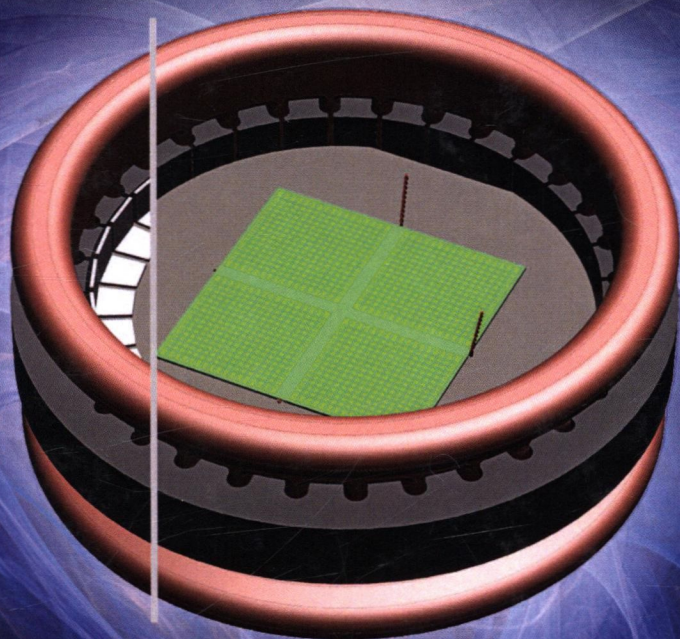


# Characterisation of Soft Magnetic Materials Under Rotational Magnetisation



Stanislaw Zurek



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The book presents practical aspects related to the measurement of rotational power loss in soft magnetic materials. The book furthermore focuses on practical aspects of performing such measurements, the associated difficulties as well as solutions to the most common problems. Numerous practical aspects, hands-on experience, and most commonly encountered pitfalls are heavily discussed in the book. The text begins with introduction to magnetism, then follows with definitions of measurement methods of rotational power loss from physical viewpoint. Two chapters describe and detail the various sensors which can be employed for such measurements as well as all the aspects of designing, making, and using a magnetising apparatus. A synthesis of the likely optimal design of a magnetising apparatus is also given, preceded with the full reasoning based on all the research carried out to date. **Characterisation of Soft Magnetic Materials Under Rotational Magnetisation** serves as an excellent starting point for any student having to perform magnetic measurements under rotational magnetisation, but also under 1D, 2D or 3D excitation. Because the methods, sensors, and apparatus are extensively discussed it will also be a great reference for more senior researchers and experts in the field. There is a whole chapter devoted to analysis of measurement uncertainty. This subject is rarely published for magnetic measurements, which makes it more difficult for all researchers to understand the concepts and methodology used in uncertainty estimation. This chapter not only introduces the whole subject, but also provides multiple step-by-step examples which can be easily followed, from very simple cases to much more complex ones. All equations are presented with full SI units which greatly helps in practical application of the presented methodology. Each chapter is written in such a way that it can be studied on its own, so that the reader can focus only on the specific aspects, as required.

**The most comprehensive book on rotational magnetisation power loss measurements.**

- Text compiled at a level accessible to self-learning students, but also containing all information required for reference for experts in the field
- Unique practical comments and know-how throughout the book, from drilling holes, through digital feedback implementation, to precision of calculations
- All equations are presented in an easy-to-use form, with the corresponding physical units as well as with numerous practical comments
- A whole chapter devoted to uncertainty analysis, with easy-to-follow explanation of the basic terms and step-by-step practical examples
- Complete definition of numerical integration for signals and power loss

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**ZUREK**

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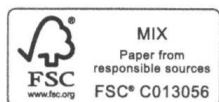
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# **Characterisation of Soft Magnetic Materials Under Rotational Magnetisation**



*This book is dedicated to the most resourceful, the wisest,  
the most hard-working and the bravest person I ever  
knew – my mother Janina Żurek who used to say:*

We learn our whole life, and we still die stupid.





