# LASERS

Anthony E. Siegman

Professor of Electrical Engineering Stanford University

University Science Books Mill Valley, California

#### University Science Books 20 Edgehill Road Mill Valley, CA 94941

Manuscript Editor: Aidan Kelly Designer: Robert Ishi

Production: Miller/Scheier Associates, Palo Alto, CA

TeXpert: Laura Poplin

Printer and Binder: The Maple-Vail Book Manufacturing Group

Copyright © 1986 by University Science Books
Reproduction or translation of any part of this work
beyond that permitted by Sections 107 or 108 of the
1976 United States Copyright Act without the permission of
the copyright owner is unlawful. Requests for permission
or further information should be addressed to
the Permissions Department, University Science Books.

Library of Congress Catalog Card Number: 86-050346

ISBN 0-935702-11-5

Printed in the United States of America

This manuscript was prepared at Stanford University using the text editing facilities of the Context and Sierra DEC-20 computers and Professor Donald Knuth's TeX typesetting system. Camera-ready copy was printed on an Autologic APS- $\mu$ 5 phototypesetter.

10 9 8 7 6 5 4 3 2 1

#### PREFACE

This book presents a detailed and comprehensive treatment of laser physics and laser theory which can serve a number of purposes for a number of different groups. It can provide, first of all, a textbook for graduate students, or even well-prepared seniors in science or engineering, describing in detail how lasers work, and a bit about the applications for which lasers can be used. Problems, references and illustrations are included throughout the book.

Second, it can also provide a solid and detailed description of laser physics and the operational properties of lasers for the practicing engineer or scientist who needs to learn about lasers in order to work on or with them.

Finally, the advanced sections of this text are sufficiently detailed that this book will provide a useful one-volume reference for the experienced laser engineer or laser researcher's bookshelf. The discussions of advanced laser topics, such as optical resonators, Q-switching, mode locking, and injection locking, extend far enough into the current state of the art to provide a working reference on these and similar topics. References for further reading in the recent literature are included in nearly every section.

One unique feature of this book is that it removes much of the quantum mystique from "quantum electronics" (the generic label often applied to lasers and laser applications). Many people think of lasers as quantum devices. In fact, however, most of the basic concepts of laser physics, and virtually all the practical details, are classical in nature. Lasers (and masers) of all types and in all frequency ranges are simply electronic devices, of great interest and importance to the electronics engineer.

In the analogous case of semiconductor electronics, for example, the transistor is not usually thought of as a quantum device. Mental images of holes and electrons as classical charged particles which accelerate, drift, diffuse and recombine are used both by semiconductor device engineers to do practical device engineering, and by solid-state physics researchers to understand sophisticated physics experiments. These classical concepts serve to explain and make understandable what is otherwise a complex quantum picture of energy bands, Bloch wavefunctions, Fermi-Dirac distributions, and occupied or unoccupied quantum states. The same simplification can be accomplished for lasers, and laser devices can then be very well understood from a primarily classical viewpoint, with only limited appeals to quantum terms or concepts.

The approach in this book is to build primarily upon the classical electron oscillator model, appropriately extended with a descriptive picture of atomic energy levels and level populations, in order to provide a fully accurate, detailed and physically meaningful understanding of lasers. This can be accomplished

without requiring a previous formal background in quantum theory, and also without attempting to teach an abbreviated and inadequate course in this subject on the spot. A thorough understanding of laser devices is readily available through this book, in terms of classical and descriptively quantum-mechanical concepts, without a prior course in quantum theory.

I have also attempted to review, at least briefly, relevant and necessary background material for each successive topic in each section of this book. Students will find the material most understandable, however, if they come to the book with some background in electromagnetic theory, including Maxwell's equations; some understanding of the concept of electromagnetic polarization in an atomic medium; and some familiarity with the fundamentals of electromagnetic wave propagation. An undergraduate-level background in optics and in Fourier transform concepts will certainly help; and although familiarity with quantum theory is not required, the student must have at least enough introduction to atomic physics to be prepared to accept that atoms do have quantum properties, especially quantum energy levels and transitions between these levels.

The discussions in this book begin with simple physical descriptions and then go into considerable analytical detail on the stimulated transition process in atoms and molecules; the basic amplification and oscillation processes in laser devices; the analysis and design of laser beams and resonators; and the complexities of laser dynamics (including spiking, Q-switching, mode locking, and injection locking) common to all types of lasers. We illustrate the general principles with specific examples from a number of important common laser systems, although this book does not attempt to provide a detailed handbook of different laser systems. Extensive references to the current literature will, however, guide the reader to this kind of information.

There is obviously a large amount of material in this book. The author has taught an introductory one-quarter "breadth" course on basic laser concepts for engineering and applied physics students using most of the material from the first part of the book on "Basic Laser Physics" (see the Table of Contents), especially Chapters 1–4, 6–8 and 11–13. A second-quarter "depth" course then adds more advanced material from Chapters 5, 9, 10, 30, 31 and selected sections from Chapters 24–29. A complete course on optical beams and resonators can be taught from Chapters 14 through 23.

