

# **CONCEPTS AND TECHNIQUES IN URBAN ANALYSIS**

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'Bola Ayeni

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*'Bola Ayemi*



**ROUTLEDGE**

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'BOLA AYENI

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