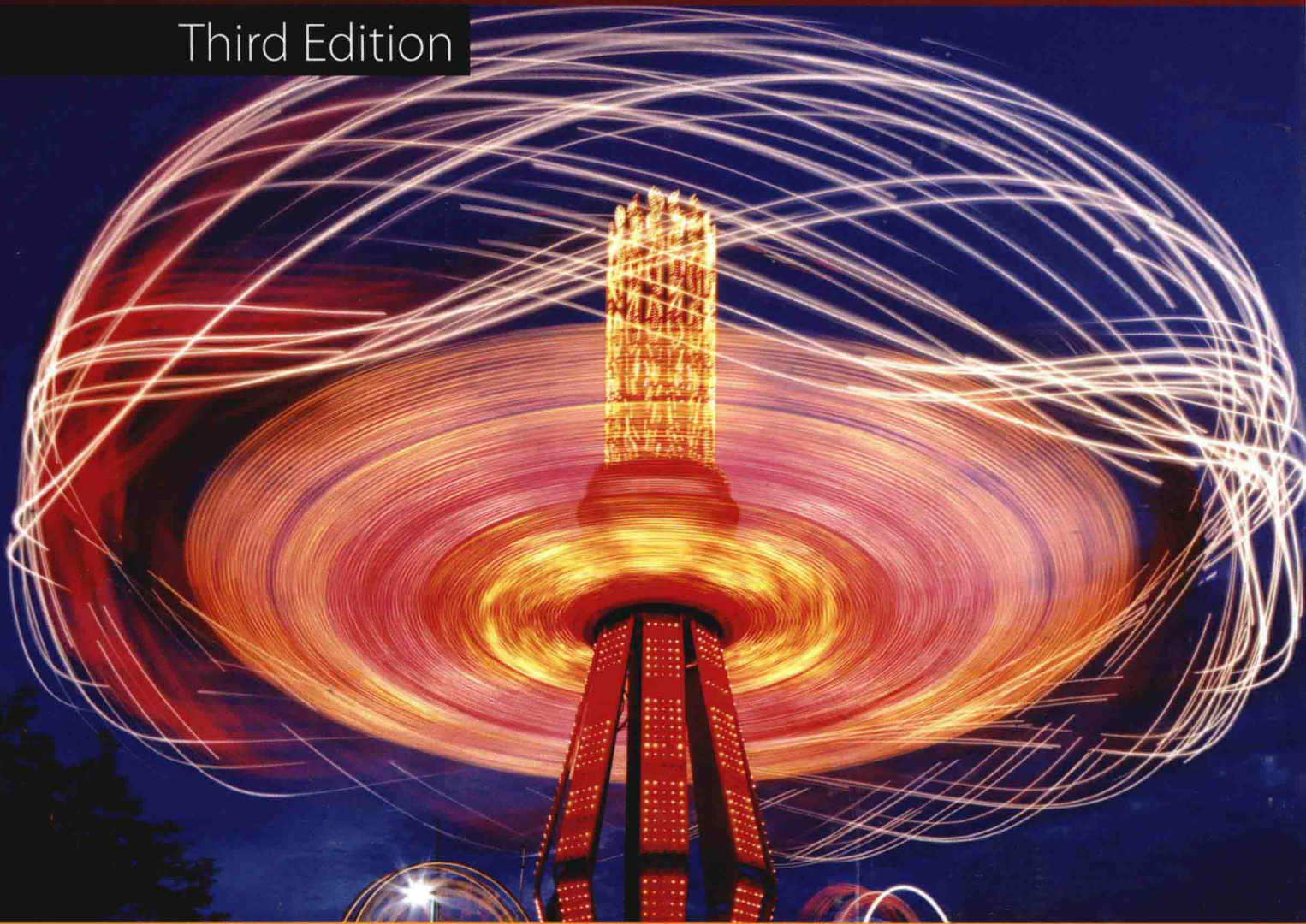


Kinematics, Dynamics, and Design of Machinery

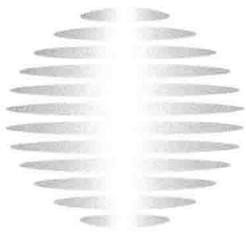
Third Edition



Kenneth J. Waldron • Gary L. Kinzel • Sunil K. Agrawal



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KINEMATICS, DYNAMICS, AND DESIGN OF MACHINERY

Third Edition

Kenneth J. Waldron

Professor Emeritus, Stanford University, USA

Professor, University of Technology, Sydney, Australia

Gary L. Kinzel

Professor Emeritus, The Ohio State University, USA

Sunil K. Agrawal

Professor, Columbia University, USA

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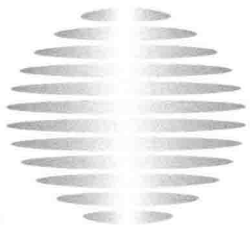
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KINEMATICS,
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About the Companion Website

This book is accompanied by two companion websites: one for students and one for certified instructors.

www.wiley.com/go/waldron/kinematics

The student website includes:

