and 21 on page 277, Problems 9 and 10 on page 585, and Problems 20 and 22 on page 791.



- Five new projects have been added. The one on page 243 asks students to design a roller coaster so the track is smooth at transition points. The project on page 554, the idea for which I thank Larry Riddle, is actually a contest in which the winning curve has the smallest arc length (within a certain class of curves).
- A CD called *Tools for Enriching Calculus (TEC)* is included with every copy of the fifth edition. See the description on page xvii.
- Conscious of the need to control the size of the book, I've put additional topics (with exercises) on the revamped web site www.stewartcalculus.com (see the description on page xvii) rather than in the text itself. These include the new topics Fourier Series and Formulas for the Remainder Term in Taylor Series, as well as topics that appeared in previous editions: Review of Basic Algebra, Rotation of Axes, and Lies My Calculator and Computer Told Me.

||| Features

- Conceptual Exercises** The most important way to foster conceptual understanding is through the problems that we assign. To that end I have devised various types of new problems. Some exercise sets begin with requests to explain the meanings of the basic concepts of the section. (See, for instance, the first few exercises in Sections 2.2, 2.5, 2.7, 11.2, 14.2, and 14.3.) Similarly, all the review sections begin with a *Concept Check* and a *True-False Quiz*. Other exercises test conceptual understanding through graphs or tables (see Exercises 2.8.1–3, 2.9.35–38, 3.7.1–4, 9.1.11–12, 10.1.24–27, 11.10.2, 13.2.1–2, 13.3.29–33, 14.1.1–2, 14.1.30–36, 14.3.3–8, 14.6.1–2, 14.7.3–4, 15.1.5–10, 16.1.11–18, 16.2.17–18, and 16.3.1–2).
- Another type of exercise uses verbal description to test conceptual understanding (see Exercises 2.5.8, 2.9.48, 4.3.59–60, and 7.8.67). I particularly value problems that combine and compare graphical, numerical, and algebraic approaches (see Exercises 2.6.35–36, 3.3.23, and 9.5.2).
- Graded Exercise Sets** Each exercise set is carefully graded, progressing from basic conceptual exercises and skill-development problems to more challenging problems involving applications and proofs.
- Real-World Data** My assistants and I spent a great deal of time looking in libraries, contacting companies and government agencies, and searching the Internet for interesting real-world data to introduce, motivate, and illustrate the concepts of calculus. As a result, many of the examples and exercises deal with functions defined by such numerical data or graphs. See, for instance, Figures 1, 11, and 12 in Section 1.1 (seismograms from the Northridge earthquake), Exercise 2.9.36 (percentage of the population under age 18), Exercise 5.1.14 (velocity of the space shuttle *Endeavour*), and Figure 4 in Section 5.4 (San Francisco power consumption). Functions of two variables are illustrated by a table of values of the wind-chill index as a function of air temperature and wind speed (Example 2 in Section 14.1). Partial derivatives are introduced in Section 14.3 by examining a column in a table of values of the heat index (perceived air temperature) as a function of the actual temperature and the relative humidity. This example is pursued further in connection with linear approximations (Example 3 in Section 14.4). Directional derivatives are introduced in Section 14.6 by using a temperature contour map to estimate the rate of change of temperature at Reno in the direction of Las Vegas. Double integrals are used to estimate the average snowfall in Colorado on December 24, 1982 (Example 4 in Section 15.1). Vector fields are introduced in Section 16.1 by depictions of actual velocity vector fields showing San Francisco Bay wind patterns.
- Projects** One way of involving students and making them active learners is to have them work (perhaps in groups) on extended projects that give a feeling of substantial accomplishment when completed. I have included four kinds of projects: *Applied Projects* involve applications that are designed to appeal to the imagination of students. The project after Section 9.3 asks whether a ball thrown upward takes longer to reach its maximum height or to fall back to its original height. (The answer might surprise you.) The project after Section 14.8 uses Lagrange multipliers to determine the masses of the three stages of a rocket so as to minimize the total mass while enabling the rocket to reach a desired velocity. *Laboratory Projects* involve technology; the one following Section 10.2 shows how to use Bézier curves to design shapes that represent letters for a laser printer. *Writing Projects* ask students to compare present-day methods with those of the founders of calculus—Fermat’s method for finding tangents, for instance. Suggested references are supplied. *Discovery Projects* anticipate results to be discussed later or encourage discovery through pattern recognition (see the one following Section 7.6). Others explore aspects of geometry: tetra-

hedra (after Section 12.4), hyperspheres (after Section 15.7), and intersections of three cylinders (after Section 15.8). Additional projects can be found in the *Instructor's Guide* (see, for instance, Group Exercise 5.1: Position from Samples) and also in the *CalcLabs* supplements.

