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MINERAL PROCESSING DESIGN AND OPERATIONS

An Introduction

Second Edition

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AMSTERDAM • BOSTON • HEIDELBERG • LONDON • NEW YORK • OXFORD • PARIS
SAN DIEGO • SAN FRANCISCO • SINGAPORE • SYDNEY • TOKYO

Elsevier
Radarweg 29, PO Box 211, 1000 AE Amsterdam, Netherlands
The Boulevard, Langford Lane, Kidlington, Oxford OX5 1GB, UK
50 Hampshire Street, 5th Floor, Cambridge, MA 02139, USA

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British Library Cataloguing-in-Publication Data

A catalogue record for this book is available from the British Library

Library of Congress Cataloging-in-Publication Data

A catalog record for this book is available from the Library of Congress

ISBN: 978-0-444-63589-1

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Typeset by Thomson Digital

Mineral Processing Design and Operations

*Dedicated to all students interested in the Science and
Technology of Mineral Processing*

*And especially to the memory of late dear Elmie Yan and
also to Chitra Gupta for her patience and forbearance while
preparing this manuscript.*

Preface to the Second Edition

Demand for the first edition of this book prompted us to revise, enlarge and update it. The format of the second edition is in keeping with the first edition. The logic of presentation remains the same.

This edition includes additional chapters on stirrer mills and magnetic separation. The stirred mills for ultrafine grinding of minerals which were developed in the last three decades are described and discussed in detail. These are now being extensively used in large-scale operating circuits for enhanced recovery of minerals from their ore body. Magnetic, conductive and electromagnetic forces for the recovery of minerals with natural or induced magnetic, conducting and semi-conducting properties are a common beneficiation technique particularly in the mineral sands and iron ore industries. The basic elements of atomic theory that help to understand magnetic forces in minerals are explained and the designing of equipment as well as separation processes of magnetic from non-magnetic minerals based on these theories are described.

The objective of the book remains the same as that of the first edition which is to help students interested in processing minerals to economically liberate and concentrate them for down-stream extraction processes. To understand the unit as well as the integrated processes the subject has been treated somewhat mathematically with the view to apply them in actual process designs and operations. In so doing it is expected that the book would suit students from the disciplines of Metallurgy, Chemical Engineering, Process Engineering and to a limited extent Electronics Engineering, who are engaged in the beneficiation of minerals and who are at under-graduate, graduate and post-graduate levels of study. Some data provided in the appendix is expected to aid in calculations of designing and plant operations. Solutions to simple and common plant problems are provided.

In writing this second edition of the book we offer our thanks to the reviewers who offered help and guidance to improve on the first edition. Also our renewed thanks to Dr Lutz Elber and Dr Halit Eren for their help and contribution in writing Chapter 20 on Process Control. We would also like to thank the various state and university libraries who helped in supplying

up-to-date information. We would especially like to thank our publishers who prompted us to write this edition; especially Dr Kostakitas, Anitha Sivaraj and Christine McElvenny who helped us to produce this edition.

**Ashok Gupta and
Denis Yan**

Perth, Western Australia, November 2015

Symbols and Units

A general convention used in this text is to use a subscript to describe the state of the quantity, for example, S for solid, L for liquid, A for air, SL or P for slurry or pulp, M for mass and V for volume. A subscript in brackets generally refers to the stream, for example, (O) for overflow, (U) for underflow, (F) for feed, (C) for concentrate and (T) for tailing. There are a number of additions to this convention which are listed later.

| | | |
|-----------|--|-----------------------|
| a | a constant | — |
| a | amplitude | m |
| a_p | particle acceleration | m/s ² |
| a_m | media acceleration | m/s ² |
| A | a constant | — |
| A | aperture | microns |
| A | area | m ² |
| A_C | cross-sectional area | m ² |
| A_E | effective area | m ² |
| A_{EFF} | areal efficiency factor | — |
| A_i | abrasion index | — |
| A_{ij} | assay of particles in the i th size and j th density fractions | — |
| A_m | cross-sectional area of media | m ² |
| A_M | assay of mineral | %, g/t, ppm |
| A_O | open area | % |
| A_{OE} | effective open area | % |
| A_p | cross-sectional area of particle | m ² |
| A_U | underflow area | m ² |
| b | a constant | — |
| b | Rosin–Rammler distribution parameter | — |
| B | magnetic induction, flux density | Wb/m ² , T |
| B_o | magnetic induction at the drum surface | Wb/m ² , T |
| B_s | magnetization saturation | T |
| B_{ij} | breakage distribution function | — |
| c | a constant | — |
| C | a constant | — |