I am very much indebted to many colleagues for help during the many years while this book was being written. I wish it were possible to thank by name all the students in my classes and my research group who lived through too many years of drafts and class notes. Special thanks must go to Judy Clark, who became a TeX and computer expert and did so much of the editing and manuscript preparation; to the Air Force Office of Scientific Research for supporting my laser research activities over many years; to Stanford University, and especially to Donald Knuth, for providing the environment, and the computerized text preparation tools, in which this book could be written; and to the Alexander von Humboldt Foundation and the Max Planck Institute for Quantum Optics in Munich, who supplied the opportunity for the manuscript at last to be completed. Finally, there are my wife Jeannie, and my family, who made it all worthwhile.

Anthony E. Siegman

### UNITS AND NOTATION

The units and dimensions in this book are almost entirely mks, or SI, except for a few concessions to long-established habits such as expressing atomic densities N in atoms/cm<sup>3</sup> and cross sections  $\sigma$  in cm<sup>2</sup>. Such non-mks values should of course always be converted to mks units before plugging them into formulas.

In general, lower-case symbols in bold-face type such as  $\mathcal{E}(r,t)$ ,  $\mathbf{b}(r,t)$ ,  $\mathbf{h}(r,t)$ , and so on refer to electromagnetic field quantities as real vector functions of space and time, while  $\mathcal{E}(r,t)$ , b(r,t), h(r,t), etc., refer to the scalar counterparts of the same quantities. Bold-face capital letters  $\mathbf{E}$ ,  $\mathbf{B}$ ,  $\mathbf{H}$ , etc., refer to the complex phasor amplitudes of the same vector quantities with  $e^{j\omega t}$  variations, while  $\tilde{E}$ ,  $\tilde{B}$ ,  $\tilde{H}$ , etc., are the complex phasor amplitudes of the corresponding scalars. As illustrated here, complex quantities are sometimes, but not always, identified by a superposed tilde.

In writing sinusoidal signals and waves, waves propagating toward positive z are written in the "electrical engineer's form" of  $\exp j(\omega t - \beta z)$  rather than the "physicist's form" of  $\exp i(kz - \nu t)$ . (This of course does not imply that  $i \equiv -j!$ ) Linewidths  $\Delta f$ ,  $\Delta \omega$ ,  $\Delta \lambda$  and pulsewidths  $\Delta t$ ,  $\tau$  or T, unless specifically noted, always mean the full width at half maximum (FWHM).

In contrast to much of the published literature, an attenuation or gain coefficient  $\alpha$  in this book always refers to an amplitude or voltage growth rate, such as for example  $\mathcal{E}(z) = \mathcal{E}(0) \exp \pm \alpha z$ . Signal powers or intensities in this book, therefore, always grow or attenuate with exponential growth coefficients  $2\alpha$  rather than  $\alpha$ .

The notation in the book has a few other minor idiosyncrasies. First, we are often concerned with signals and waves inside laser crystals, in which the host crystal itself has a dielectric constant  $\epsilon$  and an index of refraction n even without any atomic transition present. To take the dielectric properties of a possible host medium into account, the symbols  $\epsilon$ , c and  $\lambda$  in formulas in this text always refer to the dielectric permeability, velocity of light and wavelength of the radiation in the dielectric medium if there is one. We then use  $c_0$  and  $\lambda_0$  in the few cases where it is necessary to refer to these same quantities specifically in vacuum. The advantage of this choice is that all our formulas involving  $\epsilon$ , c and  $\lambda$  remain correct with or without a dielectric host medium, without needing to clutter these formulas with different powers of the refractive index n.

The other special convention peculiar to this book is the nonstandard manner in which we define the complex susceptibility  $\tilde{\chi}_{at}$  associated with a resonant atomic transition. In brief, we define the linear relationship between the induced polarization  $\tilde{P}_{at}$  on an atomic transition in a laser medium and the electric field  $\tilde{E}$  that produces this polarization by the convention that  $\tilde{P}_{at} = \tilde{\chi}_{at} \epsilon \tilde{E}$  where  $\epsilon$  is the dielectric permeability of the host laser crystal rather than the vacuum value  $\epsilon_0$  usually used in this definition. The merits of this nonstandard approach are argued in Chapter 2.

