Mathematics Applied to Electronics

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This book is designed to be used by those seeking an understanding of mathematics as it is applied to electronics. This may be in a formal setting such as a community college or in a self-study program. *Mathematics Applied to Electronics* is intended to be used by those studying to be specialists in applying the technology of electronics to achieve practical ends.

The electronics curriculum for which this book is written usually needs the support of a large and diverse amount of mathematics. The contents of a mathematics book for electronics is, therefore, based on a "trade off" between a detailed, formal, proof orientation and the need for expediency in developing a broad, general mathematics ability.

The sequence of the chapters and of the topics within each chapter has been planned both to be as vital as possible and to be compatible with the circuits books currently in use. The text provides the reader with a wide exposure to mathematics while still expediting the learning process. This process is enhanced through the use of the calculator, which is an integral part of this text. It is intended that a calculator be used whenever calculations are performed.

The early chapters of the text include selected topics from pre-algebra. The purpose of these initial chapters is twofold: first, to introduce the use of the calculator at the onset of the text; second, to focus attention on specific electronics-related mathematical topics at a level easily comprehended—thus providing the reader with a positive reinforcement in his study of mathematics as applied to electronics. This positive reinforcement may help keep the student in the class long enough for the instructor to provide additional motivation.

These early chapters are followed by several dealing with the mechanics of algebra, including the evaluation of formulas. This series of chapters culminates with a chapter devoted to equations in one unknown.

Each section of theoretical chapters is followed by one or more application chapters. The application chapters

xii Preface serve to reinforce what has been presented previously and to provide the reader with that all-important opportunity to transfer his mathematical skills to electronic concepts.

Interspersed throughout the book are chapters and topics dealing with analytical geometry. These chapters are essential because graphic concepts are important to the electronics industry and so much valuable information is presented in graphical form.

The transcendental functions are covered after the algebraic functions. Included in these chapters are the logarithmic, exponential, and trigonometric functions. These topics are followed by a series of chapters covering the mathematics of alternating current. The text concludes with chapters dealing with math analysis and number systems. These final chapters are directed to those who need a preparation for the study of calculus and computer number systems.

This text is designed to help the reader to teach himself and in this way provides a means of coordinating the instruction in the classroom with the outside assignments. The reader is guided by hundreds of detailed examples, figures, and problems. The use of SI units throughout the text will enable him to make an easy transition to any of the modern circuits books that use the SI metric system.

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Vames Harter Wallace Beitzel

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- 1-7 GENERAL INFORMATION

his chapter is intended to help you to "survive" the educational process. More specifically, it is to help you survive mathematics applied to electronics. An overview of the scope and structure is presented. Assistance is offered in helping you to select a calculator. Then, we let you in on the assumptions that we have made about you.

1-1 "YOU"

"You are the best you there is." Be kind to yourself and read through this chapter. It is written to give you an understanding of the text and how to survive the stress-producing process of becoming educated.

You are from varied backgrounds, of different ages, and have had different experiences, but all of you have a common goal—to learn more about "mathematics applied to electronics." Give yourself a gift and listen to what we have to say to you.

1-2 THE SCOPE AND STRUCTURE OF THE TEXT

We have selected from the field of mathematics those topics that support your career goal in electronics. We have tailored the topics and have streamlined the presentation so that both the special needs of the technology are met and a reasonable level of instruction is maintained.

Scope

The text material starts at the prealgebra level, covers topics in algebra, number notation, units of measurement, and graphing; moves into systems of simultaneous equations, logarithmic functions, trigonometric functions, circular functions, mathematics of phasors, and dc and ac electronic circuits; and concludes with math analysis and number systems.

Structure

A gradual progression from the known to the unknown, from the simple to the complex is achieved in the sequencing of the chapters and the topics within each chapter. The rigorous, meticulous, in-depth pursuit of particular topics common to formal courses in mathematics is not found in this book. A particular topic may be introduced in the early section of the text and then reintroduced at a later time for a more detailed or in-depth application. By using this technique, a reinforcing of the concept is possible.