Problem Solving Students usually have difficulties with problems for which there is no single well-defined procedure for obtaining the answer. I think nobody has improved very much on George Polya's four-stage problem-solving strategy and, accordingly, I have included a version of his problem-solving principles following Chapter 1. They are applied, both explicitly and implicitly, throughout the book. After the other chapters I have placed sections called *Problems Plus*, which feature examples of how to tackle challenging calculus problems. In selecting the varied problems for these sections I kept in mind the following advice from David Hilbert: "A mathematical problem should be difficult in order to entice us, yet not inaccessible lest it mock our efforts." When I put these challenging problems on assignments and tests I grade them in a different way. Here I reward a student significantly for ideas toward a solution and for recognizing which problem-solving principles are relevant.

Technology The availability of technology makes it not less important but more important to clearly understand the concepts that underlie the images on the screen. But, when properly used, graphing calculators and computers are powerful tools for discovering and understanding those concepts. This textbook can be used either with or without technology and I use two special symbols to indicate clearly when a particular type of machine is required. The icon  indicates an exercise that definitely requires the use of such technology, but that is not to say that it can't be used on the other exercises as well. The symbol  is reserved for problems in which the full resources of a computer algebra system (like Derive, Maple, Mathematica, or the TI-89/92) are required. But technology doesn't make pencil and paper obsolete. Hand calculation and sketches are often preferable to technology for illustrating and reinforcing some concepts. Both instructors and students need to develop the ability to decide where the hand or the machine is appropriate.

Tools for Enriching™ Calculus The CD-ROM called *TEC* included with every copy of this book is a companion to the text and is intended to enrich and complement its contents. Developed by Harvey Keynes at the University of Minnesota and Dan Clegg at Palomar College, *TEC* uses a discovery and exploratory approach. In sections of the book where technology is particularly appropriate, marginal icons direct students to *TEC* modules that provide a laboratory environment in which they can explore the topic in different ways and at different levels. Instructors can choose to become involved at several different levels, ranging from simply encouraging students to use the modules for independent exploration, to assigning specific exercises from those included with each module, or to creating additional exercises, labs, and projects that make use of the modules.

TEC also includes *homework hints* for representative exercises (usually odd-numbered) in every section of the text, indicated by printing the exercise number in red. These hints are usually presented in the form of questions and try to imitate an effective teaching assistant by functioning as a silent tutor. They are constructed so as not to reveal any more of the actual solution than is minimally necessary to make further progress.

Web Site: www.stewartcalculus.com

This site has been renovated and now includes the following.

- Algebra Review, with tutorial
- Additional Topics (complete with exercise sets):
 - Fourier Series, Formulas for the Remainder Term in Taylor Series,
 - Rotation of Axes, Lies My Calculator and Computer Told Me

- Drill exercises that appeared in previous editions, together with their solutions
- Problems Plus from prior editions
- Links, for particular topics, to outside web resources
- History of Mathematics, with links to the better historical web sites
- Downloadable versions of *CalcLabs* for Derive and TI graphing calculators

||| Content

A Preview of Calculus	The book begins with an overview of the subject and includes a list of questions to motivate the study of calculus.
1 • Functions and Models	From the beginning, multiple representations of functions are stressed: verbal, numerical, visual, and algebraic. A discussion of mathematical models leads to a review of the standard functions, including exponential and logarithmic functions, from these four points of view.
2 • Limits and Derivatives	The material on limits is motivated by a prior discussion of the tangent and velocity problems. Limits are treated from descriptive, graphical, numerical, and algebraic points of view. Section 2.4, on the precise ϵ - δ definition of a limit, is an optional section. Sections 2.8 and 2.9 deal with derivatives (especially with functions defined graphically and numerically) before the differentiation rules are covered in Chapter 3. Here the examples and exercises explore the meanings of derivatives in various contexts.
3 • Differentiation Rules	All the basic functions, including exponential, logarithmic, and inverse trigonometric functions, are differentiated here. When derivatives are computed in applied situations, students are asked to explain their meanings.
4 • Applications of Differentiation	The basic facts concerning extreme values and shapes of curves are deduced from the Mean Value Theorem. Graphing with technology emphasizes the interaction between calculus and calculators and the analysis of families of curves. Some substantial optimization problems are provided, including an explanation of why you need to raise your head 42° to see the top of a rainbow.
5 • Integrals	The area problem and the distance problem serve to motivate the definite integral, with sigma notation introduced as needed. (Full coverage of sigma notation is provided in Appendix E.) Emphasis is placed on explaining the meanings of integrals in various contexts and on estimating their values from graphs and tables.
6 • Applications of Integration	Here I present the applications of integration—area, volume, work, average value—that can reasonably be done without specialized techniques of integration. General methods are emphasized. The goal is for students to be able to divide a quantity into small pieces, estimate with Riemann sums, and recognize the limit as an integral.
7 • Techniques of Integration	All the standard methods are covered but, of course, the real challenge is to be able to recognize which technique is best used in a given situation. Accordingly, in Section 7.5, I present a strategy for integration. The use of computer algebra systems is discussed in Section 7.6.
8 • Further Applications of Integration	Here are the applications of integration—arc length and surface area—for which it is useful to have available all the techniques of integration, as well as applications to biology,

economics, and physics (hydrostatic force and centers of mass). I have also included a section on probability. There are more applications here than can realistically be covered in a given course. Instructors should select applications suitable for their students and for which they themselves have enthusiasm.