### LIST OF SYMBOLS

Throughout this text we attempt to follow a consistent notation for subscripts, using the conventions that:

- a= either atomic, as in atomic transition frequency  $\omega_a$  or homogeneous atomic linewidth  $\Delta\omega_a$ ; or sometimes absorption, as in absorption coefficient  $\alpha_a$ .
- c = cavity, as in cavity decay time  $\tau_c$  or cavity energy decay rate  $\gamma_c$ ; also, carrier, as in carrier frequency  $\omega_c$ .
- d = doppler, as in doppler broadening with linewidth  $\Delta \omega_d$ , and by extension any other kind of inhomogeneous broadening.
- e = external, as in cavity external coupling factor  $\delta_e$  or external decay rate  $\gamma_e$ ; also, sometimes, effective, as in effective lifetime or pumping rate.
- m = molecular or maser, generally used to refer to atomic or maser or laser quantities, e.g., laser gain coefficient  $\alpha_m$  or laser growth rate  $\gamma_m$ .
- o=ohmic, referring generally to internal ohmic and/or scattering losses, as in the ohmic loss coefficient  $\alpha_0$  or ohmic cavity decay rate  $\gamma_0$ . Also used in several other ways, generally to indicate an initial value; a thermal equilibrium value; a small-signal or unsaturated value; a midband value; or a free-space (vacuum) values, as in  $c_0$ ,  $\epsilon_0$ , and  $\lambda_0$ .
- p = pump, as in pumping rate  $R_p$  or pump transition probability  $W_p$ .

We also frequently use  $at \equiv axial$ ;  $avail \equiv available$ ;  $circ \equiv circulating$ ;  $eff \equiv effective$ ;  $eq \equiv equivalent$ ;  $inc \equiv incident$ ;  $opt \equiv optimum$ ;  $out \equiv output$ ;  $refl \equiv reflected$ ;  $rt \equiv round-trip$ ;  $sat \equiv saturation$ ;  $sp \equiv spontaneous$  or spiking;  $ss \equiv small-signal$  or steady-state; and  $th \equiv threshold$  as compound subscripts.

A partial list of symbols used in the text then includes:

- $\alpha$  = exponential gain or loss coefficient for amplitude (or voltage); also, amplitude parameter for gaussian optical pulse
- $\alpha''$  = second derivative of  $\alpha(\omega)$  with respect to  $\omega$
- $\tilde{\alpha}_n = \text{complex amplitude of } n\text{-th order Hermite-gaussian mode}$
- $\alpha_{\rm m} = {\rm maser/laser/molecular\ gain\ (or\ loss)\ coefficient}$
- $\alpha_0$  = ohmic and/or scattering loss coefficient
- $\beta$  = propagation-constant, including host dielectric effects, but usually not loss or atomic transition effects; also, chirp parameter for gaussian pulse; relaxation-time ratio in multilevel laser pumping systems; Bohr magneton
- $\beta_I = \text{Nuclear magneton}$
- $\beta', \beta'' =$  first and second derivatives of  $\beta(\omega)$  with respect to  $\omega$
- $\Delta \beta_m$  = added propagation constant term due to reactive part of an atomic transition

 $\gamma = \text{in general}$ , an energy or population decay rate

 $\gamma_c = \text{decay rate for cavity stored energy } (\equiv 1/\tau_c)$ 

 $\gamma_i$  = total downward population decay rate from energy level  $E_i$ 

 $\gamma_{ij}$  = population decay rate from upper level  $E_i$  to lower level  $E_i$ 

 $\gamma_{nr}$  = nonradiative part of total decay rate for a classical oscillator or an atomic transition

 $\gamma_{rad}$  = radiative decay rate for classical electron oscillator or real atomic transition

 $\tilde{\gamma} = \text{complex eigenvalue for optical resonator or lensquide}$ 

 $\tilde{\gamma}_{mn} = \text{complex eigenvalue for } mn$ -th order transverse eigenmode

 $\Gamma = \alpha + j\beta = ext{complex propagation constant for an optical wave}$ 

 $\Gamma = \alpha - j\beta = \text{complex gaussian pulse parameter}$ 

 $\delta$  = coefficient of (logarithmic) fractional power gain or loss, per bounce or per round trip

 $\delta_c = ext{total (round-trip)}$  power loss coefficient due to cavity losses plus external coupling

 $\delta_e$  = cavity loss coefficient due to external coupling only

 $\delta_m$  = power gain coefficient due to laser atoms

 $\delta_0 = \text{cavity less coefficient due to internal (ohmic) losses only}$ 

 $\Delta_m = AM$  or FM modulation index

 $\epsilon =$  dielectric permeability of a medium

 $\epsilon_0$  = dielectric permeability of free space (vacuum)

 $\eta=$  efficiencies of various sorts; also, characteristic impedance  $\sqrt{\mu/\epsilon}$  of a dielectric medium

 $\eta_0$  = characteristic impedance of free space (vacuum)

 $\lambda = \text{optical wavelength}$  (in a medium); also, eigenvalue for optical ray matrix

 $\lambda_0$  = optical wavelength in vacuum

 $\lambda_a, \lambda_b =$  eigenvalues of periodic lensguide or ABCD matrix

 $\Lambda =$ spatial period of optical grating

 $\mu=$  electric or magnetic dipole moment; also, magnetic permeability of a magnetic medium