# Symbols, Acronyms and Abbreviations

$\odot$	a circle with a dot represents a vector, whose direction is perpendicular to the surface of the page and the sense is pointing towards the reader
$\otimes$	a circle with a cross represents a vector, whose direction is perpendicular to the surface of the page and the sense is pointing away from the reader
1&2DM	International Workshop on 1&2 Dimensional Magnetic Measurement and Testing
1D	one-dimensional, uni-directional
2D	two-dimensional (including rotational)
2DM	International Workshop on 1&2 Dimensional Magnetic Measurement and Testing
3d	electron shell important for ferromagnetism
3D	three-dimensional
$a$	interatomic distance (m)
$a_{rec}$	range of interval in a rectangular distribution (various units)
$a_{tri}$	range of interval in a triangular distribution (various units)
a.u.	arbitrary units
A	location 'A', or ammeter
$A$	area (m <sup>2</sup> )
$A_1, A_2$	area (m <sup>2</sup> )
$A_C$	area of a conductive pad (m <sup>2</sup> )
$A_{coil}$	active area of a coil (m <sup>2</sup> )
$A_i$	numerical value of 'partial area' of $i$ -th trapezoid in mathematical integration of digital signal ( $V \cdot s$ )
AI+	positive analogue input
AI-	negative analogue input
AI GND	analogue input ground
AI SENSE	analogue input sense, reference for non-referenced single-ended mode input
AISN	<i>see</i> AI SENSE
$A_{sample}$	cross-section area of a sample (m <sup>2</sup> )
$A_{yoke}$	cross-section area of a yoke (m <sup>2</sup> )
ADC	analogue-to-digital converter
AVG	average of rectified voltage signal (V)
B	location 'B'
$B$	flux density (T)
$\bar{B}$	amplitude of purely circular $B$ (T)
$\vec{B}$	flux density vector

$B_1$	flux density in medium '1'
$B_{1n}$	normal component of $B_1$
$B_{1t}$	tangential component of $B_1$
$B_2$	flux density in medium '2'
$B_{2n}$	normal component of $B_2$
$B_{2t}$	tangential component of $B_2$
$B_A$	(amplitude of) alternating flux density (T)
$B_C$	(modulus of vector of) circular flux density (T)
$B_{mean}$	flux density averaged over an area (T)
BN	Barkhausen noise
$B_p$	peak flux density (T)
$B_{peak}$	peak flux density (T)
$B_r$	remanence (T)
$B_R$	rotational flux density (T)
$B_{sample}$	flux density in a sample (T)
$B_{yoke}$	flux density in a yoke (T)
$B_x$	x component of $B$ (T)
$B_y$	y component of $B$ (T)
$B_z$	z component of $B$ (T)
$c$	specific heat (J/(kg · K))
$C$	capacitance (F)
$C_0$	constant value in a given equation (various units)
$C_1$	constant value in a given equation (various units)
$C_2$	constant value in a given equation (various units)
$C_a$	material constant in additional component of power loss ( $J \cdot \sqrt{s/kg}$ )
$C_e$	material constant in eddy current component of power loss ( $J \cdot s/kg$ )
$C_h$	material constant in hysteresis component of power loss (J/kg)
$C_{integral}$	constant value resulting from integration of any function (various units)
$C_n$	constant value in a given equation (various units)
CNC	computer numerical control
$C_x$	constant value in a given equation (various units)
CGO	conventional grain-oriented electrical steel
$d$	thickness (m)
$d_f$	degrees of freedom (unitless)
$^e d_f$	effective degrees of freedom (unitless)
$d_r$	digit of resolution (various units)
$D$	specific density ( $kg/m^3$ )
DAC	digital-to-analogue converter
DAQ	data acquisition device
DGO	double grain-oriented electrical steel
DMM	digital multimeter
$E$	energy in (J), (J/kg) or ( $J/m^3$ )
$E_{circle}$	energy in circular motion (J)
$E_{line}$	energy in linear motion (J)
$E$	electric field (V/m)