- | | |
|--|---|
| 9 • Differential Equations | Modeling is the theme that unifies this introductory treatment of differential equations. Direction fields and Euler's method are studied before separable and linear equations are solved explicitly, so that qualitative, numerical, and analytic approaches are given equal consideration. These methods are applied to the exponential, logistic, and other models for population growth. The first five or six sections of this chapter serve as a good introduction to first-order differential equations. An optional final section uses predator-prey models to illustrate systems of differential equations. |
| 10 • Parametric Equations and Polar Coordinates | The sections on areas and tangents for parametric curves and arc length and surface area have been streamlined and combined as <i>Calculus with Parametric Curves</i> . Such curves are well suited to laboratory projects; the two presented here involve families of curves and Bézier curves. A brief treatment of conic sections in polar coordinates prepares the way for Kepler's Laws in Chapter 13. |
| 11 • Infinite Sequences and Series | The convergence tests have intuitive justifications (see page 723) as well as formal proofs. Numerical estimates of sums of series are based on which test was used to prove convergence. The emphasis is on Taylor series and polynomials and their applications to physics. Error estimates include those from graphing devices. |
| 12 • Vectors and the Geometry of Space | The material on three-dimensional analytic geometry and vectors is divided into two chapters. Chapter 12 deals with vectors, the dot and cross products, lines, planes, surfaces, and cylindrical and spherical coordinates. |
| 13 • Vector Functions | This chapter covers vector-valued functions, their derivatives and integrals, the length and curvature of space curves, and velocity and acceleration along space curves, culminating in Kepler's laws. |
| 14 • Partial Derivatives | Functions of two or more variables are studied from verbal, numerical, visual, and algebraic points of view. In particular, I introduce partial derivatives by looking at a specific column in a table of values of the heat index (perceived air temperature) as a function of the actual temperature and the relative humidity. Directional derivatives are estimated from contour maps of temperature, pressure, and snowfall. |
| 15 • Multiple Integrals | Contour maps and the Midpoint Rule are used to estimate the average snowfall and average temperature in given regions. Double and triple integrals are used to compute probabilities, surface areas, and (in projects) volumes of hyperspheres and volumes of intersections of three cylinders. |
| 16 • Vector Calculus | Vector fields are introduced through pictures of velocity fields showing San Francisco Bay wind patterns. The similarities among the Fundamental Theorem for line integrals, Green's Theorem, Stokes' Theorem, and the Divergence Theorem are emphasized. |
| 17 • Second-Order Differential Equations | Since first-order differential equations are covered in Chapter 9, this final chapter deals with second-order linear differential equations, their application to vibrating springs and electric circuits, and series solutions. |

||| Ancillaries

Calculus, Early Transcendentals, Fifth Edition, is supported by a complete set of ancillaries developed under my direction. Each piece has been designed to enhance student understanding and to facilitate creative instruction. The tables on pages xxiv–xxv describe each of these ancillaries.

||| Acknowledgments

The preparation of this and previous editions has involved much time spent reading the reasoned (but sometimes contradictory) advice from a large number of astute reviewers. I greatly appreciate the time they spent to understand my motivation for the approach taken. I have learned something from each of them.

Fifth Edition Reviewers

Martina Bode,
Northwestern University
Philip L. Bowers,
Florida State University
Scott Chapman,
Trinity University
Charles N. Curtis,
Missouri Southern State College
John W. Davenport,
Georgia Southern University
Elias Deeba,
*University of Houston–
Downtown*
Greg Dresden,
Washington and Lee University
Martin Erickson,
Truman State University
Laurene V. Fausett,
Georgia Southern University
Norman Feldman,
Sonoma State University
José D. Flores,
The University of South Dakota
Kevin A. Grasse,
The University of Oklahoma
Howard B. Hamilton,
*California State University,
Sacramento*

Gary W. Harrison,
College of Charleston
Randall R. Holmes,
Auburn University
James F. Hurley,
University of Connecticut
Matthew A. Isom,
Arizona State University
Zsuzsanna M. Kadas,
St. Michael's College
Frederick W. Keene,
Pasadena City College
Robert L. Kelley,
University of Miami
John C. Lawlor,
University of Vermont
Christopher C. Leary,
*State University of New York
at Geneseo*
William O. Martin,
*North Dakota
State University*
Gerald Y. Matsumoto,
American River College
Gordon Melrose,
Old Dominion University
Michael Montaña,
Riverside Community College