Symbols and Units

| | | |
|---------------------|--|-------------------|
| C | Curie constant | — |
| C | circulation ratio or load | — |
| C | concentration (mass solid/volume of slurry) | kg/m ³ |
| C_A | concentration of air | kg/m ³ |
| C_C | average concentration of solids in the compression zone | kg/m ³ |
| C_{CRIT} | critical concentration | kg/m ³ |
| C_D | drag coefficient | — |
| C_F | correction factor | — |
| C_F | concentration of the feed (mass of solid/volume of slurry) | kg/m ³ |
| C_i | concentration of species i | kg/m ³ |
| C_O | initial concentration (mass of solid/volume of slurry) | kg/m ³ |
| C_{MAX} | maximum concentration (mass of solid/volume of slurry) | kg/m ³ |
| $C_{\text{MS(F)}}$ | concentration of solids in the feed by mass | % |
| $C_{\text{S(C)}}$ | concentration of solid (C = concentrate, F = feed, T = tail, f = froth, P = pulp) | — |
| $C_{\text{S(U)}}$ | solids concentration in the underflow (O = overflow, F = feed) | % |
| C_t | concentration at time t (mass of solid/volume of slurry) | kg/m ³ |
| C_T | correction factor or transfer coefficient | — |
| C_U | concentration of the underflow (mass of solid/volume of slurry) | kg/m ³ |
| $C_{\text{VS(F)}}$ | concentration of solids in the feed by volume | % |
| CC | concentration criterion | — |
| CI | confidence interval | — |
| CR | confidence range | — |
| CV | coefficient of variation | — |
| C_∞ | concentration at infinite time | kg/m ³ |
| d | a constant | — |
| d | particle size, diameter | m |
| d_{32} | Sauter mean diameter | m |
| d_{50}, d_{50C} | cut or separation size, corrected cut size | microns |
| d_B | ball diameter | cm, m |
| d_C | cylpeb diameter | mm |
| d_{cutter} | cutter opening | m |
| d_d | disc diameter | m |
| d_F | 63.2% passing size in the feed | m |
| d_H | diameter of helix stirrer | m |
| d_l | liberation size | m |
| d_m | media diameter | m |
| d_M | mill diameter | m |
| d_{MAX} | largest dimension | m |
| d_{MIN} | smallest dimension | m |
| d_{MID} | mid-range dimension | m |
| d_N | nominal diameter | m |
| d_w | wire diameter | m |

| | | |
|------------|---|-------------|
| D | discharge mass ratio (liquid/solid) | – |
| D | displacement, distance, diameter | m |
| D^* | dimensionless parameter | – |
| D_c | cyclone diameter | m |
| D_i | inlet diameter | m |
| D_o | overflow diameter | m |
| D_u | underflow diameter | m |
| e | a constant | – |
| e^+, e^- | quantity of charge | C |
| E | energy | kWh |
| E | potential difference | V |
| E_B | energy of rebound | Wh |
| E_C | corrected partition coefficient | – |
| E_G | specific grinding energy | kWh/t |
| E_i | partition coefficient of size i = recovery of size i in the U/F | – |
| E_o | uniform electric field strength | N/C, V/m |
| E_O | efficiency based on oversize | – |
| E_p | Ecart probability, probable error of separation | – |
| E_s | surface electric field intensity | N/C, V/m |
| E_T | total energy | kW |
| E_U | efficiency based on undersize | – |
| f | a constant | – |
| $f(J_B)$ | ball load-power function | – |
| f_p, f_f | function relating to the order of kinetics for pulp and froth | – |
| $f(r)$ | ball wear rate | kg/h |
| $f(s)$ | suspensoid factor | – |
| f_i | mass fraction of size i in the circuit feed | – |
| F_{80} | 80% passing size of feed | microns |
| F | feed size | cm, microns |
| F | floats at SG | – |
| F | froth stability factor | – |
| F | feed mass ratio (liquid/solid) | – |
| F_B | Rowland ball size factor | – |
| F_B | buoyancy force | N |
| F_C | Bond mill factor | – |
| F_C | centrifugal force | N |
| F_d | diffusion force | N |
| F_D | drag force | N |
| F_e | electrostatic force | N |
| F_E | electric dipole force | N |
| F_f | frictional force | N |
| F_g | gravitational force | N |
| F_{gt} | tangential component of gravitational force | N |