 $\mu_e$  = electric dipole moment

 $\mu_m = \text{magnetic dipole moment}$ 

 $\mu_0$  = magnetic permeability of free space

 $\rho$  = amplitude reflection or transmission of optical mirror or beamsplitter; also, distance between two points;  $\rho(\omega)$  = cavity mode density

 $\tilde{
ho}=$  complex amplitude reflection or transmission of optical mirror or beamsplitter

 $\sigma$  = ohmic conductivity; also, transition cross section, standard deviation

 $\sigma_{ij} =$ cross section for stimulated transition from level  $E_i$  to  $E_j$ 

 $\tau$  = lifetime or decay time

 $\tau_c$  = cavity decay time due to all internal losses plus external coupling

 $\tau_i$  = total lifetime (energy decay time) for energy level  $E_i$ 

 $\theta, \phi, \psi$  = phase shifts and phase angles of various sorts

 $\psi(\mathbf{r},t) =$ Schrödinger wave function

 $\psi_{mn}$  = Guoy phase shift for an mn-th order gaussian beam

 $\tilde{\chi} = \text{susceptibility of a dielectric or magnetic medium} = \chi' + j\chi''$ 

 $\chi', \chi'' = \text{real and imaginary parts of } \tilde{\chi}$ 

 $\tilde{\chi}_{at}$  = susceptibility of a resonant atomic transition

 $\tilde{\chi}_e, \tilde{\chi}_m = \text{electric (magnetic) dipole susceptibilities}$ 

 $\omega = \text{frequency (in radians/second)}$ 

 $\omega'$  = in general, a frequency that has been shifted, pulled, or modified in some small manner

 $\omega_a$  = atomic transition frequency

 $\omega_b =$  a beat frequency (between two signals)

 $\omega_c$  = cavity or circuit resonant frequency; also, carrier frequency

 $\omega_i(t)$  = instantaneous frequency of a phase-modulated signal

 $\omega_m$  = generally, a modulation frequency of some sort

 $\omega_q$  = resonant frequency of q-th axial mode

 $\omega_R$  = Rabi frequency on an atomic transition

 $\omega_{sp} = \text{Spiking or relaxation-oscillation frequency}$ 

 $\delta\omega_q$  = frequency pulling of axial mode frequency  $\omega_q$ 

 $\Delta \omega = \text{linewidth}$ , or frequency tuning, in radians/sec

 $\Delta\omega_a = \text{atomic linewidth (FWHM)}$ nin radians/sec

 $\Delta\omega_{ax}$  = axial mode spacing between adjacent axial modes

 $\Omega$  = solid angle; also, radian frequency or rotation rate

 $\tilde{a}_i, \tilde{b}_i = \text{normalized wave amplitudes}$ 

A = area

 $A_{ji} = \text{Einstein } A \text{ coefficient on } E_j \rightarrow E_i \text{ transition}$ 

ABCD = matrix elements for optical ray matrix or paraxial optical system

b = magnetic field as real function of space and time; also, confocal parameter for gaussian beam

 b = magnetic field as real vector function of space and time; also, confocal parameter for gaussian beam

B = magnetic field; also, pressure-broadening coefficient or "B integral" for nonlinear interaction

 $\tilde{B} = \text{phasor amplitude of sinusoidal } B \text{ field}$ 

c = velocity of light in a material medium

 $c_0$  = velocity of light in vacuum

C =in general, an unspecified constant; also, electrical capacitance; coupling coefficient in mode competition analysis

CC =complex conjugate (of preceding term)

CEO = classical electron oscillator model

d = electric displacement as real function of space and time; also, distance or displacement

d = electric displacement as real vector function of space and time

D =dimensionless dispersion parameter

 $\tilde{D}$  = phasor amplitude of sinusoidal electric displacement

e =magnitude of electronic charge

 $\mathcal{E}$  = electric field; usually, real field  $\mathcal{E}(x,t)$  as function of space and time

 $\tilde{E} = \text{phasor amplitude of sinusoidal } E \text{ field}$ 

 $E_n(t)$  = amplitude of *n*-th mode in a normal mode expansion

f = frequency in Hz ( $\equiv$  cycles/sec); also, lens focal length

 $f^{\#} = \text{lens } f\text{-number}$ 

 $\Delta f$  = linewidth, or frequency detuning, in Hz

 $\Delta f_a$  = atomic transition linewidth (FWHM) in Hz

 $\Delta f_d$  = doppler or inhomogeneous linewidth (FWHM) in Hz

 $\vec{F}$  = oscillator strength for an atomic transition; also, lens f-number

 $\mathcal{F}$  = finesse, of interferometer or laser cavity

 $\tilde{F}(x) =$  Fresnel integral function

 $F_{ji} = \text{oscillator strength of } E_j \rightarrow E_i \text{ atomic transition } \equiv \gamma_{\text{rad},ji}/3\gamma_{\text{rad,ceo}}$ 

g = amplitude (or voltage) gain, as a number; also, gaussian stable resonator parameter; magnetic resonance g value