Hussain S. Nur,
*California State University,
Fresno*
Mike Penna,
*Indiana University–Purdue
University Indianapolis*
John Ringland,
*State University of New York
at Buffalo*
E. Arthur Robinson, Jr.,
The George Washington University
Rob Root
Lafayette College
Teresa Morgan Smith,
Blinn College
Donald W. Solomon,
*University of Wisconsin–
Milwaukee*
Kristin Stoley,
Blinn College
Paul Xavier Uhlig,
*St. Mary's University,
San Antonio*
Dennis H. Wortman,
*University of Massachusetts,
Boston*
Xian Wu,
University of South Carolina

Previous Edition Reviewers

- B. D. Aggarwala,
University of Calgary
- John Alberghini,
Manchester Community College
- Michael Albert,
Carnegie-Mellon University
- Daniel Anderson,
University of Iowa
- Donna J. Bailey,
Northeast Missouri State University
- Wayne Barber,
Chemeketa Community College
- Neil Berger,
University of Illinois, Chicago
- David Berman,
University of New Orleans
- Richard Biggs,
University of Western Ontario
- Robert Blumenthal,
Oglethorpe University
- Barbara Bohannon,
Hofstra University
- Jay Bourland,
Colorado State University
- Stephen W. Brady,
Wichita State University
- Michael Breen,
Tennessee Technological University
- Stephen Brown
- Robert N. Bryan,
University of Western Ontario
- David Buchthal,
University of Akron
- Jorge Cassio,
Miami-Dade Community College
- Jack Ceder,
*University of California,
Santa Barbara*
- James Choike,
Oklahoma State University
- Barbara Cortzen,
DePaul University
- Carl Cowen,
Purdue University
- Philip S. Croke,
Vanderbilt University
- Daniel Cyphert,
Armstrong State College
- Robert Dahlin
- Gregory J. Davis,
*University of Wisconsin—
Green Bay*
- Daniel DiMaria,
Suffolk Community College
- Seymour Ditor,
University of Western Ontario
- Daniel Drucker,
Wayne State University
- Kenn Dunn,
Dalhousie University
- Dennis Dunninger,
Michigan State University
- Bruce Edwards,
University of Florida
- David Ellis,
San Francisco State University
- John Ellison,
Grove City College
- Garret Etgen,
University of Houston
- Theodore G. Faticoni,
Fordham University
- Newman Fisher,
San Francisco State University
- William Francis,
*Michigan Technological
University*
- James T. Franklin,
Valencia Community College, East
- Stanley Friedlander,
Bronx Community College
- Patrick Gallagher,
Columbia University—New York
- Paul Garrett,
*University of Minnesota—
Minneapolis*
- Frederick Gass,
Miami University of Ohio
- Bruce Gilligan,
University of Regina
- Matthias K. Gobbert,
*University of Maryland,
Baltimore County*
- Gerald Goff,
Oklahoma State University
- Stuart Goldenberg,
*California Polytechnic
State University*
- John A. Graham,
*Buckingham Browne &
Nichols School*
- Richard Grassl,
University of New Mexico
- Michael Gregory,
University of North Dakota
- Charles Groetsch,
University of Cincinnati
- Salim M. Haïdar,
Grand Valley State University
- D. W. Hall,
Michigan State University
- Robert L. Hall,
*University of Wisconsin—
Milwaukee*
- Darel Hardy,
Colorado State University
- Melvin Hausner,
*New York University/
Courant Institute*
- Curtis Herink,
Mercer University
- Russell Herman,
*University of North Carolina
at Wilmington*
- Allen Hesse,
Rochester Community College
- Gerald Janusz,
*University of Illinois at
Urbana-Champaign*
- John H. Jenkins,
*Embry-Riddle Aeronautical
University, Prescott Campus*
- Clement Jeske,
*University of Wisconsin,
Platteville*
- Carl Jockusch,
*University of Illinois at
Urbana-Champaign*
- Jan E. H. Johansson,
University of Vermont
- Jerry Johnson,
Oklahoma State University
- Matt Kaufman
- Matthias Kowski,
Arizona State University
- Virgil Kowalik,
Texas A&I University

Kevin Kreider,
University of Akron
 Leonard Krop,
DePaul University
 Mark Krusemeyer,
Carleton College
 David Leeming,
University of Victoria
 Sam Lesseig,
*Northeast Missouri
 State University*
 Phil Locke,
University of Maine
 Joan McCarter,
Arizona State University
 Phil McCartney,
Northern Kentucky University
 Igor Malyshev,
San Jose State University
 Larry Mansfield,
Queens College
 Mary Martin,
Colgate University
 Nathaniel F. G. Martin,
University of Virginia
 Tom Metzger,
University of Pittsburgh
 Teri Jo Murphy,
University of Oklahoma
 Richard Nowakowski,
Dalhousie University
 Wayne N. Palmer,
Utica College
 Vincent Panico,
University of the Pacific