Symbols and Units

| | | |
|--------------|---|------------------|
| F_G | correction factor for extra fineness of grind | – |
| F_i | settling factor | – |
| F_i | inertia or centrifugal force | N |
| F_l | electric field gradient force | N |
| F_M | magnetic force | N |
| F_{MR} | radial component of magnetic force | N |
| F_{OS} | correction factor for oversized feed | – |
| F_R | correction factor for low reduction ratio | – |
| F_S | mass flow rate | kg/s, t/h |
| F_S | Bond slurry or slump factor | – |
| F_v | viscous force (drag) | N |
| g | gravitational constant (9.81) | m/s ² |
| G | grade (assay) | %, g/t, ppm |
| G, G_{bp} | net grams of undersize per revolution | g/rev |
| G' | grinding parameter of circulating load | – |
| ΔG | free energy | J |
| h | parameter = x/σ | – |
| h_l, h_l^* | distances within the conical section of a mill | M |
| H | hindrance factor | – |
| H | height | m, cm |
| H | magnetic field strength | A/m |
| H_B | height of rebound pendulum | m |
| H_B | height of bed | m |
| H_C | height of ball charge | m |
| H_C | height of the start of the critical zone in sedimentation | m |
| H_{OF} | height of the clarification zone (overflow) | m |
| H_R | height of rest | m |
| H_S | hindered settling factor | – |
| H_t | height at time t | m |
| H_U | mudline height at the underflow concentration | m |
| H_∞ | height after infinite time | m |
| i | current | A |
| I | impact crushing strength | kg.m/mm |
| I | imperfection | – |
| J_B | fraction of mill volume occupied by bulk ball charge | – |
| J_C | fraction of mill volume in cylindrical section occupied by balls and coarse ore | – |
| J_G | superficial gas velocity | m/s |
| J_R | fraction of mill volume occupied by bulk rock charge | – |
| J_P | fraction of mill volume filled by the pulp/slurry | – |
| k | constant | – |
| K | Boltzmann's constant, 1.381×10^{-23} | J/K |
| k_A, k_A' | rate constant for air removal via froth and tailings respectively | – |

| | | |
|---------------------|--|---------------------------------|
| k_C, k_{C50} | screening rate constant, crowded condition, normal and half size | t/h/m ² |
| k_e | Coulomb's constant, 8.99×10^9 | Nm ² /C ² |
| k_F, k_S | rate constant for fast and slow component respectively | min ⁻¹ |
| k_i | comminution coefficient of fraction coarser than i th screen | – |
| k_S, k_{S50} | screening rate constant, separated condition, normal and half size | m ⁻¹ |
| K | constant | – |
| K | ratio of vertical to horizontal media pressure | – |
| K | flatness factor | – |
| K_{D0} | material constant | – |
| KE | kinetic energy | kW |
| L | length | m |
| L_A | aperture size | m |
| L_{AE} | effective aperture | m |
| L_C | length of cyclone | m |
| L_{CYL}, L_{CONE} | length of cylindrical and cone sections | m |
| L_D | drum radius | m |
| L_E | distance between electrodes | m |
| L_{EFF} | effective grinding length | m |
| L_F | Nordberg loading factor | – |
| L_{MIN}, L_{MAX} | minimum and maximum crusher set | m |
| L_r | distance from centre of rotation | m |
| L_T | crusher throw | m |
| L_V | length of vortex finder | m |
| L_{VF} | length from end of vortex finder to apex of a cyclone | m |
| m | moisture (wet mass/dry mass) | – |
| m | mass | g |
| m | mineralogical factor | kg/m ³ |
| $m_{i(U)}$ | mass of size i in the underflow ($F = \text{feed}$) | kg |
| m_k | mass fraction of makeup balls of size k | – |
| $m(r)$ | cumulative mass fraction of balls less than size r | – |
| m_T | mass rate of ball replacement per unit mass of balls | kg/h.t |
| $m_{U(F)}$ | mass fraction of undersize in the feed | – |
| $m_{U(O)}$ | mass fraction of undersize in the oversize | – |
| $m_{U(U)}$ | mass fraction of undersize in the undersize | – |
| M | magnetization | A/m |
| M | mass | kg, t |
| M_I | mass of new feed | g |
| M_B | mass of block | kg |
| M_B | mass of balls | kg |
| M_C | mill capacity | t/h |
| M_C | mass of crushing weight | kg |
| M_F | mass of feed | t |
| M_F | mass of fluid | kg |

