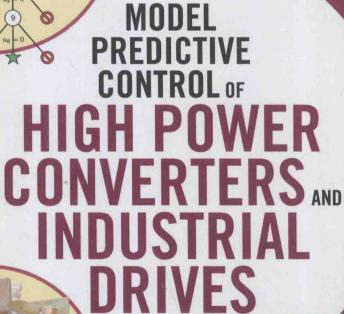
TOBIAS GEYER





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# MODEL PREDICTIVE CONTROL OF HIGH POWER CONVERTERS AND INDUSTRIAL DRIVES

**Tobias Geyer** 

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# To Luci, David, and Jan

## Preface

This book focuses on model predictive control (MPC) schemes for industrial power electronics. The emphasis is on three-phase ac-dc and dc-ac power conversion systems for high-power applications of 1 MVA and above. These systems are predominantly based on multilevel voltage source converters that operate at switching frequencies well below 1 kHz. The book mostly considers medium-voltage (MV), variable-speed drive systems and, to a lesser extent, MV grid-connected converters. The proposed control techniques can also be applied to low-voltage power converters when operated at low pulse number, that is, at small ratios between the switching frequency and the fundamental frequency.

For high-power converters, the pulse number typically ranges between 5 and 15. As a result, the concept of averaging, which is commonly applied to power electronic systems to conceal the switching aspect from the control problem, leads to performance deterioration. In general, to achieve the highest possible performance for a high-power converter, averaging is to be avoided, and the traditionally used current control loop and modulator should be replaced by one single control entity.

This book proposes and reviews control methods that fully exploit the performance potential of high-power converters, by ensuring fast control at very low switching frequencies and low harmonic distortions. To achieve this, the control and modulation problem is addressed in one computational stage. Long prediction horizons are required for the MPC controllers to achieve excellent steady-state performance. The resulting optimization problem is computationally challenging, but can be solved in real time by branch-and-bound methods. Alternatively, the optimal switching sequence to be applied during steady-state operation—the so-called optimized pulse pattern (OPP)—can be precomputed offline and refined online to achieve fast closed-loop control.

To this end, the research vision is to combine the benefits of deadbeat control methods (such as direct torque control) with the optimal steady-state performance of OPPs, by resolving the antagonism between the two. Three such MPC methods are presented in detail.

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First and foremost, I would like to thank Georgios Papafotiou, who introduced me to the exciting field of power electronics, Stefan Schröder, who taught me the fundamentals of high power electronics, and Manfred Morari, who showed me how to achieve meaningful research results.

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# List of Abbreviations

### Abbreviations

alternating current

A/D

analog-to-digital

AFE

active front end

ANPC

active neutral-point-clamped

CB-PWM

carrier-based pulse width modulation

CPU DB

central processing unit deadbeat

de

direct current

DFE

diode front end

DFT

discrete Fourier transform

DPC

direct power control

DSC

direct self-control

DSP

digital signal processor direct torque control

DTC **EMF** 

electromotive force

FACTS

flexible ac transmission system

FC.

flying capacitor

FCS

finite control set

FOC

field-oriented control

FPGA

field-programmable gate array gate-commutated thyristor

GCT

**IGBT** 

insulated-gate bipolar transistor

IGCT

integrated-gate-commutated thyristor

IM

induction machine

LOR

linear quadratic regulator

MIMO MLD

multiple-input multiple-output

MMC

mixed logical dynamical modular multilevel converter

MPC

model predictive control

MPDBC

model predictive direct balancing control

MPDCC

model predictive direct current control

MPDPC model predictive direct power control model predictive direct torque control model predictive pulse pattern control

MV medium-voltage
NPC neutral-point-clamped
OPP optimized pulse pattern
PCC point of common coupling
PI proportional-integral

PMSM permanent magnet synchronous machine

pu per unit

PWM pulse width modulation QP quadratic program rms root-mean-square

SHE selective harmonic elimination
SISO single-input single-output
SVM space vector modulation
TDD total demand distortion
THD total harmonic distortion

VC vector control
V/f volts per frequency
VOC voltage-oriented control
VSD variable-speed drive
VSI voltage source inverter

### Variables

 $\begin{array}{ll} i,\,v & \text{instantaneous value of variables that are functions of time} \\ \vec{i},\,\vec{v} & \text{space vectors} \\ I,\,V & \text{rms values} \\ x & \text{column vector} \\ x^T & \text{row vector} \\ X & \text{matrix} \\ \mathcal{S} & \text{set} \end{array}$ 

### Symbols

 $egin{array}{ll} \mathbf{0}_{n imes m} & ext{zero matrix of dimensions } n imes m \ A & ext{system matrix (discrete time)} \ B & ext{input matrix (discrete time)} \end{array}$ 

c coefficient C capacitance (F)

C input matrix (continuous or discrete time)

 $egin{array}{ll} d & & \text{pulse number} \\ D & & \text{determinant} \\ e,E & & \text{energy (J or pu)} \\ f & & \text{frequency (Hz or pu)} \\ \end{array}$ 

F system matrix (continuous time)
G input matrix (continuous time)