F. J. Papp,
University of Michigan–Dearborn
 Mark Pinsky,
Northwestern University
 Lothar Redlin,
The Pennsylvania State University
 Tom Rishel,
Cornell University
 Joel W. Robbin,
*University of Wisconsin–
 Madison*
 Richard Rockwell,
Pacific Union College
 Richard Ruedemann,
Arizona State University
 David Ryeburn,
Simon Fraser University
 Richard St. Andre,
Central Michigan University
 Ricardo Salinas,
San Antonio College
 Robert Schmidt,
South Dakota State University
 Eric Schreiner,
Western Michigan University
 Mihr J. Shah,
Kent State University–Trumbull
 Theodore Shifrin,
University of Georgia
 Wayne Skrapek,
University of Saskatchewan
 Larry Small,
Los Angeles Pierce College
 William Smith,
University of North Carolina

Edward Spitznagel,
Washington University
 Joseph Stampfli,
Indiana University
 M. B. Tavakoli,
Chaffey College
 Stan Ver Nooy,
University of Oregon
 Andrei Verona,
*California State University–
 Los Angeles*
 Russell C. Walker,
Carnegie Mellon University
 William L. Walton,
McCallie School
 Jack Weiner,
University of Guelph
 Alan Weinstein,
*University of California,
 Berkeley*
 Theodore W. Wilcox,
*Rochester Institute
 of Technology*
 Steven Willard,
University of Alberta
 Robert Wilson,
University of Wisconsin–Madison
 Jerome Wolbert,
*University of Michigan–
 Ann Arbor*
 Mary Wright,
*Southern Illinois University–
 Carbondale*
 Paul M. Wright,
Austin Community College

In addition, I would like to thank George Bergman, Stuart Goldenberg, Emile LeBlanc, Gerald Leibowitz, Charles Pugh, Marina Ratner, Peter Rosenthal, and Alan Weinstein for their suggestions; Dan Clegg for his research in libraries and on the Internet; Arnold Good for his treatment of optimization problems with implicit differentiation; Al Shenk and Dennis Zill for permission to use exercises from their calculus texts; COMAP for permission to use project material; George Bergman, David Bleecker, Dan Clegg, Victor Kaftal, Anthony Lam, Jamie Lawson, Ira Rosenholtz, Lowell Smylie, and Larry Wallen for ideas for exercises; Dan Drucker for the roller derby project; Tom Farmer, Fred Gass, John Ramsay, Larry Riddle, and Philip Straffin for ideas for projects; Dan Anderson and Dan Drucker for solving the new exercises; and Jeff Cole and Dan Clegg for their careful preparation and proofreading of the answer manuscript. I'm grateful to Jeff Cole for suggesting ways to improve the exercises. Dan Clegg acted as my assistant throughout; he proofread, made suggestions, and contributed many of the new exercises.

In addition, I thank those who have contributed to past editions: Ed Barbeau, Fred Brauer, Andy Bulman-Fleming, Bob Burton, Tom DiCiccio, Garret Etgen, Chris Fisher, Gene Hecht, Harvey Keynes, Kevin Kreider, E. L. Koh, Zdislav Kovarik, David Leep, Lothar Redlin, Carl Riehm, Doug Shaw, and Saleem Watson.

I also thank Stephanie Kuhns, Kathi Townes, and Brian Betsill of TECHarts for their production services and the following Brooks/Cole staff: Kirk Bomont, editorial production project manager; Karin Sandberg, Stephanie Taylor, and Bryan Vann, marketing team; Stacy Green, assistant editor, and Jessica Zimmerman, editorial assistant; Earl Perry, technology project manager, and Jessica Reed, print/media buyer. They have all done an outstanding job.

I have been very fortunate to have worked with some of the best mathematics editors in the business over the past two decades: Ron Munro, Harry Campbell, Craig Barth, Jeremy Hayhurst, Gary Ostedt, and now Bob Pirtle. Bob continues in that tradition of editors who, while offering sound advice and ample assistance, trust my instincts and allow me to write the books that I want to write.

JAMES STEWART

|||| Ancillaries for Instructors

Instructor's Resource CD-ROM

ISBN 0-534-39340-3

Contains Electronic Instructor's Guide, Electronic Solutions, BCA Testing, Instructions for BCA Homework, and electronic transparencies (CalcLink).

◦ <http://bca.brookscole.com>

Tools for Enriching™ Calculus CD-ROM

by Harvey B. Keynes, James Stewart, and Dan Clegg

ISBN 0-534-39731-X

TEC provides a laboratory environment in which students can explore selected topics. TEC also includes homework hints for representative exercises.

Instructor's Guide

by Douglas Shaw, Harvey B. Keynes, and James Stewart

ISBN 0-534-39334-9

Each section of the main text is discussed from several viewpoints and contains suggested time to allot, points to stress, text discussion topics, core materials for lecture, workshop/discussion suggestions, group work exercises in a form suitable for handout, and suggested homework problems. An electronic version is available on the Instructor's Resource CD-ROM.