- Movie files for selected linkage animations
- Sample Solidworks files illustrating the use of GCP
- MATLAB[®] programs
- The instructor website (password protected) includes:
 - Solutions manual
 - PowerPoint teaching slides
 - Textbook figures
 - Material in student website

Preface

One of the most amazing aspects of the preparation of this new edition of *Kinematics, Dynamics, and Design of Machinery* is the radical nature of the changes we found to be necessary. The first edition of this work appeared in September 1998, and it is appropriate to reflect on the changes that have occurred during the intervening eighteen years. Although this is a core subject in the mechanical engineering curriculum that has been taught in one form or another throughout the period in which it has been recognized as a technical discipline, there have been many recent changes. In 1998, most production machines were still driven by a single prime mover with their various functions mechanically coordinated. It is true that industrial robots were well established in some industries, notably the manufacture of automobiles, but they were still the exception rather than the rule in utilizing digital coordination of multiple actuators. The first edition of this work broke new ground as an undergraduate text by including chapters on robots and spatial mechanisms. Of course, this picture has totally changed with embedded controllers ubiquitous in our appliances, automobiles, and production machinery. Multiple functions are now much more likely to be coordinated digitally. We have recognized this reality by expanding the material on actuation and creating a new Chapter 17. We have, in that chapter, created an interface to courses on control, and particularly digital control.

It is even truer that the tools available to the machine designer are completely different from what was available in 1998. At that time, computer-aided engineering software was certainly well established, but modern solid modeling packages were not well developed. The constraint management capabilities built into these tools provide a very powerful new capability that renders special purpose mechanism design software—such as that we, ourselves, developed—obsolete. In recognition of this new reality, we have introduced a chapter on Geometric Constraint Programming as Chapter 2, and examples of solving mechanism design problems by this means in Chapters 3, 4, 5, and 6. In addition, Chapter 10 on cam design has been completely revised to base it on methods employing instant centers that are much simpler than the methods we used in the earlier editions. For this reason, although this text covers the same technological territory that the first edition did, it is a very different presentation that takes full advantage of new design technologies.

It is also true that the way in which the subject matter is taught has changed. In the years preceding 1998, this material most often formed the content of a separate course in the mechanical engineering curriculum. Since that time, it has become one element in an overarching discipline of mechanical systems, or *mechatronics*. As such, this material is often interleaved with material from control systems engineering and other related disciplines. To facilitate the use of our material as a component of a mechanical systems course, or in machine design courses, we have attempted to make each chapter as modular as possible. There is a box at the beginning of each chapter stating which material from elsewhere in the book is a prerequisite for successful study of that chapter. It is intended that, if the instructor so desires, he or she can place before their students only the material they intend to cover.

In addition to updating even those sections that are similar to those of Editions 1 and 2, we have added a significant number of new problems, including some open-ended design problems. Supporting material that was included on a CD with Editions 1 and 2 is now available on the companion website maintained by John Wiley & Sons: www.wiley.com/go/waldron/kinematics. It has also been updated as necessary.

We trust that this new presentation will be welcomed as an up-to-the-minute teaching tool and a useful reference for instructors and practitioners in this field. Yes, the new approaches are likely to take instructors who have taught the material for a number of years out of their comfort zone, but we believe the required extra effort to become familiar with the new techniques will prove to be very worthwhile.

In order to take advantage of the Geometric Constraint Programming (GCP) techniques, it is necessary for students to have access to parametric design software that incorporates constraint managers. We believe that tomorrow's students will increasingly be working with solid modeling

packages throughout the curriculum. If this should prove not to be true, inexpensive drawing packages that have constraint managers are readily available.

We would like to express our sincere thanks to the colleagues and students who have contributed to the success of the three editions of this book. For the third edition, we especially acknowledge the help of Profs. James Schmiedeler and Edward Kinzel who co-developed the GCP procedure. Both provided assistance on writing Chapter 2 and parts of Chapter 3, and Jim in particular generously provided his tutorial notes to facilitate the development of the teaching material. We would also like to thank Dr. Matthew Detrick who rewrote the GUI-based kinematic programs for the new versions of MATLAB®. The programs for both the previous and current versions of MATLAB are included in the supplementary material for the book.

KENNETH J. WALDRON

Professor Emeritus, Stanford University

Professor, University of Technology, Sydney

GARY L. KINZEL

Professor Emeritus, The Ohio State University

SUNIL K. AGRAWAL

Professor, Columbia University

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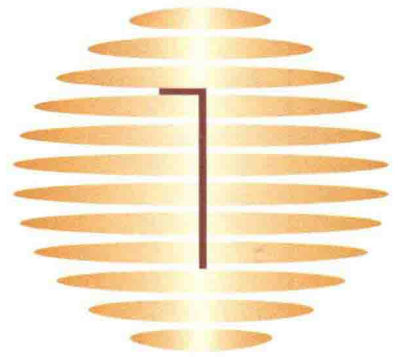
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Introduction



Prerequisite Knowledge Needed for Chapter 1

No prior knowledge is required for this chapter. It is an advantage to have completed undergraduate courses in statics and dynamics, but is certainly not essential.