$\vec{E}$	electric field vector
EDM	electrical discharge machining
<i>EMF</i>	electromotive force (V)
ENOB	effective number of bits
$E_x$	x component of electric field (V/m)
$E_y$	y component of electric field (V/m)
$E_y$	Young's modulus of elasticity (Pa)
$E_z$	z component of electric field (V/m)
<i>f</i>	frequency (Hz)
<i>F</i>	mechanical force (N)
FEM	finite-element method
<i>FF</i>	form factor (unitless)
<i>FFF</i>	flux fringing factor (unitless)
FSO	full-scale output
<i>g</i>	gravity (m/s <sup>2</sup> )
$g_a$	acceleration (m/s <sup>2</sup> )
<i>G</i>	gain (unitless)
$G_{corr}$	correction gain (unitless)
$G_{DF}$	digital feedback gain (unitless)
$G_{sys}$	system gain (unitless)
<i>GF</i>	gauge factor (unitless)
<i>h</i>	generic function (various units)
$h_0, h_1, h_2, h_i, h_n$	amplitudes of harmonics (various units)
<i>H</i>	magnetic field strength (A/m)
$\vec{H}$	magnetic field vector
$H_1$	magnetic field strength in medium '1'
$H_{1n}$	normal component of $H_1$
$H_{1t}$	tangential component of $H_1$
$H_2$	magnetic field strength in medium '2'
$H_{2n}$	normal component of $H_2$
$H_{2t}$	tangential component of $H_2$
$H_a$	applied magnetic field (A/m)
$H_c$	coercivity (A/m)
${}_B H_c$	coercivity value derived from a $B-H$ loop (A/m)
${}_J H_c$	coercivity value derived from a $J-H$ loop (A/m)
$H_d$	demagnetising magnetic field (A/m)
$H_{mean}$	magnetic field strength averaged over an area (A/m)
HGO	high-permeability grain-oriented electrical steel
$H_p$	peak magnetic field strength (A/m)
$H_x$	x component of $H$ (A/m)
$H_y$	y component of $H$ (A/m)
$H_z$	z component of $H$ (A/m)
<i>i</i>	subsequent item in a set, series or array
<i>I</i>	electric current (A)
$I_1$	primary current (A)

$I_2$	secondary current (A)
$I_e$	eddy current (A)
$I_p$	peak current (A)
$I_x$	current for the $x$ channel (A)
$I_y$	current for the $y$ channel (A)
IM	intermodulation
IMD	intermodulation
$j$	subsequent item in a set, series or array
$J$	magnetic polarisation (T)
$J_1$	parallel polarisation (T)
$J_{\perp}$	perpendicular polarisation (T)
$J_p$	peak polarisation (T)
$J_{sat}$	saturation polarisation (T)
$k$	coefficient of mechanical friction (unitless)
$k_Q$	coverage factor (unitless)
$k_{Q,t}$	Student's distribution correction factor (unitless)
$K$	Poynting–Umov vector (W)
$K_0$	magnetocrystalline anisotropy constant ( $J/m^3$ )
$K_1$	magnetocrystalline anisotropy constant ( $J/m^3$ )
$K_2$	magnetocrystalline anisotropy constant ( $J/m^3$ )
$K_t$	heat transfer coefficient ( $W/(kg \cdot K)$ )
$l$	length or distance (m)
$l_1$	length or distance (m)
$l_2$	length or distance (m)
$l_{coil}$	length or path of the coil (m)
$l_{gap}$	length of air gap (m)
$l_{lag}$	lagging distance in circular motion (m)
$l_{surface}$	length or path on the surface of the sample (m)
$l_{yoke}$	length of yoke (m)
$L$	inductance (H)
$m$	mass (kg)
$M$	magnetisation (A/m)
MAE	magneto-acoustic emissions
MMF	magnetomotive force (A)
MOKE	magneto-optic Kerr effect
$M_S$	magnetisation saturation (A/m)
$n$	number of items, e.g. turns or points (unitless)
$N$	number of items, e.g. turns or points (unitless)
$N_1$	primary turns (unitless)
$N_2$	secondary turns (unitless)
$N_{BN}$	number of elements (values) in the digitised Barkhausen noise
$N_d$	demagnetising coefficient (unitless)
NO	non-oriented electrical steel
$nom$	nominal value (various units)
NTC	negative temperature coefficient
opamp	operational amplifier