Instructor's Guide for AP® Calculus

by Douglas Shaw and Robert Gerver, contributing author

ISBN 0-534-39341-1

Taking the perspective of optimizing preparation for the AP exam, each section of the main text is discussed from several viewpoints and contains suggested time to allot, points to stress, daily quizzes, core materials for lecture, workshop/discussion suggestions, group work exercises in a form suitable for handout, tips for the AP exam, and suggested homework problems.

Complete Solutions Manual

Single Variable Early Transcendentals

by Daniel Anderson, Jeffery A. Cole, and Daniel Drucker

ISBN 0-534-39332-2

Multivariable Early Transcendentals

by Dan Clegg and Barbara Frank

ISBN 0-534-39359-4

Includes worked-out solutions to all exercises in the text.

Printed Test Items

ISBN 0-534-39336-5

Contains multiple-choice and short-answer test items that key directly to the text.



Brooks/Cole Assessment (BCA) Testing

ISBN 0-534-39335-7

Available online or on CD-ROM, browser-based BCA is fully integrated text-specific testing, tutorial, and course management software. With no need for plug-ins or downloads, BCA offers algorithmically generated problem values and machine-graded free response mathematics.

◦ <http://bca.brookscole.com>

Text-Specific Videos

ISBN 0-534-39325-X

Text-specific videotape sets, available at no charge to adopters, consisting of one tape per text chapter. Each tape features a 10- to 20-minute problem-solving lesson for each section of the chapter. Covers both single- and multivariable calculus.

Transparencies by James Stewart

Single Variable ISBN 0-534-39337-3

Multivariable ISBN 0-534-39383-7

Full-color, large-scale sheets of reproductions of material from the text.

|||| Ancillaries for Instructors and Students

Stewart Specialty Web Site

www.stewartcalculus.com

Contents: Algebra Review with tutorial ◦ Additional Topics ◦ Drill exercises ◦ Problems Plus ◦ Web Links ◦ History of Mathematics ◦ Downloadable versions of CalcLabs for Derive and TI graphing calculators



BCA Homework

ISBN 0-534-39380-2

BCA Homework allows instructors to assign machine-gradable homework problems that help students identify where they need additional help. That assistance is available through worked-out solutions that guide students through the steps of problem solving, or via live online tutoring at vMentor. The tutors at this online service will skillfully guide students through a problem, using unique two-way audio and whiteboard features.

◦ <http://bca.brookscole.com>

The Brooks/Cole Mathematics Resource Center Web Site

<http://mathematics.brookscole.com>

When you adopt a Thomson–Brooks/Cole mathematics text, you and your students will have access to a variety of teaching and learning resources. This Web site features everything from

book-specific resources to newsgroups. It's a great way to make teaching and learning an interactive and intriguing experience.

WebTutor™ on WebCT

ISBN 0-534-39328-4

Lecture notes, discussion threads, and quizzes on WebCT.



Journey Through Calculus

by Bill Ralph in conjunction with James Stewart

Student Version ISBN 0-534-26220-1

Instructor's Version ISBN 0-534-36823-9

A Calculus CD-ROM that brings together activities, tutorials, testing, a computer algebra system, and calculus content into one unified environment.

Student Resources



Tools for Enriching™ Calculus CD-ROM

by Harvey B. Keynes, James Stewart, and Dan Clegg

ISBN 0-534-39731-X

TEC provides a laboratory environment in which students can explore selected topics. TEC also includes homework hints for representative exercises.

Interactive Video SkillBuilder CD-ROM

ISBN 0-534-39326-8

Think of it as portable office hours! The Interactive Video Skillbuilder CD-ROM contains more than eight hours of video instruction. The problems worked during each video lesson are shown next to the viewing screen so that students can try working them before watching the solution. To help students evaluate their progress, each section contains a ten-question Web quiz (the results of which can be emailed to the instructor) and each chapter contains a chapter test, with answers to each problem. Also included is MathCue Tutorial software. This dual-platform software presents and scores problems and tutors students by displaying annotated, step-by-step solutions. Problem sets may be customized.

Study Guide

Single Variable Early Transcendentals by Richard St. Andre

ISBN 0-534-39331-4

Multivariable by Richard St. Andre

ISBN 0-534-39358-6

Contains a short list of key concepts, a short list of skills to master, a brief introduction to the ideas of the section, an elaboration of the concepts and skills, including extra worked-out examples, and links in the margin to earlier and later material in the text and Study Guide.

Student Solutions Manual

Single Variable Early Transcendentals

by Daniel Anderson, Jeffery A. Cole, and Daniel Drucker

ISBN 0-534-39333-0

Multivariable

by Dan Clegg and Barbara Frank

ISBN 0-534-39360-8

Provides completely worked-out solutions to all odd-numbered exercises within the text, giving students a way to check their answers and ensure that they took the correct steps to arrive at an answer.