 $g(v), g(\omega) = \text{normalized lineshapes}$ 

 $\tilde{g} = \text{complex amplitude (or voltage) gain, as a (complex) number}$ 

 $g_i, g_j =$  degeneracy factors for quantum energy levels  $E_i$  and  $E_j$ 

 $g_I$  = nuclear magnetic resonance g value

 $\tilde{g}_{rt}$  = round-trip voltage gain inside an optical cavity

G =power gain (as a number); also, electrical conductance

 $G_{dB}$  = power gain in decibels

h = magnetic intensity as real function of space and time; also, Planck's constant

 $\hbar = h/2\pi$ 

h = magnetic H field as real vector function of space and time

 $h_n = n$ -th order polynomial function

 $\tilde{H}$  = phasor amplitude of sinusoidal H field

 $H_n = n$ -th order hermite polynomial

 $I = \text{intensity (power/unit area) of an optical wave; also sometimes, loosely, total power in the wave$ 

 $I_m = \text{modified Bessel function of order } m$ 

 $I_{sat} = \text{amplifier (or absorber) saturation intensity}$ 

j =current density as real function of space and time; also,  $\sqrt{-1}$ 

j = current density as real vector function of space and time

J = phasor amplitude of sinusoidal current density

 $J_m =$ Bessel function of order m

 $k = \text{propagation vector of optical wave} = \omega/c$ 

K =scalar constant in various equations (especially coupled rate equations); also, spring constant in classical oscillator model

L = length; electrical inductance

m = electron mass; also, magnetization (magnetic dipole moment per unit volume) as real function of time

m = magnetization (magnetic dipole moment per unit volume) as real vector function of space and time

 $m, \tilde{m} = \text{half-trace parameter for ray or } ABCD \text{ matrix}$ 

M =proton mass; molecular mass

 $\tilde{M}=$  phasor amplitude of sinusoidal magnetic dipole moment

M = optical ray matrix or ABCD matrix

n = refractive index; also, photon number n(t) (number of photons per cavity mode)

 $n_2 =$ optical Kerr coefficient  $n_{2E}$  or  $n_{2I}$ 

N = atomic number or level population; usually interpreted as atoms per unit volume, sometimes as total number of atoms

 $\Delta N = ext{population difference, or population difference density, on an atomic transition } (\Delta N_{ij} \equiv N_i - N_j)$ 

N = Fresnel number  $a^2/L\lambda$  for an optical beam or resonator

 $N_c =$ collimated Fresnel number for an unstable optical resonator

 $N_{eq}$  = equivalent Fresnel number for an unstable optical resonator

 $N_i$  = population, or population density, in atomic energy level  $E_i$ 

p = perimeter, period or round-trip path length, for cavities or periodic lensguides; also, electric polarization (electric dipole moment per unit volume) as real function of time, and laser mode density or mode number

p = electric polarization (electric dipole moment per unit volume) as real vector function of space and time

 $p_m$  = path length (round-trip) through an atomic or laser gain medium

P =power, in watts; also, pressure, in torr

 $P_n(t)$  = polarization driving term for *n*-th order cavity mode in coupled-mode expansion

P = phasor amplitude of sinusoidal electric polarization

q =axial mode index

 $\tilde{q}=$  complex gaussian beam parameter or complex radius of curvature

 $\hat{q}$  = reduced gaussian beam parameter,  $\tilde{q}/n$ 

\* = amplitude reflectivity of mirror or beamsplitter; also, dimensionless or normalized pumping rate; displacement off axis of optical ray

r' = reduced slope n dr/dz for optical ray

r = shorthand for spatial coordinates x, y, z

 $\tilde{r}_{ij} = \text{complex scattering matrix element, or mirror or beamsplitter reflection coefficient}$ 

 $r_p$  = dimensionless pumping rate or inversion ratio, relative to threshold pumping rate or threshold inversion density

dr = volume element, dV or dx dy dz

R = power reflectivity of mirror or beamsplitter ( $\equiv |r|^2$ ); also, electrical resistance; radius of curvature for mirror, dielectric interface, or optical wave

 $\hat{R}$  = reduced radius of curvature R/n.