Symbols and Units

| | | |
|----------------------|--|-------------------|
| M_{FT} | mass of floats | kg, t |
| M_F | Nordberg mill factor | — |
| M_i | mass/mass fraction of i th increment | kg, t |
| M_{oi} | cumulative mass fraction retained on i th screen at zero time | — |
| M_{ij} | mass percent of the i th size fraction and j th density fraction | % |
| M_{MIN} | minimum mass of sample required | kg, t |
| M_p | mass of particle | kg |
| M_r | cumulative mass fraction of balls of size r in the charge | — |
| M_R | mass of rock | kg |
| M_R | mass fraction of rock to total charge (rock + water) | — |
| M_S | mass of striking pendulum | kg |
| M_S | mass of solid | kg, t |
| $M_{S(f)}$ | mass of solid in froth | — |
| $M_{S(F)*S(C)*S(T)}$ | mass of solid feed, concentrate and tailing respectively | kg, t |
| M_{SK} | mass of sinks | kg, t |
| $M_{S(p)}$ | mass of solid in the pulp | kg, t |
| M_w | mass of water | kg, t |
| $\Delta M(t)$ | mass of top size particle | kg, t |
| n | number of revolutions/min | min^{-1} |
| n | number of increments, measurements | — |
| n | order of rate equation | — |
| n | number of unpaired electrons | — |
| $n(r)$ | cumulative number fraction of balls of size less than r | — |
| n_s | number of sub-lots | — |
| N | number of mill revolutions | — |
| N | revolutions per second | s^{-1} |
| N | number of strokes/min | min^{-1} |
| N | number | — |
| N | concentration of ions per unit volume | m^{-3} |
| N' | number of particles/gram | g^{-1} |
| N_o | Avogadro's number, molecules/mol | — |
| N_L | number of presentations per unit length | m^{-1} |
| N_m | number of media per unit volume | m^{-3} |
| N_S | number of stress events | — |
| o_i | mass fraction of size i in the overflow | — |
| p | Probability | — |
| p_i | mass fraction of size i in the new feed | — |
| P | product size | microns |
| P | proportion of particles | — |
| P | pressure | Pa |
| P | powers roundness factor | — |
| P | jig power | W |
| P | JKSimFloat ore floatability parameter | — |