CalcLabs with Maple

Single Variable

by Philip Yasskin, Albert Boggess, David Barrow, Maurice Rahe, Jeffery Morgan, Michael Stecher, Art Belmonte, and Kirby Smith

ISBN 0-534-39370-5

Multivariable

by Philip Yasskin and Art Belmonte

ISBN 0-534-39361-6

CalcLabs with Mathematica

Single Variable by Selwyn Hollis

ISBN 0-534-39371-3

Multivariable by Selwyn Hollis

ISBN 0-534-39362-4

Each of these comprehensive lab manuals will help students learn to effectively use the technology tools available to them. Each lab contains clearly explained exercises and a variety of labs and projects to accompany the text.

A Companion to Calculus

by Dennis Ebersole, Doris Schattschneider, Alicia Sevilla, and Kay Somers

ISBN 0-534-26592-8

Written to improve algebra and problem-solving skills of students taking a calculus course, every chapter in this companion is keyed to a calculus topic, providing conceptual background and specific algebra techniques needed to understand and solve calculus problems related to that topic. It is designed for calculus courses that integrate the review of precalculus concepts or for individual use.

Linear Algebra for Calculus

by Konrad J. Heuvers, William P. Francis, John H. Kuisti, Deborah F. Lockhart, Daniel S. Moak, and Gene M. Ortnor

ISBN 0-534-25248-6

This comprehensive book, designed to supplement the calculus course, provides an introduction to and review of the basic ideas of linear algebra.



TO THE STUDENT


Reading a calculus textbook is different from reading a newspaper or a novel, or even a physics book. Don't be discouraged if you have to read a passage more than once in order to understand it. You should have pencil and paper and calculator at hand to sketch a diagram or make a calculation.


Some students start by trying their homework problems and read the text only if they get stuck on an exercise. I suggest that a far better plan is to read and understand a section of the text before attempting the exercises. In particular, you should look at the definitions to see the exact meanings of the terms. And before you read each example, I suggest that you cover up the solution and try solving the problem yourself. You'll get a lot more from looking at the solution if you do so.


Part of the aim of this course is to train you to think logically. Learn to write the solutions of the exercises in a connected, step-by-step fashion with explanatory sentences—not just a string of disconnected equations or formulas.

The answers to the odd-numbered exercises appear at the back of the book, in Appendix H. Some exercises ask for a verbal explanation or interpretation or description. In such cases there is no single correct way of expressing the answer, so don't worry that you haven't found the definitive answer. In addition, there are often several different forms in which to express a numerical or algebraic answer, so if your answer differs from mine, don't immediately assume you're wrong. For example, if the answer given in the back of the book is $\sqrt{2} - 1$ and you obtain $1/(1 + \sqrt{2})$, then you're right and rationalizing the denominator will show that the answers are equivalent.

The icon  indicates an exercise that definitely requires the use of either a graphing calculator or a computer with graphing software. (Section 1.4 discusses the use of these graphing devices and some of the pitfalls that you may encounter.) But that doesn't mean that graphing devices can't be used to check your work on the other exercises as well. The symbol  is reserved for problems in which the full resources of a computer algebra system (like Derive, Maple, Mathematica, or the TI-89/92) are required.

You will also encounter the symbol , which warns you against committing an error. I have placed this symbol in the margin in situations where I have observed that a large proportion of my students tend to make the same mistake.

The icon  indicates a reference to the CD-ROM *Journey Through Calculus*. The symbols in the margin refer you to the location in *Journey* where a concept is introduced through an interactive exploration or animation.

The CD-ROM *Tools for Enriching Calculus*, which is included with this textbook, is referred to by means of the symbol . It directs you to modules in which you can explore aspects of calculus for which the computer is particularly useful. *TEC* also provides *Homework Hints* for representative exercises that are indicated by printing the exercise number in red: **23**. These homework hints ask you questions that allow you to make progress toward a solution without actually giving you the answer. You need to pursue each hint in an active manner with pencil and paper to work out the details. If a particular hint doesn't enable you to solve the problem, you can click to reveal the next hint.

The other CD-ROM that comes with this book is *Interactive Video Skillbuilder*, which contains videos of instructors explaining two or three of the examples in every section of the text. Also on the CD is a video in which I offer advice on how to succeed in your calculus course.

I recommend that you keep this book for reference purposes after you finish the course. Because you will likely forget some of the specific details of calculus, the book will serve as a useful reminder when you need to use calculus in subsequent courses. And, because this book contains more material than can be covered in any one course, it can also serve as a valuable resource for a working scientist or engineer.

Calculus is an exciting subject, justly considered to be one of the greatest achievements of the human intellect. I hope you will discover that it is not only useful but also intrinsically beautiful.

