

Engineering Mechanics

# DYNAMICS

Fourteenth Edition

R. C. Hibbeler



ENGINEERING MECHANICS

# DYNAMICS

FOURTEENTH EDITION.

R. C. HIBBELER

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## To the Student

With the hope that this work will stimulate  
an interest in Engineering Mechanics  
and provide an acceptable guide to its understanding.

# PREFACE

The main purpose of this book is to provide the student with a clear and thorough presentation of the theory and application of engineering mechanics. To achieve this objective, this work has been shaped by the comments and suggestions of hundreds of reviewers in the teaching profession, as well as many of the author's students.

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## New to this Edition

**Preliminary Problems.** This new feature can be found throughout the text, and is given just before the Fundamental Problems. The intent here is to test the student's conceptual understanding of the theory. Normally the solutions require little or no calculation, and as such, these problems provide a basic understanding of the concepts before they are applied numerically. All the solutions are given in the back of the text.

**Expanded Important Points Sections.** Summaries have been added which reinforces the reading material and highlights the important definitions and concepts of the sections.

**Re-writing of Text Material.** Further clarification of concepts has been included in this edition, and important definitions are now in boldface throughout the text to highlight their importance.

**End-of-the-Chapter Review Problems.** All the review problems now have solutions given in the back, so that students can check their work when studying for exams, and reviewing their skills when the chapter is finished.

**New Photos.** The relevance of knowing the subject matter is reflected by the real-world applications depicted in the over 30 new or updated photos placed throughout the book. These photos generally are used to explain how the relevant principles apply to real-world situations and how materials behave under load.

**New Problems.** There are approximately 30% new problems that have been added to this edition, which involve applications to many different fields of engineering.

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## Hallmark Features

Besides the new features mentioned above, other outstanding features that define the contents of the text include the following.

**Organization and Approach.** Each chapter is organized into well-defined sections that contain an explanation of specific topics, illustrative example problems, and a set of homework problems. The topics within each section are placed into subgroups defined by boldface titles. The purpose of this is to present a structured method for introducing each new definition or concept and to make the book convenient for later reference and review.

**Chapter Contents.** Each chapter begins with an illustration demonstrating a broad-range application of the material within the chapter. A bulleted list of the chapter contents is provided to give a general overview of the material that will be covered.

**Emphasis on Free-Body Diagrams.** Drawing a free-body diagram is particularly important when solving problems, and for this reason this step is strongly emphasized throughout the book. In particular, special sections and examples are devoted to show how to draw free-body diagrams. Specific homework problems have also been added to develop this practice.

**Procedures for Analysis.** A general procedure for analyzing any mechanical problem is presented at the end of the first chapter. Then this procedure is customized to relate to specific types of problems that are covered throughout the book. This unique feature provides the student with a logical and orderly method to follow when applying the theory. The example problems are solved using this outlined method in order to clarify its numerical application. Realize, however, that once the relevant principles have been mastered and enough confidence and judgment have been obtained, the student can then develop his or her own procedures for solving problems.

**Important Points.** This feature provides a review or summary of the most important concepts in a section and highlights the most significant points that should be realized when applying the theory to solve problems.

**Fundamental Problems.** These problem sets are selectively located just after most of the example problems. They provide students with simple applications of the concepts, and therefore, the chance to develop their problem-solving skills before attempting to solve any of the standard problems that follow. In addition, they can be used for preparing for exams, and they can be used at a later time when preparing for the Fundamentals in Engineering Exam.

**Conceptual Understanding.** Through the use of photographs placed throughout the book, theory is applied in a simplified way in order to illustrate some of its more important conceptual features and instill the physical meaning of many of the terms



used in the equations. These simplified applications increase interest in the subject matter and better prepare the student to understand the examples and solve problems.

**Homework Problems.** Apart from the Fundamental and Conceptual type problems mentioned previously, other types of problems contained in the book include the following:

- **Free-Body Diagram Problems.** Some sections of the book contain introductory problems that only require drawing the free-body diagram for the specific problems within a problem set. These assignments will impress upon the student the importance of mastering this skill as a requirement for a complete solution of any equilibrium problem.
- **General Analysis and Design Problems.** The majority of problems in the book depict realistic situations encountered in engineering practice. Some of these problems come from actual products used in industry. It is hoped that this realism will both stimulate the student's interest in engineering mechanics and provide a means for developing the skill to reduce any such problem from its physical description to a model or symbolic representation to which the principles of mechanics may be applied.

Throughout the book, there is an approximate balance of problems using either SI or FPS units. Furthermore, in any set, an attempt has been made to arrange the problems in order of increasing difficulty except for the end of chapter review problems, which are presented in random order.

