

**The Determination  
of Ionization Constants**  
*A Laboratory Manual*

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# **The Determination of Ionization Constants**

## ***A Laboratory Manual***

THIRD EDITION

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## **The Determination of Ionization Constants**

## Preface

This practical manual is devised for organic chemists and biochemists who, in the course of their researches and without previous experience, need to determine an ionization constant. We are gratified that earlier editions were much used for this purpose and that they also proved adequate for the in-service training of technicians and technical officers to provide a Department with a  $pK$  service. The features of previous editions that gave this wide appeal have been retained, but the subject matter has been revised, extended, and brought up to date.

We present two new chapters, one of which describes the determination of the stability constants of the complexes which organic ligands form with metal cations. The other describes the use of more recently introduced techniques for the determination of ionization constants, such as Raman and nuclear magnetic resonance spectroscopy, thermometric titrations, and paper electrophoresis.

Chapter 1 gives enhanced help in choosing between alternative methods for determining ionization constants. The two chapters on potentiometric methods have been extensively revised in the light of newer understanding of electrode processes and of the present state of the art in instrumentation.

In the spectrometric methods chapter, the newer IUPAC symbols replace the old. Also the treatment of Hammett's acidity function has been brought up to date. This chapter concludes with help for the preparative organic chemist, namely a rapid spectrometric titration. This yields an approximate  $pK$ , knowledge of which will suggest conditions under which the new substance can be extracted and purified in higher yields.

The chapter on zwitterions and other ampholytes has been largely rewritten to give a clearer presentation, and much new information has been incorporated.

The tables of typical ionization constants, in Chapter 9, have been re-compiled from the most reliable of available values, and many additional substances will be found there. This chapter has a new section on substances which modify their ionization by equilibrating with pseudobases (e.g. acridinium and pyrylium salts, also triphenylmethane dyes). The chapter concludes with a new table of the ionization constants of 370 commonly prescribed drugs and other biologically active substances.

Help in the interpretation of ionization constants is provided. It is shown how these are related to solubility (Chapter 5), how the degree of ionization at any pH can be calculated (Appendix V), and how ionization constants can aid in deciphering an unknown structure (Chapter 1).

We advise a beginner, before he tackles any unknown substance, to 'enroll' in a course by repeating, in the order printed, each worked example in Chapters 2 and 4, both the practical work and the calculations (only easily procurable substances are needed). Much time can be saved in the calculations if the results are set out as shown in these worked examples.

The first examples require only a few, very simple calculations. We have taken care to define the parameters within which these simple methods suffice, and to state clearly when refinements of calculation are needed. We have introduced the more complicated calculations as gradually as possible, and with full explanatory detail. To lessen the tedium of the lengthier calculations, we have devised computer programs. These are presented in a form which clearly shows the pathways of their derivation, to help those who would like to use a desk (electronic) calculator instead of a computer.

Because this is a practical manual, we have touched only lightly on the theory of ionization (Chapter 1 and Appendices I and II). For theoretical study, E.J. King's book *Acid-Base Equilibria* (1965) and R.G. Bates' *Determination of pH, Theory and Practice* (1973) are recommended. Many useful data will also be found in *Electrolyte Solutions* by R.A. Robinson and R.H. Stokes (1959), and *Solution Equilibria* by F.R. Hartley, C. Burgess and R. Alcock (1980), the latter being particularly helpful with the experimental approach to finding stability constants of metal complexes.

We thank Dr D.D. Perrin for helpful discussions.

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# 1 Introduction

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## 1.1 What is meant by 'ionization constants'?

In this book, the term 'ionization constant' means any constant which is used to measure the strength of acids and bases. Although sometimes referred to as 'dissociation constant', this term is vague because ionization forms only a corner of the vast field of dissociation phenomena. Thus substrates dissociate from enzymes, micelles dissociate into monomers, and iodine molecules dissociate into iodine atoms. Many other such equilibrium processes are known, but the majority of these dissociations are not ionizations. On the other hand zwitterions are ionized but they are not dissociated.

A minor objection to the term ionization constants is that the constant for a base represents an equilibrium in which one ion gives rise to another ion (see equation 1.3, p. 4). This difficulty disappears if we define ionization constants with reference to hydrogen and hydroxyl ions only.