Cut here and keep for reference

Algebra

Arithmetic Operations

$$a(b + c) = ab + ac$$

$$\frac{a + c}{b} = \frac{a}{b} + \frac{c}{b}$$

$$\frac{a}{b} + \frac{c}{d} = \frac{ad + bc}{bd}$$

$$\frac{\frac{a}{b}}{\frac{c}{d}} = \frac{a}{b} \times \frac{d}{c} = \frac{ad}{bc}$$

Exponents and Radicals

$$x^m x^n = x^{m+n}$$

$$(x^m)^n = x^{mn}$$

$$(xy)^n = x^n y^n$$

$$x^{1/n} = \sqrt[n]{x}$$

$$\sqrt[n]{xy} = \sqrt[n]{x} \sqrt[n]{y}$$

$$\frac{x^m}{x^n} = x^{m-n}$$

$$x^{-n} = \frac{1}{x^n}$$

$$\left(\frac{x}{y}\right)^n = \frac{x^n}{y^n}$$

$$x^{m/n} = \sqrt[n]{x^m} = (\sqrt[n]{x})^m$$

$$\sqrt[n]{\frac{x}{y}} = \frac{\sqrt[n]{x}}{\sqrt[n]{y}}$$

Factoring Special Polynomials

$$x^2 - y^2 = (x + y)(x - y)$$

$$x^3 + y^3 = (x + y)(x^2 - xy + y^2)$$

$$x^3 - y^3 = (x - y)(x^2 + xy + y^2)$$

Binomial Theorem

$$(x + y)^2 = x^2 + 2xy + y^2 \quad (x - y)^2 = x^2 - 2xy + y^2$$

$$(x + y)^3 = x^3 + 3x^2y + 3xy^2 + y^3$$

$$(x - y)^3 = x^3 - 3x^2y + 3xy^2 - y^3$$

$$(x + y)^n = x^n + nx^{n-1}y + \frac{n(n-1)}{2}x^{n-2}y^2$$

$$+ \cdots + \binom{n}{k}x^{n-k}y^k + \cdots + nxy^{n-1} + y^n$$

$$\text{where } \binom{n}{k} = \frac{n(n-1) \cdots (n-k+1)}{1 \cdot 2 \cdot 3 \cdots k}$$

Quadratic Formula

$$\text{If } ax^2 + bx + c = 0, \text{ then } x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

Inequalities and Absolute Value

$$\text{If } a < b \text{ and } b < c, \text{ then } a < c.$$

$$\text{If } a < b, \text{ then } a + c < b + c.$$

$$\text{If } a < b \text{ and } c > 0, \text{ then } ca < cb.$$

$$\text{If } a < b \text{ and } c < 0, \text{ then } ca > cb.$$

$$\text{If } a > 0, \text{ then}$$

$$|x| = a \text{ means } x = a \text{ or } x = -a$$

$$|x| < a \text{ means } -a < x < a$$

$$|x| > a \text{ means } x > a \text{ or } x < -a$$

Geometry

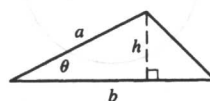
Geometric Formulas

Formulas for area A , circumference C , and volume V :

Triangle

$$A = \frac{1}{2}bh$$

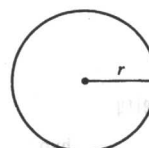
$$= \frac{1}{2}ab \sin \theta$$



Circle

$$A = \pi r^2$$

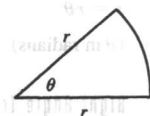
$$C = 2\pi r$$



Sector of Circle

$$A = \frac{1}{2}r^2\theta$$

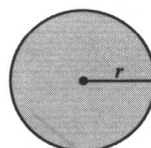
$$s = r\theta \text{ (}\theta \text{ in radians)}$$



Sphere

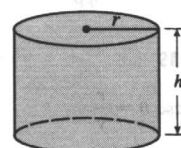
$$V = \frac{4}{3}\pi r^3$$

$$A = 4\pi r^2$$



Cylinder

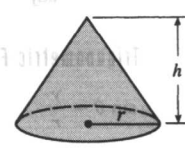
$$V = \pi r^2 h$$



Cone

$$V = \frac{1}{3}\pi r^2 h$$

$$A = \pi r \sqrt{r^2 + h^2}$$



Distance and Midpoint Formulas

Distance between $P_1(x_1, y_1)$ and $P_2(x_2, y_2)$:

$$d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$\text{Midpoint of } \overline{P_1P_2}: \left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2}\right)$$

Lines

Slope of line through $P_1(x_1, y_1)$ and $P_2(x_2, y_2)$:

$$m = \frac{y_2 - y_1}{x_2 - x_1}$$

Point-slope equation of line through $P_1(x_1, y_1)$ with slope m :

$$y - y_1 = m(x - x_1)$$

Slope-intercept equation of line with slope m and y-intercept b :

$$y = mx + b$$

Circles

Equation of the circle with center (h, k) and radius r :

$$(x - h)^2 + (y - k)^2 = r^2$$