Nozomu Yoshida

# Seismic Ground Response Analysis



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## **Preface**

Earthquake resistant design is an important consideration for designing structures in seismic prone areas including Japan. Recently, following the developments in seismology and earthquake engineering, design earthquake motion is defined at the engineering seismic base layer (engineering bedrock) or the seismic bedrock regardless of the structural type and the ground type. Therefore, in order to get the design earthquake motion at the ground surface or at the foundation of a structure, engineers need to make a seismic ground response analysis.

I graduated from the Department of Architecture and Architectural Engineering, Kyoto University (Japan), and my thesis for doctor of engineering was cyclic behavior of steel braces subjected to earthquake loading. Several years after my post-doctoral life in the university, I joined Sato Kogyo, a general contractor firm, and I engaged in the design of the RCWS (reactor cooling water system) of a nuclear power plant. There, I faced a problem on how to consider the liquefaction of the crushed rock that was used to fill the excavated area during construction just neighboring the grit chamber. I visited Prof. Ishihara, University of Tokyo, to get an idea. He introduced a computer program YUSAYUSA and I engaged to improve it with him, which is now open for public from my website (Yoshida and Towhata 1991), and it was my first technical paper in this field. Soon after, Prof. Ishihara introduced me to Prof. Finn, University of British Columbia, Canada, and I got a chance to stay with him for 1 year. I engaged to develop the computer code TARA-3 (Finn et al. 1986). After coming back to Japan, I decided to change my research topic from structure to geotechnics, especially earthquake geotechnical engineering.

There were many differences between the structure and the soil as engineering materials and I was sometimes overwhelmed by these differences. Why, for example, stress-strain curve is expressed by, so-called, G- $\gamma$  and h- $\gamma$  relationships, and why just an approximated method is called an equivalent linear method, etc. Modeling the stress-strain behaviour was not a big issue in structural engineering, but it was a big issue in the new field. The error of the analysis was very large compared with the one in my former field. Things that are believed to be common

vi Preface

sense looked curious to me. So, it was a new world for me and I believed that I could contribute something in this field, which is the reason why I decided to move to the earthquake geotechnical engineering.

I started as an academician in the university several years ago quitting my second practical engineering job in Oyo Corporation, a consulting company. I was surprised that there is no time to teach the seismic ground response analysis in the syllabus. There are many topics that should be taught in the university, but time is limited. Seismic ground response analysis is a difficult issue because all other issues taught are necessary in order to understand the behavior during an earthquake.

On the other hand, seismic ground response analysis is an essential tool for the practical engineers. Then I had a question how they study this subject. Just that time, I was asked a lecture titled "seismic ground response analysis for practical use" from Prof. Wakamatsu, Kanto Gakuin University, who was a board member of the Japan Association for Earthquake Engineering (JAEE). Fortunately, the lecture was successful such that the JAEE turned away many people as the room became full. Then I understood that practical knowledge is desired from the practical engineer.

I published a book in Japanese in 2010 (Yoshida 2010) on the seismic ground response analysis based on this lecture. There are already many books on this subject. I feel, however, that there is no book that gives the knowledge or techniques required by the engineering practice or that the engineer can refer in their daily job. Many books deal with only the theoretical field, but there are many issues that cannot be discussed only by theory. So I especially focused on these topics. Soon after the publication of the Japanese book, Prof. Ansal and Dr. Tönük, Bogazici University, Turkey, suggested me to write an English version of this book. I omitted many theoretical descriptions in the Japanese version, but I think it would be better to add some theoretical parts for the foreign readers, which was also a suggestion by Dr. Tönük. So this is quite a new book.

This book deals with the total stress analysis, and the effective stress analysis or the liquefaction analysis is not considered partly because the effective stress analysis is more difficult compared with the total stress analysis and partly because another volume may be required to write the introductory part of the liquefaction analysis.

The author wishes sincere thanks to Prof. Wakamatsu who gave a chance to publish the Japanese book, and Prof. Ansal and Dr. Tönük who suggested the English version. Thanks are extended to Drs. Ohya, Port and Airport Research Institute, and Dr. Miura, Oyo cooperation, for their pre-reading of the Japanese version. Thanks are also extended to Dr. Tönük and Prof. Bhattacharya, University of Surry, UK, who checked my English.

## **Notes for Reading This Book**

This book follows SI unit system (Promotion committee of SI unit 1999). In other words, kN, m, and s are used for force, length, and time, respectively. Unit for pressure is expressed by kPa instead of kN/m<sup>2</sup>. In the field of seismology, Gal

Preface vii

(gal) has been used for acceleration, but it is not used in this book although it is possible as exceptional treatment. In the same manner, kine has been frequently used for velocity, but is not used in the book, either, because it is a non-SI unit. When converting the old unit system into the SI units, acceleration of gravity g is usually taken as  $9.8 \text{ m/s}^2$ , but  $10 \text{ m/s}^2$  can also be used. Error of 2% appears by this interpolation, but it is an acceptable error in many fields of engineering.

All the figures and equations are given using the SI unit. In the field of the geotechnical engineering, many empirical equations have been developed, and they are usually valid only in the specified unit. They are also rewritten in the SI unit system in this book.

Recently, information and data are published not only in the technical paper but also in the website. Here, unlike the technical paper, contents of the web are sometimes revised or erased, in which case the reader cannot find the data. In this book, the valid date of the existing website is shown in brackets [].