- **Computer Problems.** An effort has been made to include some problems that may be solved using a numerical procedure executed on either a desktop computer or a programmable pocket calculator. The intent here is to broaden the student's capacity for using other forms of mathematical analysis without sacrificing the time needed to focus on the application of the principles of mechanics. Problems of this type, which either can or must be solved using numerical procedures, are identified by a "square" symbol (■) preceding the problem number.

The many homework problems in this edition, have been placed into two different categories. Problems that are simply indicated by a problem number have an answer and in some cases an additional numerical result given in the back of the book. An asterisk (\*) before every fourth problem number indicates a problem without an answer.

**Accuracy.** As with the previous editions, apart from the author, the accuracy of the text and problem solutions has been thoroughly checked by four other parties: Scott Hendricks, Virginia Polytechnic Institute and State University; Karim Nohra, University of South Florida; Kurt Norlin, Bittner Development Group; and finally Kai Beng, a practicing engineer, who in addition to accuracy review provided suggestions for problem development.

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## Contents

The book is divided into 11 chapters, in which the principles are first applied to simple, then to more complicated situations.

The kinematics of a particle is discussed in Chapter 12, followed by a discussion of particle kinetics in Chapter 13 (Equation of Motion), Chapter 14 (Work and Energy), and Chapter 15 (Impulse and Momentum). The concepts of particle dynamics contained in these four chapters are then summarized in a “review” section, and the student is given the chance to identify and solve a variety of problems. A similar sequence of presentation is given for the planar motion of a rigid body: Chapter 16 (Planar Kinematics), Chapter 17 (Equations of Motion), Chapter 18 (Work and Energy), and Chapter 19 (Impulse and Momentum), followed by a summary and review set of problems for these chapters.

If time permits, some of the material involving three-dimensional rigid-body motion may be included in the course. The kinematics and kinetics of this motion are discussed in Chapters 20 and 21, respectively. Chapter 22 (Vibrations) may be included if the student has the necessary mathematical background. Sections of the book that are considered to be beyond the scope of the basic dynamics course are indicated by a star (★) and may be omitted. Note that this material also provides a suitable reference for basic principles when it is discussed in more advanced courses. Finally, Appendix A provides a list of mathematical formulas needed to solve the problems in the book, Appendix B provides a brief review of vector analysis, and Appendix C reviews application of the chain rule.

**Alternative Coverage.** At the discretion of the instructor, it is possible to cover Chapters 12 through 19 in the following order with no loss in continuity: Chapters 12 and 16 (Kinematics), Chapters 13 and 17 (Equations of Motion), Chapter 14 and 18 (Work and Energy), and Chapters 15 and 19 (Impulse and Momentum).

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## Acknowledgments

The author has endeavored to write this book so that it will appeal to both the student and instructor. Through the years, many people have helped in its development, and I will always be grateful for their valued suggestions and comments. Specifically, I wish to thank all the individuals who have contributed their comments relative to preparing the fourteenth edition of this work, and in particular, R. Bankhead of Highline Community College, K. Cook-Chennault of Rutgers, the State University of New Jersey, E. Erisman, College of Lake County Illinois, M. Freeman of the University of Alabama, H. Lu of University of Texas at Dallas, J. Morgan of Texas A & M University, R. Neptune of the University of Texas, I. Orabi of the University of New Haven, T. Tan, University of Memphis, R. Viesca of Tufts University, and G. Young, Oklahoma State University.

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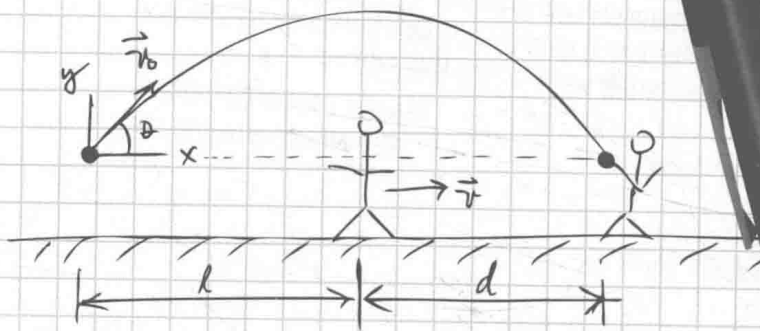
Lastly, many thanks are extended to all my students and to members of the teaching profession who have freely taken the time to e-mail me their suggestions and comments. Since this list is too long to mention, it is hoped that those who have given help in this manner will accept this anonymous recognition.

I would greatly appreciate hearing from you if at any time you have any comments, suggestions, or problems related to any matters regarding this edition.