 $R_p$  = pumping rate in atoms per second and, usually, per unit volume

s = spatial frequency (cycles/unit length)

s = shorthand for transverse spatial coordinates x, y

ds = transverse area element dA or dx dy

 $S = \text{multiport scattering matrix (matrix elements } S_{ij})$ 

t =time; also, amplitude transmission through mirror, beamsplitter, or light modulator

 $ilde{t} = ext{complex amplitude transmission coefficient through mirror, beamsplitter or light modulator}$ 

 $ilde{t}_{ij} = ext{complex scattering matrix element, or mirror/beamsplitter transmission coefficient}$ 

 $T = \text{power transmission of mirror or beamsplitter } (\equiv |t|^2); \text{ also, cavity round-trip transit time, or temperature } (K)$ 

T =dimensionless susceptibility tensor

 $T_b =$ laser oscillation build-up time

 $T_{nr}$  = temperature of "nonradiative" surroundings

 $T_{rad}$  = temperature of radiative surroundings

 $T_1$  = energy decay time, population recovery time, longitudinal relaxation time

 $T_2$  = dephasing time, collision time, transverse relaxation time

 $T_2^*$  = effective  $T_2$  or dephasing time for inhomogeneous (gaussian) transition

 $\tilde{u} = \text{complex}$  (and usually normalized) optical wave amplitude

U =energy or, more commonly, energy density (energy per unit volume)

 $U_a$  = energy density in a collection of atoms or atomic energy level populations

 $U_{bbr} =$ energy density of blackbody radiation

v = velocity of an atom, an electron, or a wave

 $\tilde{v} = \text{complex spot size for Hermite-gaussian modes}$ 

 $v_g = \text{group velocity}$ 

 $v_{\phi} = \text{phase velocity}$ 

 $V, V_c = \text{volume (of a cavity mode or field pattern)}$ 

w = gaussian spot size parameter (1/e amplitude point)

 $w_{ij}$  = total relaxation transition probability (per atom, per second) from level  $E_i$  to level  $E_j$ 

 $W_{ij}$  = stimulated transition probability (per atom, per second) from level  $E_i$  to level  $E_j$ 

 $W_p$  = pumping transition probability (per atom, per second)

x(t) = displacement of electronic charge in classical electron oscillator model

 $z_D$  = dispersion length for dispersive pulse broadening

 $z_R$  = Rayleigh range for a gaussian or collimated optical beam

Z = atomic number

 $2^*$  = dimensionless population saturation factor, with values between  $2^* = 1$  (lower level empties out rapidly) and  $2^* = 2$  (lower level bottlenecked)

3\* = dimensionless polarization overlap factor for atomic interactions, with numerical value between 0 and 3

### CONTENTS

	Pretace	XIII
	Units and Notation	xv
	List of Symbols	xvii
BASIC L	ASER PHYSICS	
1.	An Introduction to Lasers	1
2.	Stimulated Transitions: The Classical Oscillator Model	80
3.	Electric Dipole Transitions in Real Atoms	118
4.	Atomic Rate Equations	176
5.	The Rabi Frequency	221
6.	Laser Pumping and Population Inversion	243
7.	Laser Amplification	264
8.	More On Laser Amplification	307
9.	Linear Pulse Propagation	331
10.	Nonlinear Optical Pulse Propagation	362
11.	Laser Mirrors and Regenerative Feedback	398
12.	Fundamentals of Laser Oscillation	457
13.	Oscillation Dynamics and Oscillation Threshold	491
	•	
OPTICA	AL BEAMS AND RESONATORS	
14.	Optical Beams and Resonators: An Introduction	558
15.	Ray Optics and Ray Matrices	581
16.	Wave Optics and Gaussian Beams	626
17.	Physical Properties of Gaussian Beams	663
18.	Beam Perturbation and Diffraction	698
19.	Stable Two-Mirror Resonators	744
20.	Complex Paraxial Wave Optics	777
21.	Generalized Paraxial Resonator Theory	815
22.	Unstable Optical Resonators	858
23.	More on Unstable Resonators	891
I ASER	DYNAMICS AND ADVANCED TOPICS	•
24.	Laser Dynamics: The Laser Cavity Equations	923
<b>2</b> 5.	Laser Spiking and Mode Competition	954
26.		1004
27.	Active Laser Mode Coupling	1041
<sup>3</sup> 28.		1104
29.	· · · · · · · · · · · · · · · · · · ·	1129
30.	Hole Burning and Saturation Spectroscopy	1171
31.	Magnetic-Dipole Transitions	1213