$p$	instantaneous power loss (W)
$P$	power in (W), (W/kg) or (W/m <sup>3</sup> )
$P_a$	additional component of power loss, in (W), (W/kg) or (W/m <sup>3</sup> )
$P_{circle}$	power in circular motion (W)
$P_e$	eddy current component of power loss, in (W), (W/kg) or (W/m <sup>3</sup> )
$P_h$	hysteresis component of power loss, in (W), (W/kg) or (W/m <sup>3</sup> )
$P_h$	hysteresis component of power loss, in (W), (W/kg) or (W/m <sup>3</sup> )
$PA$	partial area (various units)
PID	proportional–integral–derivative (controller)
$P_{rot}$	rotational power loss, in (W), (W/kg) or (W/m <sup>3</sup> )
$P_x$	component in calculation of rotational power loss, in (W), (W/kg) or (W/m <sup>3</sup> )
$P_y$	component in calculation of rotational power loss, in (W), (W/kg) or (W/m <sup>3</sup> )
PLC	power line cycles (unitless)
PS	power spectrum of Barkhausen noise signal
PTC	positive temperature coefficient
$Q$	probability (unitless)
$Q_t$	probability in Student's $t$ -distribution (unitless)
$r$	radius (m)
$R$	resistance ( $\Omega$ )
$R_0$	additional resistance ( $\Omega$ )
$R_1, R_2$	resistance values ( $\Omega$ )
$R_{in}$	input resistance ( $\Omega$ )
$R_m$	measured resistance ( $\Omega$ )
$R_{ref}$	reference resistance ( $\Omega$ )
$R_s$	resistance of a shunt resistor ( $\Omega$ )
RS– and RS+	remote sensing connections for a half-bridge circuit
RCP	Rogowski–Chattock potentiometer
RMS	root mean square
$s$	system gain, equivalent to $G_{sys}$ (unitless)
$S$	sensitivity or sensitivity coefficient (various units)
$S_{control}$	controlled signal (various units)
$S_{corr}$	correction signal (various units)
$S_{diff}$	difference signal (various units)
$S_{gen}$	generated signal (various units)
$S_H$	signal from sensor of $H$ (various units)
$S_{target}$	target signal (various units)
SC– and SC+	shunt calibration connections for a half-bridge circuit
SI	International System of units ( <i>Le Système International d'unités</i> )
$t$	time (s)
$t_D$	delay time (s)
$t_L$	triggering correction time (s)
$t_{on}$	time instant of a start of a process (s)
$t_{off}$	time instant of an end of a process (s)
$t_s$	sampling time interval (s)

$T$	length of cycle or period (s)
$T_0$	starting temperature (K)
THD	total harmonic distortion (%)
$T_m$	measured temperature (K)
$T_{ref}$	reference temperature (K)
TNP	total number of peaks of Barkhausen noise signal (unitless)
TSA	total sum of amplitudes of Barkhausen noise signal (V)
TX	transformer
$u$	uncertainty (various units)
$u_c$	combined uncertainty (various units)
$e u_c$	expanded combined uncertainty (various units)
$u_s$	standard uncertainty (various units)
$u_{s,S}$	scaled standard uncertainty (various units)
$v$	variable (various units)
$\bar{v}$	average of a variable $v$ (various units)
$v_{-1}, v_0, v_1, \text{ etc.}$	subsequent values (various units)
$v_i$	$i$ th value (various units)
$v'_{-1}, v'_0, v'_1, \text{ etc.}$	subsequent approximated values (various units)
$v_E$	expected value (V)
$v_L$	triggering level (V)
$v_n$	$n$ th value (various units)
$v_{nom}$	nominal value (various units)
$v_R$	real or actual value (V)
$v(t)$	approximating function (V)
$V$	voltage (V)
V	voltmeter
$V_0$	voltage (V)
$V_1$	voltage (V)
$V_2$	voltage (V)
$V_3$	voltage (V)
$V_a$	voltage at a point 'a' (V)
$V_A$	voltage in part 'A' (V)
$V_{avg}$	average voltage (V)
$V_{AVG}$	average voltage (V)
$V_b$	voltage at a point 'b' (V)
$V_B$	voltage in part 'B' (V)
$V_{B-coil}$	$B$ -coil voltage (V)
$V_{BN}$	output voltage of a Barkhausen noise sensor (V)
$V_H$	output voltage of a Hall-effect sensor (V)
$V_i$	$i$ th numerical voltage value (V)
$V_{in}$	input voltage (V)
$V_{indirect}$	voltage induced in an indirect coil (V)
$V_m$	measurand (various units)
$V_M$	magnetic potential (A/m)
$V_{M(A,B)}$	magnetic potential difference between points 'A' and 'B' (A/m)
$V_{max}$	maximum voltage (V)