This chapter outlines the concepts discussed later in the book. It is supplemented by a general revision of basic theory in Appendices I and II.

## 1.2 Why do we determine ionization constants?

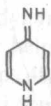
Ionization constants reveal the proportions of the different ionic species into which a substance is divided at any chosen pH. Appendix V (p. 203) shows how to calculate the percentage of an acid or a base that is ionized at various values of pH and  $pK_a$ . It may be deduced from the equations of Appendix V, and also from Fig. 1.1 that a small change in pH can make a large change in the

percentage ionized. This is particularly significant if the values of pH and pK lie close together, as they do near the point of half neutralization.

Information about ionization is useful in many ways. For example, different ionic species have different ultraviolet spectra, and significant spectrophotometry can be done only when the pH is so chosen that only *one* ionic species is present. The ionic species of a given substance differ in other physical properties, and in chemical and biological properties as well (Albert, 1979). Ionization constants, by defining the pH range in which a substance is least ionized, indicate the conditions under which it can be isolated in maximal yield (see Chapter 5) and this information has much value in preparative chemistry.

Ionization constants, too, can help to discover the structure of a newly isolated substance. The first question to ask is: Does the postulated structure predict the experimentally determined  $pK_a$  values, when calculated theoretically by the method of Perrin, Dempsey and Serjeant (1981)? If so, a considerable verification of the proffered structure has been achieved. Several other ways in which ionization constants reveal structure will now be mentioned. For a fuller treatment of the subject, see Barlin and Perrin's review (1972).

When tautomerism is possible, the structure with the more weakly acidic proton is favoured because it must have the mobile hydrogen more firmly bonded. Ionization constants determinations first showed that 2- and 4-aminopyridine ( $pK_a$  6.9 and 9.2) had the structures of primary amines in equilibrium with very little of the imine tautomers (e.g. (1.1)), because 1-methyl-2-imino- and 1-methyl-4-imino-pyridines had  $pK_a$ s 12.2 and 12.5, respectively (Angyal and Angyal, 1952). Similar reasoning helped to assign structures to the products obtained by methylating the mono-aminopyrimidines, i.e. whether the *exo*- or the *endo*-nitrogen atom was alkylated (Brown, Hoerger and Mason, 1955). Again, the methylation of 4-nitroimidazole (1.2) gave 1- and 3-methyl derivatives, whose structures were easily assigned from the large and expected difference in  $pK_a$  ( $-0.53$  and  $2.13$  units, respectively). (Grimison, Ridd and Smith, 1960).



(1.1)



(1.2)

The presence of *covalently* bound water can be detected in a heterocyclic amine by the anomalously high  $pK_a$  values that it engenders, by strengthening bases and *weakening* acids (Albert, 1976; Albert and Armarego, 1965).

To distinguish between a zwitterion and an ordinary ampholyte, in amphoteric substances, there is no better method than to compare the  $pK_a$  values as determined in water with those determined in dilute ethanol (see, further, Chapter 8).

Many pairs of geometrical isomers have had their members correctly assigned by comparison of ionization constants (Pascual and Simon, 1964). Axial

#### 4 The determination of ionization constants

carboxy groups are weaker than their equatorial analogues, and many conformational problems have been solved by this knowledge (Barlin and Perrin, 1972). Differences in  $pK_a$  values form the basis for separating many chemically similar substances, such as the various penicillins that arise side-by-side from a fermentation (see also Chapter 5, p. 103).

### 1.3 Brief summary of the chemistry of ionization

The Brønsted-Lowry theory (Brønsted, 1923) is the most useful and widely accepted description of the ionization of both acids and bases (see Appendix I). The underlying concept of this theory is the definition of an acid as any substance that can ionize to give a solvated hydrogen ion (i.e. a proton stabilized by interaction with either the solvent or a substance in solution). Conversely a base is a substance which can accept a hydrogen ion.