*Russell Charles Hibbeler*  
*hibbeler@bellsouth.net*

# your work...

## PART A



given :  $v = 7.000 \text{ m/s}$  ;  $t = 2.000 \text{ s}$  ;  $l = 18.00 \text{ m}$

$$d = v \cdot t \Rightarrow d = (7.000 \text{ m/s})(2.000 \text{ s}) = 14.00 \text{ m}$$

$$x = l + d \Rightarrow x = 18.00 \text{ m} + 14.00 \text{ m} = 32.00 \text{ m}$$

$$g = 9.807 \text{ m/s}^2$$

$$v_{0x} = \frac{x}{t} = \frac{32.00 \text{ m}}{2.000 \text{ s}} = 16.00 \text{ m/s (COMP. X)}$$

$$v_{0y} = \frac{1}{2} g t = \frac{1}{2} (9.807 \text{ m/s}^2)(2.000 \text{ s}) = 9.80 \text{ m/s (COMP. Y)}$$

$$v_0 = v_{0x} + v_{0y} = 16.00 \text{ m/s} + 9.80 \text{ m/s} = 25.80 \text{ m/s (TOTAL)}$$

$$\boxed{v_0 = 25.80 \text{ m/s}}$$

# your answer specific feedback

Express the initial speed to four significant figures in meters per second.

$\sqrt{\phantom{x}}$

$\Delta \Sigma \Phi$

$\updownarrow$

vec

$\leftarrow$

$\rightarrow$

$\circlearrowright$

$\text{m/s}$

?

$v_0 =$    $\text{m/s}$

Submit

[Hints](#)

[My Answers](#)

[Give Up](#)

[Review Part](#)

**Incorrect; Try Again; 5 attempts remaining**

This is the sum of the components of the velocity. You need to use the Pythagorean theorem to find the total velocity.

You may need to review [Vector Magnitudes](#).

[www.MasteringEngineering.com](http://www.MasteringEngineering.com)

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## Resources for Instructors

- **MasteringEngineering.** This online Tutorial Homework program allows you to integrate dynamic homework with automatic grading and adaptive tutoring. MasteringEngineering allows you to easily track the performance of your entire class on an assignment-by-assignment basis, or the detailed work of an individual student.
- **Instructor's Solutions Manual.** This supplement provides complete solutions supported by problem statements and problem figures. The fourteenth edition manual was revised to improve readability and was triple accuracy checked. The Instructor's Solutions Manual is available on Pearson Higher Education website: [www.pearsonhighered.com](http://www.pearsonhighered.com).
- **Instructor's Resource.** Visual resources to accompany the text are located on the Pearson Higher Education website: [www.pearsonhighered.com](http://www.pearsonhighered.com). If you are in need of a login and password for this site, please contact your local Pearson representative. Visual resources include all art from the text, available in PowerPoint slide and JPEG format.
- **Video Solutions.** Developed by Professor Edward Berger, Purdue University, video solutions are located in the study area of MasteringEngineering and offer step-by-step solution walkthroughs of representative homework problems from each section of the text. Make efficient use of class time and office hours by showing students the complete and concise problem-solving approaches that they can access any time and view at their own pace. The videos are designed to be a flexible resource to be used however each instructor and student prefers. A valuable tutorial resource, the videos are also helpful for student self-evaluation as students can pause the videos to check their understanding and work alongside the video. Access the videos at [www.masteringengineering.com](http://www.masteringengineering.com)

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## Resources for Students

- **MasteringEngineering.** Tutorial homework problems emulate the instructor's office-hour environment, guiding students through engineering concepts with self-paced individualized coaching. These in-depth tutorial homework problems are designed to coach students with feedback specific to their errors and optional hints that break problems down into simpler steps.
- **Dynamics Study Pack.** This supplement contains chapter-by-chapter study materials and a Free-Body Diagram Workbook.
- **Video Solutions** Complete, step-by-step solution walkthroughs of representative homework problems from each section. Videos offer fully worked solutions that show every step of representative homework problems—this helps students make vital connections between concepts.
- **Dynamics Practice Problems Workbook.** This workbook contains additional worked problems. The problems are partially solved and are designed to help guide students through difficult topics.

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## Ordering Options

The *Dynamics Study Pack* and MasteringEngineering resources are available as stand-alone items for student purchase and are also available packaged with the texts. The ISBN for each valuepack is as follows:

- *Engineering Mechanics: Dynamics* with Study Pack: ISBN: 0134116658
- *Engineering Mechanics: Dynamics Plus MasteringEngineering* with Pearson eText — Access Card Package: ISBN: 0134116992

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