$ V _{mean}$	mean value of rectified voltage (V)
$V_{min}$	minimum voltage (V)
$V_{NP}$	needle probe sensor voltage (V)
$V_{out}$	output voltage (V)
$V_{pk-pk}$	voltage peak-to-peak (V)
$V_r$	voltage across a shunt resistor (V)
$V_{ref}$	reference voltage (V)
$V_{res}$	voltage resolution (V)
$V_{RMS}$	RMS value of voltage (V)
$V_s$	sample volume (m <sup>3</sup> )
$V_{shunt}$	voltage across shunt resistor (V)
$V_{supply}$	supply voltage (V)
$V_{th}$	thermal noise voltage (V)
$V_x$	voltage for the $x$ channel (V)
$V_y$	voltage for the $y$ channel (V)
W	wattmeter
$W_R$	rotational loss (W)
WCM	Wolfson Centre for Magnetics, Cardiff University, Cardiff, UK
$x$	direction in orthogonal system of coordinates
$x'$	apparent direction, deviated from $x$
$y$	direction in orthogonal system of coordinates
$y'$	apparent direction, deviated from $y$
$z$	direction in orthogonal system of coordinates
$\vec{x}$	unit vector in direction $x$
$\vec{y}$	unit vector in direction $y$
$\vec{z}$	unit vector in direction $z$

## GREEK CHARACTERS

$\alpha$	arbitrary direction of magnetostriction (rad)
$\alpha_{iron}$	ferromagnetic form of iron
$\alpha_k$	angle of rotation of polarised light beam in the longitudinal Kerr effect (rad)
$\gamma$	electric conductivity (S/m)
$\gamma_{iron}$	non-ferromagnetic form of iron
$\Gamma$	function described by Equation 5.9
$\Delta$	change or difference of any parameter
$\Delta l$	change of length (m)
$\Delta t$	change of time (s)
$\delta$	error of angular positioning (rad)
$\theta$	angle of rotation (rad)
$\theta_x$	angle of rotation of apparent axis $x'$ (rad)
$\theta_y$	angle of rotation of apparent axis $y'$ (rad)
$\vartheta$	angle of incident beam in Kerr microscopy (rad)
$\lambda$	magnetostriction (m/m or unitless)
$\lambda_{pk-pk}$	peak-to-peak magnetostriction (m/m or unitless)



$\mu$	magnetic permeability, $\mu = \mu_r \cdot \mu_0$ (H/m)
$\mu_0$	magnetic constant, magnetic permeability of free space $\mu_0 = 4 \cdot \pi \cdot 10^{-7}$ (H/m)
$\mu_1$	magnetic permeability of medium '1'
$\mu_2$	magnetic permeability of medium '2'
$\mu_r$	relative magnetic permeability $\mu_r = \mu/\mu_0$ (unitless)
$\rho$	correlation coefficient (unitless)
$\zeta$	tangential stress (Pa)
$\sigma$	stress (Pa)
$\sigma_s$	standard deviation (various units)
$v\sigma_s^2$	variance (various units)
$\sigma_{s,rec}$	standard deviation in rectangular distribution (various units)
$\sigma_{s,tri}$	standard deviation in triangular distribution (various units)
$\sigma_{sdom}$	standard deviation of the mean (various units)
$\tau$	torque (N · m)
$\phi$	phase angle or angular lag (rad)
$\omega$	angular frequency (rad/s)
$\Phi$	magnetic flux (Wb)
$\Phi_{coil}$	magnetic flux in a coil (Wb)
$\Phi_{sample}$	magnetic flux in a sample (Wb)
$\Phi_{yoke}$	magnetic flux in a yoke (Wb)
$\chi$	magnetic susceptibility, $\chi = \mu_r - 1$ (unitless)