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```
H
           Hessian matrix
i, i, I
           current (A or pu)
           identity matrix of dimensions n \times n, I_n = \text{diag}(1, 1, \dots, 1)
I_n
           imaginary unit, \sqrt{-1}
j
J
           cost function
k-
           discrete time step
K
           transformation matrix
           discrete time step (relative to k)
L
           inductance (H)
           modulation index
m
M
            moment of inertia (kg m<sup>2</sup> or pu)
            order of harmonic, number of modules
n
N
            length of switching sequence
            number of pole pairs
p
            power factor
pf
P
            (instantaneous) real power (W or pu)
0
            (instantaneous) reactive power (Var or pu)
q, Q
            penalty vector or matrix
R
            resistance (\Omega or pu)
sl
S
            apparent power (V A or pu)
t
            time (s or pu)
T
            torque (N m or pu)
            switch position, input (or manipulated) variable
71. 71.
\Delta u, \Delta u
            change in switch position
U, U
            sequence of switch positions (switching sequence)
v, v, V
            voltage (V or pu)
V
            generator matrix
x. x
            state variable
X
            reactance (pu)
            output variable
y. y
 Z
            impedance (\Omega or pu)
a
            switching angle in pulse pattern (rad)
            load angle, that is, angle between the stator and rotor flux vectors (rad)
8
            (half of the) bound width
€. €
            degree of bound violation (at a time step)
            rms bound violation (over the prediction horizon)
€. €
 X
            scalar penalty weight
 X
            flux linkage vector (Wb)
            phase angle (rad)
            radius of sphere
 P
            total leakage factor
 \sigma
 A
            angle (argument) in pulse pattern (rad)
 \nu, \nu
            insertion index
            angular position of a reference frame (rad)
 10.10
            flux (linkage) (pu)
```

xxiv List of Abbreviations

 $\Psi$  flux (linkage) magnitude (pu)  $\tau$  time constant (s or pu)

 $\omega$  rotational speed or angular frequency (rad/s or pu)

 $\xi, \xi, \zeta, \zeta$  slack or auxiliary variable

### Subscripts

 $c_{
m on}, c_{
m off}, c_{
m rr}$  turn–on, turn–off and reverse recovery energy loss coefficients (J/(VA))

 $\begin{array}{lll} C_m & \text{module capacitance (F)} \\ f_c & \text{carrier frequency} \\ f_{\mathrm{DL}} & \text{frequency of deadlocks} \\ f_{\mathrm{sw}} & \text{switching frequency} \\ i_1 & \text{fundamental current} \\ i_a, i_b, i_c & \text{phase } a, b, \text{ and } c \text{ currents} \end{array}$ 

 $i_{\alpha}, i_{\beta}$  real and imaginary parts of the current (in the stationary reference frame)

 $i_B$  base current

 $egin{array}{ll} i_c & ext{converter current vector} \ i_{
m circ} & ext{circulating current vector} \end{array}$ 

 $i_d$ ,  $i_q$  real and imaginary parts of the current (in the rotating reference frame)

 $egin{array}{lll} egin{array}{lll} egin{arra$ 

 $egin{array}{ll} i_{
m rip} & {
m ripple \ current \ vector} \ i_s & {
m stator \ current \ vector} \ i_T & {
m anode \ current} \end{array}$ 

 $I_{\mathrm{TDD}}$  total demand distortion (TDD) of the current

 $L_{hr}$  branch inductor

 $L_{ls}$  stator leakage inductance rotor leakage inductance

 $L_m$  main (or magnetizing) inductance

 $L_{\sigma}$  total leakage inductance

 $N_p$  prediction horizon (number of time steps)  $N_s$  switching horizon (number of switching events)

 $T_e$  electromechanical torque

 $T_{e, {
m min}}$  lower bound on the electromagnetic torque upper bound on the electromagnetic torque

 $T_{\ell}$  load torque

 $T_p$  prediction horizon (length in time)  $\theta_p$  prediction horizon (angular interval)

 $T_s$  sampling interval

 $u_{\text{opt}}$  optimal control input (or manipulated variable)

 $v_{
m dc}$  instantaneous dc-link voltage  $V_{
m dc}$  nominal dc-link voltage

 $v_{\rm dc,lo}, v_{\rm dc,up}$  instantaneous voltage of the lower and upper dc-link half, respectively

 $v_n$  neutral point potential

List of Abbreviations XXV

$v_{\mathrm{ph}}$	phase voltage
$\omega_1$	fundamental frequency
$\omega_{\mathrm{fr}}$	angular speed of the reference frame
$\omega_g$	electrical grid frequency
$\omega_m$	mechanical shaft speed
$\omega_r$	electrical angular speed of the rotor
$\omega_*$	stator frequency
$\omega_m$ $\omega_r$ $\omega_s$ $\omega_{\rm sl}$	slip frequency

### Superscripts

$i^*$	current reference
$\vec{i}$	current space vector
$\hat{i}_n$	amplitude of harmonic current of order $n$
i'	scaled version of $i$ , e.g., when turned into the per unit system
71.	switch position multiplied with the generator matrix $V$

$\bar{u}$ s	witch position multiplied with the generator matrix $V$
Operations	
$\mathrm{d}x/\mathrm{d}t$	time derivative of the variable $x$
$\exp(x)$ , $e^x$	exponential of the variable $x$
$\Re\{x\}$	real part of the complex variable $x$
$\Im\{x\}$	imaginary part of the complex variable $x$
$conj\{x\}$	complex conjugate of the complex variable $x$
$x \times y$	cross product of the vectors x and y
$x \in \mathcal{S}$	variable $x$ belongs to the set $S$
$x^T$	transpose of the vector $x$
$X^{-1}$	inverse of the matrix $X$
x	absolute value of the scalar $x$
$\ x\ _1$	1-norm of the vector $\mathbf{x}$ (sum of the absolute values)
$\ oldsymbol{x}\ _2$	2-norm or length of the vector $\mathbf{x}$ (square root of the sum of the squared values,
	Euclidian norm). To simplify the notation, we will often simply write $  x  $
$\ x\ _{\infty}$	infinity-norm of the vector <b>x</b> (largest absolute value)

# About the Companion Website

Don't forget to visit the companion website for this book:

www.wiley.com/go/geyermodelpredictivecontrol



There you will find valuable material designed to enhance your learning, including animations of the control concepts.

Scan this QR code to visit the companion website



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