## LIST OF TOPICS

	Pretace	X111
	Units and Notation	xv
	List of Symbols	xvi
BASIC LAS	SER PHYSICS	
Chapter 1	An Introduction to Lasers	
1.1	What Is a Laser?	2
1.2	Atomic Energy Levels and Spontaneous Emission	6
1.3	Stimulated Atomic Transitions	18
1.4	Laser Amplification	30
1.5	Laser Pumping and Population Inversion	35
1.6	Laser Oscillation and Laser Cavity Modes	39
1.7 •	Laser Output-Beam Properties	49
1.8	A Few Practical Examples	60
1.9	Other Properties of Real Lasers	66
1 1 0	Historical Background of the Laser	74
1.11	Additional Problems for Chapter 1	76
Chapter 2	Stimulated Transitions: The Classical Oscillator Mo	del
2.1	The Classical Electron Oscillator	80
2.2	Collisions and Dephasing Processes	89
2.3	More on Atomic Dynamics and Dephasing	97
2.4	Steady-Ctate Response: The Atomic Susceptibility	102
<b>2.5</b>	Conversion to Real Atomic Transitions	110
Chapter 3	Electric Dipole Transitions in Real Atoms	
3.1 ·	Decay Rates and Transition Strengths in Real Atoms	118
3.2	Line Broadening Mechanisms in Real Atoms	126
3.3	Polarization Properties of Atomic Transitions	135
3.4	Tensor Susceptibilities	143
3.5	The "Factor of Three"	150
3.6	Degenerate Energy Levels and Degeneracy Factors	153
3.7	Inhomogeneous Line Broadening	157
Chapter 4	Atomic Rate Equations	
<i>A</i> 1	Power Transfer From Signals to Atoms	176

4.2	Stimulated Transition Probability	181
4.3	Blackbody Radiation and Radiative Relaxation	187
4.4	Nonradiative Relaxation	195
4.5	Two-Level Rate Equations and Saturation	204
4.6	Multilevel Rate Equations	211
Chapter 5	The Rabi Frequency	
5.1	Validity of the Rate Equation Model	221
5.2	Strong Signal Behavior: The Rabi Frequency	229
Chapter 6	Laser Pumping and Population Inversion	
6.1	Steady-State Laser Pumping and Population Inversion	243
6.2	Laser Gain Saturation	252
6.3	Transient Laser Pumping	257
Chapter 7	Laser Amplification	•
7.1	Practical Aspects of Laser Amplifiers	264
7.2	Wave Propagation in an Atomic Medium	266
7.3	The Paraxial Wave Equation	276
7.4	Single-Pass Laser Amplification	279
7.5	Stimulated Transition Cross Sections	286
7.6	Saturation Intensities in Laser Materials	292
7.7	Homogeneous Saturation in Laser Amplifiers	297
Chapter 8	More On Laser Amplification	
8.1	Transient Response of Laser Amplifiers	307
8.2	Spatial Hole Burning, and Standing-Wave Grating Effects	316
8.3	More on Laser Amplifier Saturation	323
Chapter 9	Linear Pulse Propagation	
9.1	Phase and Group Velocities	331
9.2	The Parabolic Equation	339
9.3	Group Velocity Dispersion and Pulse Compression	343
9.4	Phase and Group Velocities in Resonant Atomic Media	351
9.5	Pulse Broadening and Gain Dispersion	356
Chapter 10	Nonlinear Optical Pulse Propagation	
10.1	Pulse Amplification With Homogeneous Gain Saturation	362
10.2	Pulse Propagation in Nonlinear Dispersive Systems	375
10.3	The Nonlinear Schrödinger Equation	387
10.4	Nonlinear Pulse Broadening in Optical Fibers	388
10.5	Solitons in Optical Fibers	392
Chapter 11	Laser Mirrors and Regenerative Feedback	
11.1	Laser Mirrors and Beam Splitters	398
11.2	Interferometers and Resonant Optical Cavities	408
. 11.3	Resonance Properties of Passive Optical Cavities	413

11.4	"Delta Notation" for Cavity Gains and Losses	<b>428</b>
11.5	Optical-Cavity Mode Frequencies	432
11.6	Regenerative Laser Amplification	440
11.7	Approaching Threshold: The Highly Regenerative Limit	447
Chapter 12	Fundamentals of Laser Oscillation	
12.1	Oscillation Threshold Conditions	457
12.2	Oscillation Frequency and Frequency Pulling	462
12.3	Laser Output Power	473
12.4	The Large Output Coupling Case	485
Chapter 13	Oscillation Dynamics and Oscillation Threshold	
13.1	Laser Oscillation Buildup	491
13.2	Derivation of the Cavity Rate Equation	497
13.3	Coupled Cavity and Atomic Rate Equations	505
13.4	The Laser Threshold Region	510
13.5	Multiple-Mirror Cavities and Etalon Effects	524
13.6	Unidirectional Ring-Laser Oscillators	532
13.7	Bistable Optical Systems	538
13.8	Amplified Spontaneous Emission and Mirrorless Lasers	547
14.1 14.2	Optical Beams and Resonators: An Introduction  Transverse Modes in Optical Resonators  The Mathematics of Optical Resonator Modes	559 565
14.3	Build-Up and Oscillation of Optical Resonator Modes	569
Chapter 15	Ray Optics and Ray Matrices	
15.1	Paraxial Optical Rays and Ray Matrices	581
15.2	Ray Propagation Through Cascaded Elements	593
15.3	Rays in Periodic Focusing Systems	599
15.4	Ray Optics With Misaligned Elements	607
15.5	Ray Matrices in Curved Ducts	614
15.6	Nonorthogonal Ray Matrices	616
Chapter 16	Wave Optics and Gaussian Beams	
16.1	The Paraxial Wave Equation	626
16.2	Huygens' Integral	630
16.3	Gaussian Spherical Waves	637
16.4	Higher-Order Gaussian Modes	642
16.5	Complex-Argument Gaussian Modes	649
16.6	Gaussian Beam Propagation in Ducts	652