In this book we deal almost exclusively with the determination of ionization constants in aqueous solutions. Most salts are completely ionized in aqueous solution, but this is not the case with many acids and bases. Very strong acids and bases are definable as those completely ionized in the pH range 0–14. Less strong acids and bases are incompletely ionized in parts of this range as is calculable from their ionization constants by the equations given at the head of Appendix V. It should also be noted that, in parts of the above range, the ions of salts formed from weak acids (or bases) are partly hydrolysed in aqueous solution, i.e. those ions are in equilibrium with the corresponding neutral species. This behaviour is also taken care of in the equations of Appendix V.

Brønsted (1923) was the first to show the advantage of having the ionization of both acids and bases (i.e. conjugate acids) expressed on the same scale, just as pH is used for alkalinity as well as for acidity. For acids the ionization process is



and the ionization constant,  $K_a$ , is given by

$$K_a = \frac{\{H^+\} \{A^-\}}{\{HA\}} \quad (1.2)$$

where  $\{ \}$  represents the activity of each ionic species (in mol litre<sup>-1</sup>).

For bases the ionization is



and

$$K_a = \frac{\{H^+\} \{B\}}{\{BH^+\}} \quad (1.4)$$

At a given temperature, the constants expressed by equations (1.2) and (1.4)

are thermodynamic quantities also known as *thermodynamic ionization constants* which we shall refer to henceforth as  $K_a^T$ . These constants are independent of concentration, because all the terms involved are in terms of *activities* (see Appendix II). Another type of constant that we shall use is the *concentration ionization constant*,  $K_a^C$ , which is defined for acids as

$$K_a^C = \frac{[H^+][A^-]}{[HA]} \quad (1.5)$$

in which square brackets denote the *concentration* (as opposed to the activity) of each ionic species. To yield whole numbers (rather than negative powers of ten, which are hard to remember and clumsy to write), equation (1.5) is generally used in the following form, in which  $pK_a$  is the negative logarithm of the ionization constant:

$$pK_a = pH + \log[HA]/[A^-] \quad (1.5a)$$

For bases, the corresponding expression is

$$K_a = \frac{[H^+][B]}{[BH^+]} \quad (1.6)$$

or

$$pK_a = pH + \log[BH^+]/[B] \quad (1.6a)$$

The main difference between thermodynamic and concentration constants is that the *activities* of the ions have to be taken care of in calculating the former. These activities compensate for the attraction which ions can exert on one another (ion-pair effects) as well as the incomplete hydration of ions in solutions that are too concentrated. The lower the concentration, the less this interaction becomes until, at infinite dilution, the concentration constant becomes numerically equal to the thermodynamic constant. These differences are dealt with in Chapter 3 (p. 47) where help is given in deciding what allowance must be made for activity effects (p. 48). Equation (1.5) can be used for the sake of simplicity provided that: (a) constants are determined in solutions not stronger than 0.01 molar; and (b) only univalent ions are present.

For the present it need only be noted that the activity of a neutral species (molecule) does not differ appreciably from its concentration, at any dilution; and that pH, as commonly determined, is nearer to hydrogen ion activity than to hydrogen ion concentration, although at low ionic strength ( $I = \leq 0.01$ ) these terms do not differ greatly\* between pH 2 and 10. Hence  $\{A^-\}$  is the only unfamiliar quantity in equation (1.2), because  $[HA]$  can be substituted for  $\{HA\}$ , and  $\{H^+\}$  is read from the measuring instrument.

\*See, further, Appendix III.



## 6 The determination of ionization constants

### 1.4 The nature of $pK_a$ values

Ionization constants are small and inconvenient figures and hence it has become customary to use their negative logarithms (known as  $pK_a$  values) which are convenient both in speech and writing (see equation 1.5a). Thus the  $pK_a$  of acetic acid (4.76) corresponds to the ionization constant  $1.75 \times 10^{-5}$ . Again, the  $pK_a$  of ammonia is 9.26, which is more convenient to use than the ionization constant ( $5.5 \times 10^{-10}$ ).  $pK_b$  values for bases (see Appendix I), found only in the older literature, (e.g. 4.74 for ammonia at 25°C) can be converted to  $pK_a$  values by subtraction from the negative logarithm of the ionic product of water ( $K_w$ ) at the temperature of determination. The value of  $pK_w$  is 14.17 at 20°C, 14.00 at 25°C, and 13.62 at 37°C (see Appendix IV). Thus

$$pK_a + pK_b = 14.00 \quad \text{at } 25^\circ\text{C}. \quad (1.7)$$

It is evident that  $pK_a$  values are very convenient for comparing the strengths of acids (or of bases). The stronger an acid, the lower its  $pK_a$ ; the stronger a base, the higher its  $pK_a$ .