| | | |
|----------------------|--|-------------------|
| P | probability | – |
| P_{80} | 80% passing size of product | microns |
| P_A, P_C, P_E, P_F | probability of adherence, collision, emergence, froth recovery | – |
| P_{CON} | power of the conical part of a mill | kW |
| P_{CYL} | power for the cylindrical part of a mill | kW |
| P_D | particle distribution factor | – |
| P_F | pinning factor | – |
| P_g | pressure due to gravity | N/m ² |
| P_G | proportion of gangue particles | – |
| P_{ij} | proportion of particles in the i th size and j th density fractions | – |
| P_L | liberation factor | – |
| P_m | grinding media pressure | N/m ² |
| P_M | proportion of mineral particles | – |
| P_M | mill power | kW |
| P_{NET} | net mill power draw | kW |
| P_{NL} | no load power | kW |
| P_{OS} | period of oscillation | s |
| P_R | relative mill power | – |
| P_S | particle shape factor | – |
| P_S | power at the mill shaft | kW |
| PE | potential energy | kW |
| ΔP | pressure drop | kPa |
| q | alternate binomial probability = $1 - p$ | – |
| Q | capacity | t/h |
| Q_1, Q_2 | point charges | C |
| Q_B | makeup ball addition rate | kg/day |
| Q_B | basic feed rate (capacity) | t/h/m |
| $Q_{MS(O)}$ | flowrate of solids by mass in the overflow ($U = U/F$, $F = \text{feed}$) | t/h |
| $Q_{MS(C)}$ | mass flow of solid in concentrate | t/h |
| $Q_{M(F)}$ | capacity, of feed slurry by mass | t/h |
| Q_O | tonnage of oversize material | t/h |
| Q_U | capacity of the underflow | t/h |
| $Q_{V(C)}, (T), (F)$ | flowrate by volume in concentrate, tailing and feed respectively | m ³ /h |
| $Q_{V(f)}$ | flowrate by volume in the froth | m ³ /h |
| $Q_{VL(O)}$ | capacity (flowrate) of liquid by volume in the overflow ($U = \text{underflow}$, $F = \text{feed}$) | m ³ /h |
| $Q_{V(O)}$ | flowrate by volume of overflow (pulp) ($U = \text{underflow}$) | m ³ /h |
| $Q_{VOL(U)}$ | flowrate by volume of entrained overflow liquid in the U/F | m ³ /h |
| $Q_{VOP(U)}$ | flowrate by volume of entrained overflow pulp in the U/F | m ³ /h |
| $Q_{VOS(U)}$ | flowrate by volume of entrained overflow solids in the U/F | m ³ /h |
| $Q_{VS(O)}$ | flowrate by volume of solids in the overflow ($U = U/F$, $F = \text{feed}$) | m ³ /h |
| Q_w | ball wear rate | mm/h |
| r | radius | m |

Symbols and Units

| | | |
|-----------------|--|-------------------|
| r | ratio of rate constants = $k_A'/(k_A + k_A')$ | — |
| r_0 | fraction of test screen oversize | — |
| r_1, r_2 | radius within the conical section of a mill | m |
| r_p | particle radius | m |
| r_v | vector radius | m |
| R | radius | m |
| R | recovery | % |
| R | reduction ratio | — |
| \bar{R} | the mean radial position of the active part of the charge | m |
| R' | fractional recovery, with respect to the feed to the first cell | — |
| R' | mass of test screen oversize after grinding | g |
| R_1, R_2, R_3 | Dietrich coefficients | — |
| R_C | radius of cone at a distance L_i from cylindrical section | m |
| Re_A, Re_C | Reynolds number in the apex and cone section respectively | — |
| Re_p | particle Reynolds number | — |
| R_F | froth recovery factor | — |
| R_i | radial distance to the inner surface of the active charge | m |
| R_0 | mass of test screen oversize before grinding | g |
| R_p | radial distance of particle from the centre of a mill | m |
| R_{RO} | optimum reduction ratio | — |
| R_T | radius at the mill trunnion | m |
| R_V | recovery of feed volume to the underflow | — |
| R_∞ | recovery at infinite time | — |
| S | speed | m/s |
| S | sinks at SG | — |
| S | surface area | m ² |
| S | spacing, distance | m |
| S^* | dimensionless parameter | — |
| S_B | surface area of ball | m ² |
| S_B | bubble surface area flux | s ⁻¹ |
| S_F | Nordberg speed factor | — |
| S_i | breakage rate function | min ⁻¹ |
| SE | stress energy | Nm |
| SE_{vb} | specific energy per unit volume at level b | Nm/m ³ |
| SG, SG_s | specific gravity, specific gravity of solid | — |
| SI | stress intensity of grinding media | Nm |
| t | time | h, min, s |
| t_{10} | size that is one tenth the size of original particle | mm |
| \bar{t}_A | mean time taken for active part or charge to travel from the toe to the shoulder | s |
| t_D | detention or residence time | h |
| \bar{t}_F | mean time for free fall from the shoulder to the toe | s |