1.1 HISTORICAL PERSPECTIVE

A mechanism is a machine composed of rigid members that are joined together. Joints permit the members to interact with one another. Portions of the surfaces of the members that contact one another form the joints. The geometries of the contacting surface segments determine the properties of each joint.

Mechanisms are used for diverse purposes. Some are incorporated into items we use every day. Figure 1.1 shows a mechanism whose function is to magnify the force generated by a user squeezing the handles to a very large force exerted by the jaws. It is also designed to lock in place while generating that force, so the handles can be released while the jaws remain clamped on a work piece. This is an example of a planar mechanism because the members of the mechanism all move parallel to a single plane of motion. Many familiar mechanisms have this characteristic. Planar mechanisms are the primary focus of Chapters 3 through 7 of this book. Mechanisms whose primary function is transmitting force, like this one, are discussed in Chapter 14.

Other mechanisms are characterized by points in their members following paths that are curves in space. In Figure 1.2, the leg mechanisms allow the feet to be placed anywhere within a volume of space. Each mechanism is primarily used to generate a straight-line foot trajectory relative to the body, so that the machine can walk at a constant height with uniform speed. Notice that the critical function here is the ability to have a designated point generate a path of specified geometry (a straight line). This is known as a path generation problem. The leg mechanisms used here are called pantographs. A pantograph is a special kind of planar mechanism discussed in Section 8.1.3.

Figure 1.3 is the drive mechanism of an ornithopter, a vehicle that flies by flapping its wings like a bird. Here a spatial trajectory of the entire wing must be generated relative to the body, not just the path of a point, as was the case with Figure 1.2. The wings must flap relative to the body, but they must also rotate about the long axis of the wing at the top of the flap to allow the wing to generate lift. The wing must rotate back (feathering) at the bottom of the flap to minimize air resistance to the upstroke. This is an example of using a mechanism to generate a specified path in space of a whole body (the wing). We call this a motion-generation problem. There are many other ways in which mechanisms are used. Here the wings are flapped by two planar four-bar mechanisms that are geared

FIGURE 1.1

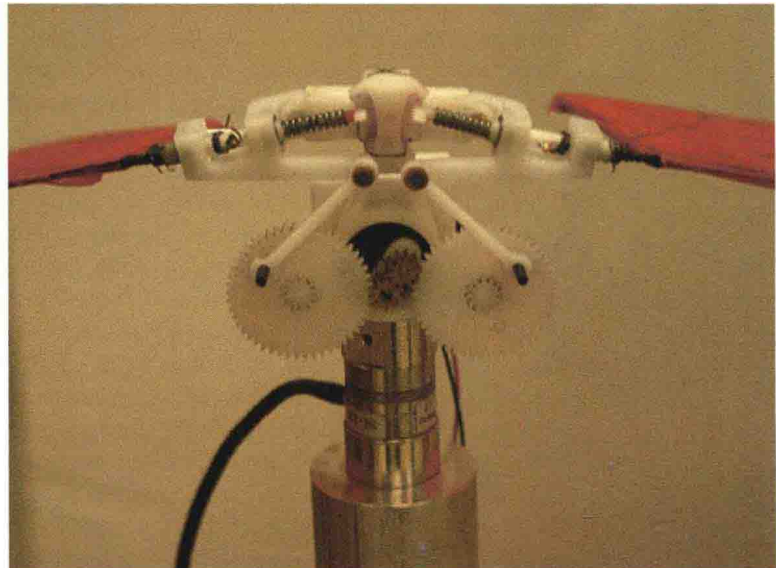
A pair of vice-grip pliers. A planar mechanism that multiplies the force applied by a user to the handles to apply a much greater force at the jaws. The mechanism is also designed to be locked in the closed position.

**FIGURE 1.2**

The Adaptive Suspension Vehicle [7]. Each leg is a planar pantograph mechanism hinged to the body about an axis parallel to the longitudinal axis of the vehicle. The feet can be placed anywhere within a volume of space, so this is, overall, a spatial mechanism. The pantograph mechanism allows the ankle joint to be moved in a straight line relative to the vehicle body by a single hydraulic cylinder.

**FIGURE 1.3**

The drive mechanism of an ornithopter [1]. The mechanism must both flap the wings and rotate them about their long axes at the top and bottom of the flapping motion. A pair of four-bar mechanisms that are geared together accomplish the flapping motion. Cam and follower mechanisms are used to accomplish rotation of the wing at the top and bottom of the flapping motion.



together. The rotation about the wing axis is accomplished by a cam-and-follower mechanism. Cam mechanisms are discussed in Chapter 10.

Other common examples of ways in which mechanisms are used include the suspension of an automobile. A mechanism is used to maintain the wheels in a proper relationship with the body of the vehicle while allowing them to move to accommodate variations in the profile of the road. The suspension functions as a mechanical filter isolating the body of the vehicle and its occupants from bumps in the road.