Table 1.1 gives the approximate  $pK_a$  values of some common acids and bases. Acids and bases of equivalent strengths have been placed opposite one another. It will prove advantageous to commit this table to memory in order to have a number of reference points for assessing the significance of new  $pK_a$  values. Many more values are in Chapter 9. For help in rapid interconversion of  $K_a$  and  $pK_a$  see Table 11.1 on p. 195.

Table 1.1 Approximate strengths of some common acids and bases

Acids	$pK_a$	Bases	$pK_a$
Hydrochloric acid*		Sodium hydroxide*	
	1		13
Oxalic acid	2	Acetamidine	12
	3	Ethylamine	11
Benzoic acid	4		10
Acetic acid	5	Ammonia	9
Carbonic acid	6	Many alkaloids†	8
4-Nitrophenol	7		7
	8		6
Hydrocyanic acid,		Aniline, pyridine,	
boric acid	9	quinoline	5
Phenol	10		4
	11		3
	12		2
Sucrose	13	4-Nitroaniline	1

\*Completely ionized in the range pH 0–14.

†Also local anaesthetics and antipsychotics

### 1.5 The shape of a titration curve

When an acid is dissolved in water it ionizes in accordance with equation (1.1). The addition of hydroxyl ions (in the form of potassium hydroxide, for example) disturbs the equilibrium by combining with the hydrogen ions produced by ionization. This reaction greatly alters the ratio of ionized species to neutral species. For example, if exactly one mole equivalent of sodium hydroxide is added, the acid will be quantitatively converted to its anion ( $A^-$ ), and hence the solution, if evaporated, will give the sodium salt. All the protons available from the acid will undergo the reaction with hydroxyl ions  $H^+ + OH^- \rightarrow H_2O$ . However, if only 0.1 mole equivalent of sodium hydroxide is added, then 10% of the amount of acid originally dissolved will be converted to the anion, leaving 90% of the original quantity as the neutral species of the acid (HA). Again, if 0.5 mole equivalent is added, the solution will contain equimolar amounts of (HA) and ( $A^-$ ). Equation (1.5a) reveals that the  $pK_a$  value of the acid may be calculated if the pH is measured under conditions of partial neutralization, because the ratio  $[HA]/[A^-]$  is known from the degree of neutralization. Thus when 0.1 mole equivalent has been added, the equation becomes  $pK_a = pH + \log(90/10)$ , or  $pK_a = pH + 0.95$ ; and for 0.5 mole equivalent  $pK_a = pH + \log(50/50)$ , i.e. at 50% neutralization the  $pK_a$  equals the pH. When plotted, as in Fig. 1.1, these results give a *titration curve*, which is

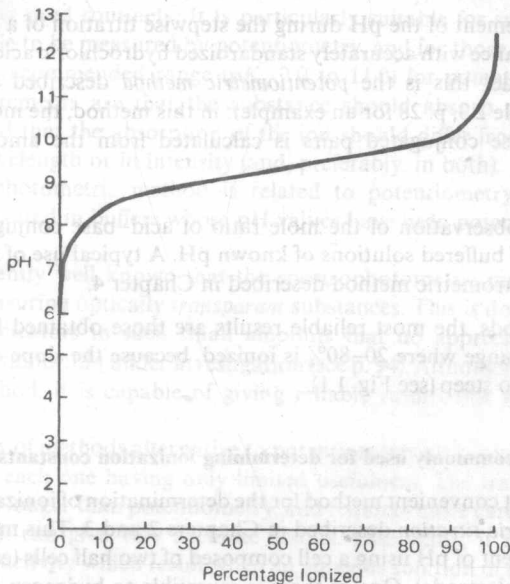


Figure 1.1 A typical titration curve.