COMPUTATIONAL TECHNIQUES AND APPLICATIONS: CTAC-85

COMPUTATIONAL TECHNIQUES AND APPLICATIONS: CTAC-85

Proceedings of the Computational Techniques and Applications Conference held at the University of Melbourne, Australia 25-28 August, 1985

Edited by:

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NORTH-HOLLAND - AMSTERDAM • NEW YORK • OXFORD • TOKYO

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ISBN: 0 444 87995 1

Publishers:
ELSEVIER SCIENCE PUBLISHERS B.V.
P.O. Box 1991
1000 BZ Amsterdam
The Netherlands

Sole distributors for the U.S.A. and Canada:
ELSEVIER SCIENCE PUBLISHING COMPANY, INC.
52 Vanderbilt Avenue
New York, N.Y. 10017
U.S.A.

Library of Congress Cataloging-in-Publication Data

International Conference on Computational Techniques and Applications (2nd : 1985 : University of Melbourne) Computational techniques and applications, CTAC-85.

Includes bibliographies.

1. Mathematical analysis—Congresses. I. Noye, John, 1930—

11. May, Robert (Robert L.) III. Title. QA299.6.156 1985 515 86-4414 ISBN 0-444-87995-1 (U.S.)

PREFACE

Following the very successful 1981 Conference on Numerical Solutions of Partial Differential Equations held at Queen's College, University of Melbourne, it was decided to hold a similar meeting in 1983, namely a Computational Techniques and Applications Conference (CTAC-83) in the Faculty of Engineering of the University of Sydney. At CTAC-83 the Computational Mathematics Group of the Applied Mathematics Division of the Australian Mathematical Society was formed, with its main function to oversee the organisation of biennial conferences in the CTAC series. This volume is the proceedings of the second such conference, CTAC-85, held in the Department of Mathematics of the University of Melbourne, Australia from 25th to 28th August, 1985.

There were six invited speakers who gave one-hour Keynote Lectures. They were Professor Bill Morton, Oxford University, England, "Characteristic Galerkin and Lagrange Galerkin Methods for Evolutionary PDEs", Dr. Pat Roache, Ecodynamic Research Associates Inc., Albuquerque, New Mexico, "The ELF Codes: Electrode Design for Lasers and Switches", Professor Bob Mattheij, Katholieke Universiteit, The Netherlands, "Stable Solution of Boundary Value Problems of Ordinary Differential Equations", Associate-Professor Graham de Vahl Davis, University of New South Wales, Australia, "Finite Difference Methods for Viscous Flow and Heat Transfer", Dr. Clive Fletcher, University of Sydney, Australia, "Finite Element Techniques for Slightly Viscous Flows", and Dr. Grant Steven, University of Sydney, "Constrained or Unconstrained Minimization and Penalty Methods in Finite Element Structural Analysis".

In addition, 48 research papers of one-half hour duration were presented. Refinements of various numerical techniques used in applications and experiences in applying these methods to solve practical problems were reported. These papers have been categorised into the following groups: techniques for partial differential equations, techniques for ordinary differential equations, fluid flow and heat transfer, tides and waves, flow through porous media, elasticity and structures, and miscellaneous.

A special mention must be made of the work done by the committee which organised the conference so efficiently. Thanks also go to the various organisations which assisted financially and otherwise — they are listed separately.

vi Preface

Finally, our personal thanks go to Drs. Arjen Sevenster (Mathematics Editor), John Butterfield (Technical Editor) and Clive Ewing (Promotions Department) of Elsevier Science Publishers B.V. in Amsterdam, for their assistance in arranging the publication of this book.

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The University of Adelaide

Robert May
Royal Melbourne Institute of Technology

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COMPUTATIONAL TECHNIQUES AND APPLICATIONS CONFERENCE CTAC-85

CONFERENCE ORGANISING COMMITTEE

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THE COMPUTATIONAL MATHEMATICS GROUP DIVISION OF APPLIED MATHEMATICS AUSTRALIAN MATHEMATICAL SOCIETY

The proposal to form a Computational Mathematics Group as a Specialist Group of the Division of Applied Mathematics was initiated by the committee who organised the Computational Techniques and Applications Conference (CTAC-83) held in Sydney in 1983. This volume forms the proceedings of CTAC-85, the second in the CTAC series.

The second meeting of the Computational Mathematics Group of the Division of Applied Mathematics of the Australian Mathematical Society took place on August 30 during CTAC-85. At this meeting the second committee of the Computational Mathematics Group was elected. It consists of:

Chairman:

Dr. B.J. NOYE

Department of Applied Mathematics

The University of Adelaide

Adelaide

South Australia

Australia

Secretary:

Dr. C.A.J. FLETCHER

Department of Mechanical Engineering

The University of Sydney

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Committee: Associate-Professor G. de VAHL DAVIS

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Department of Mathematics Royal Melbourne Institute of Technology Victoria Australia

Ex Officio: Chairman

Division of Applied Mathematics Australian Mathematical Society (presently Professor J.R. BLAKE Mathematics Department The University of Wollongong New South Wales

Australia)

The major responsibility of this Group is the organisation of the biennial Computational Techniques and Applications Conferences which are intended to foster communication between the users of computational mathematics who work in a wide range of disciplines.

The next such conference (CTAC-87) will be held in Sydney, Australia, in August 1987. The Convenor will be Dr. C.A.J. Fletcher, Department of Mechanical Engineering, The University of Sydney, Sydney, New South Wales 2006, Australia. All enquiries concerning CTAC-87 should be addressed to him.

ACKNOWLEDGEMENTS

The assistance of the following organisations is gratefully acknowledged:

Centre for Mathematical Analysis, Australian National University
The British Council
Trans Australian Airlines
Applied Mathematics Division, Australian Mathematical Society

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