Chapter 17	Physical Properties of Gaussian Beams	
< 17.1	Gaussian Beam Propagation	663
17.2	Gaussian Beam Focusing	675
17.3	Lens Laws and Gaussian Mode Matching	680
17.4	Axial Phase Shift: The Guoy Effect	682
17.5	Higher-Order Gaussian Modes	685
17.6	Multimode Optical Beams	695
Chapter 18	Beam Perturbation and Diffraction	
18.1	Grating Diffraction and Scattering Effects	698
18.2	Aberrated Laser Beams	706
18.3	Aperture Diffraction: Rectangular Apertures	712
18.4	Aperture Diffraction: Circular Apertures	727
Chapter 19	Stable Two-Mirror Resonators	
19.1 '	Stable Gaussian Resonator Modes	744
19.2	Important Stable Resonator Types	750
19.3	Gaussian Transverse Mode Frequencies	761
19.4	Misalignment Effects in Stable Resonators	767
19.5	Gaussian Resonator Mode Losses	769
Chapter 20	Complex Paraxial Wave Optics	
20.1	Huygens' Integral and ABCD Matrices	777
20.2	Gaussian Beams and ABCD Matrices	782
20.3	Gaussian Apertures and Complex ABCD Matrices	786
20.4	Complex Paraxial Optics	792
20.5	Complex Hermite-Gaussian Modes	798
20.6	Coordinate Scaling with Huygens' Integrals	805
20.7	Synthesis and Factorization of ABCD Matrices	811
Chapter 21	Generalized Paraxial Resonator Theory	
21.1	Complex Paraxial Resonator Analysis	815
21.2	Real and Geometrically Stable Resonators	820
21.3	Real and Geometrically Unstable Resonators	822
21.4	Complex Stable and Unstable Resonators	828
21.5	Other General Properties of Paraxial Resonators	835
21.6	Multi-Element Stable Resonator Designs	841
21.7	Orthogonality Properties of Optical Resonator Modes	847
Chapter 22	Unstable Optical Resonators	
22.1	Elementary Properties	858
22.2	Canonical Analysis for Unstable Resonators	867
22.3	Hard-Edged Unstable Resonators	874
22.4	Unstable Resonators: Experimental Results	884
Chapter 23	More on Unstable Resonators	100
23.1	Advanced Analyses of Unstable Resonators	891

23.2	Other Novel Unstable Resonator Designs	899
23.3	Variable-Reflectivity Unstable Resonators	913
LASER DYN	NAMICS AND ADVANCED TOPICS	
Chapter 24	Laser Dynamics: The Laser Cavity Equations	
24.1	Derivation of the Laser Cavity Equations	923
24.2	External Signal Sources	932
24.3	Coupled Cavity-Atom Equations	941
24.4	Alternative Formulations of the Laser Equations	944
24.5	Cavity and Atomic Rate Equations	949
Chapter 25	Laser Spiking and Mode Competition	
25.1	Laser Spiking and Relaxation Oscillations	955
<b>25.2</b>	Laser Amplitude Modulation	971
25.3	Laser Frequency Modulation and Frequency Switching	980
25.4	Laser Mode Competition	992
Chapter 26	Laser Q-Switching	
26.1	Laser Q-Switching: General Description	1004
26.2	Active Q-Switching: Rate-Equation Analysis	1008
26.3	Passive (Saturable Absorber) Q-Switching	1024
26.4	Repetitive Laser Q-Switching	1028
26.5	Mode Selection in $Q$ -Switched Lasers	. 1034
26.6	Q-Switched Laser Applications	1039
Chapter 27	Active Laser Mode Coupling	
27.1	Optical Signals: Time and Frequency Descriptions	1041
27.2	Mode-Locked Lasers: An Overview	1056
27.3	Time-Domain Analysis: Homogeneous Mode Locking	1061
27.4	Transient and Detuning Effects	1075
27.5	Frequency-Domain Analysis: Coupled Mode Equations	1087
27.6	The Modulator Polarization Term	1092
27.7	FM Laser Operation	1095
Chapter 28	Passive Mode Locking	
28.1	Pulse Shortening in Saturable Absorbers	1104
28.2	Passive Mode Locking in Pulsed Lasers	1109
28.3	Passive Mode Locking in CW Lasers	1117
Chapter 29	Laser Injection Locking	
29.1	Injection Locking of Oscillators	1130
29.2	Basic Injection Locking Analysis	1138
29.3	The Locked Oscillator Regime	1142
29.4	Solutions Outside the Locking Range	1148