We have purposefully structured the book so that you will receive a positive feeling about the course you are taking. We have provided you with hundreds of detailed examples to make it possible for you to "learn on your own" and become responsible for educating yourself. If the class you are in is taught in a traditional lecture demonstration manner, then the self-educating aspects of the text may be used to prepare for the next day's lesson and to assist in doing the assigned out-of-class work. In addition, if you have been absent, the material missed may be studied and mastered on an individual basis.

1-3 THE LEARNING PROCESS

The process of becoming educated is usually accompanied by a feeling of uncertainty. Learning a new idea for the first time, coupled with the experience of attending college, is very stressful. Many students face these situations and far too many fail in the first weeks of the semester because they were unable to "adjust" to the learning experience.

We as educators recognize these feelings and have made a conscious effort to keep the stress level down by:

- 1. Selecting only the topics necessary for a rounded exposure to mathematics as it applies to electronics.
- 2. Integrating the scientific calculator into the learning process.
- 3. Designing the presentation so that you may have sufficient time to become familiar with the ideas and learn the concepts.
- 4. Providing detailed examples, tables, illustrations, and explanations; thus sufficient information is presented in a variety of ways so that you will be interested and motivated.
- 5. Presenting the concepts in a clear, uncluttered manner reinforced with examples and graded problem sets.
- 6. Setting the reading level to communicate with you rather than to impress you or your instructor.

1-4 STUDY AND SURVIVAL

How, where, and when you study this text will greatly influence your survival of the educational process. If survival is in your plans, then prepare for class, do your homework, and study for your tests. You can "set yourself up to fail." You can make excuses and be preoccupied with "more important activities." You need to recognize that your education is your responsibility, not the responsibility of the instructor. Your survival in a course is dependent solely upon your choices of how, where, and when you study.

How

Study by reading the material in each section. Work through each example with pencil, paper, and calculator. If you are to become educated, you must be an active participant in the process.

Where

Study where you won't be distracted by friends, noise, or activities. Study where you will have all the materials needed for study. Remember, you must work through and write down the examples and problems. Success in mathematics comes by you *doing*, not by watching someone else.

When

3

Study each day. As a student you have a very limited time with which to work. Most of you have full- or part-time jobs, families, and other commitments, which when coupled with going to school leaves very little time for study. You must understand that much of your education takes place outside the classroom. When you do required assignments that use pencil, paper, and a calculator, you are educating yourself by becoming an active

Surviving Mathematics

participant in the educational process. As a rule, one to three hours of active study are needed to fully learn a new idea. To corrupt an old saying, "an hour a day, keeps drop-out away."

The object of education is to survive the process of becoming educated. The means of survival is through active study, participation, and preparation. Be kind to yourself by choosing to study daily.

1-5 SELECTING A CALCULATOR

First and foremost, purchase a name brand scientific calculator. Don't think that it's too expensive. You are worth it! An inadequate calculator will cost you time and energy that would be better spent elsewhere. Purchase a full-function calculator that is not programmable.

Table 1-1 lists the functions and operations that will be used in this text. As you may see from this list, there is a lot to learn about the calculator. Since the calculator will play a significant role in your educatior, buy a good one. The major manufacturers of calculators have reasonably priced instruments available that have all the functions and operations mentioned in Table 1-1.

Before purchasing, try out various calculators. Talk to the advanced students in your department about their calculators. Look at Table 1-1 to see which functions and operations are required. If you already have a calculator that has the capabilities introduced in Chapters 2 and 3, live with it before buying a new one.

1-6 ASSUMPTIONS MADE BY US ABOUT YOU

We have made several assumptions about you that we would like to share with you.

- ☐ We assume that you have mastered the skills of arithmetic, including adding, subtracting, multiplying, dividing, fractions (both decimal fractions and built-up fractions), and percentage.
- ☐ We assume that you will have a scientific calculator with you while studying this text. We have made provisions in the text for a lesser calculator, but if you are to get the most out of your education, the scientific calculator will be necessary.
- \square We assume that you have an active interest in the field of electronics.
- ☐ We assume that you will work through each example. A great deal of information has been included in the examples.
- ☐ We assume that you will have your owner's guide for your calculator available with your calculator.

1-7 GENERAL INFORMATION

In addition to the previous assumptions, you need to be aware of the following:

☐ The leading zero in decimal numbers as in 0.357 is used to set off the decimal point.