Abbreviations are used for several Japanese organizations which appear frequently in this book. They are as follows

AIJ: Architectural Institute of Japan

JAEE: Japan Association for Earthquake Engineering

JGS: Japanese Geotechnical Society
JSCE: Japan Society of Civil Engineering

JSSMFE: Japan Society of Soil Mechanics and Foundation Engineering, renamed

JGS in 1995

PARI: Port and Airport Research Institute PWRI: Public Work Research Institute

Sendai, Miyagi, Japan

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## **Contents**

1	Prop	agation of Earthquake Waves in the Ground		
	and I	Fundamentals of Earthquake Motion	1	
	1.1	Wave Propagation from Source to the Site	1	
		1.1.1 Path of Wave Propagation and Analysis Region	3	
		1.1.2 Path of Body Wave Propagation	5	
	1.2	Amplification of Earthquake Wave	6	
		1.2.1 First Mechanism: Change of Wave Velocity	6	
		1.2.2 Second Mechanism: Reflection at the Ground Surface	7	
		1.2.3 Third Mechanism: Reflections		
		from Underlying Layers	8	
		1.2.4 Fourth Mechanism: Resonance	9	
		1.2.5 Example of Earthquake Motion Amplification	11	
		1.2.6 Amplification of P-Wave	13	
	1.3	Attenuation of Earthquake Wave and Upper Bound		
		Earthquake Motion	15	
	Refe	rences	20	
2	Intro	oduction of Seismic Ground Response Analysis	23	
	2.1	Brief History of Seismic Ground Response Analysis		
	2.2	Procedure of Seismic Ground Response Analysis	25	
	References			
3	Input Earthquake Motions			
	3.1	Engineering Seismic Base Layer	31	
	3.2	Historical Earthquake Motions	36	
	3.3	Intensity of Design Ground Motion	38	
	3.4	Synthesized Earthquake Motions	40	
	3.5	Strong Ground Motion Databases	41	
	Refe	References		

Contents

4	Fund	lamental	s of Soil Mechanics	45
	4.1	Stress a	and Strain	45
		4.1.1	Positive Directions of Stress and Strain	45
		4.1.2	Effective Stress Principle	47
	4.2	Charact	teristics of Soil Behavior	48
		4.2.1	Volume Change	48
		4.2.2	Shear Deformation	49
		4.2.3	Other Parameters	49
		4.2.4	Dilatancy	50
		4.2.5	Constitutive Relations for Elastic Behavior	51
		4.2.6	Confining Stress Dependency	53
	4.3	Nonlin	ear Characteristics	54
		4.3.1	Nonlinear Characteristics Against Shear	56
		4.3.2	Nonlinear Characteristics Under Volumetric Change	56
	Refe	rences		58
=	T C:	C.:11 TI	3-4:	0
5	5.1		esting	61
	5.1		rd Penetration Test	61
		5.1.1	Energy Correction	62
	5.0	5.1.2	Effective Confining Stress Dependency	63
	5.2		gging	65
			Methods	67
	5.4		gical Age of Soil	68
	5.5 D-6-		uity of Soil Layers	69
	Refe	rences		71
6	Lab	oratory 7	Test and Assemble of Test Result	73
	6.1	Soil Sa	ampling	73
	6.2	Physic	al Tests	74
	6.3	Cyclic	Shear Deformation Characteristics Test	75
	6.4	Test A	pparatus	77
		6.4.1	Cyclic Triaxial Test	78
		6.4.2	Cyclic Direct Simple Shear Test	79
		6.4.3	Cyclic Torsional Shear Test	80
	6.5	Effect	of Sample Disturbance During Sampling and Traveling	81
	6.6		ilation of Test Results	85
		6.6.1	Hardin-Drnevich Model	85
		6.6.2	GHE Model	87
		6.6.3		90
		6.6.4	Double Hyperbolic Model	90
		6.6.5	Confining Stress Dependency	91
	6.7	Applic	cability and Limitations of Cyclic Shear Test	92
		6.7.1	Strain Range and Accuracy of Test	92
		6.7.2	Effect of Excess Porewater Pressure Generation	94
		6.7.3	Effect of Loading Speed	98
		6.7.4	Damping Characteristics	102

Contents xi

		6.7.5	Cyclic Shear Deformation Characteristics	105	
		152	and Shear Strength	105	
		6.7.6	Behavior at Large Strains	106	
		6.7.7	Effect of Number of Loading Cycles	109	
	D C	6.7.8	Initial Stress and Its Effect to Analysis	111	
	Refer	ences		114	
7			Mechanical Soil Properties	119	
	7.1		Properties	119	
		7.1.1	Equation by Imai et al.	120	
		7.1.2	Evaluation by Japan Road Bridge Design	101	
		7.1.3	Specifications  Equations Developed for Port Facilities	121 122	
		7.1.3			
			Equations Frequently Used in Buildings Design	123	
		7.1.5 7.1.6	Equations by Iwasaki et al.	124	
	7.0		Equations Based on Laboratory Tests	125	
	7.2		ear Properties	129	
		7.2.1 7.2.2	Equations by PWRI	130	
		1.2.2	Equations Involved in Technical Standards for Port and Harbor Facilities	135	
		7.2.3	Equations Involved in Standards for Railway	133	
		1.4.5	Structures	137	
		7.2.4	Equation in Building Standard Law	138	
		7.2.5	Equation by Central Research Institute	130	
		1.2.0	of Electric Research Industry	120	
		7.2.6	Study Compiled by Seed and Idriss	138 141	
		7.2.7	Equation by Yasuda et al.	141	
		7.2.8	Study by Vucetic and Dobry	144	
		7.2.9		144	
		7.2.10	Study by Oyamada et al.	144	
		7.2.10	Study by Imazu and Fukutake	143	
		7.2.11	Study by Wakamatsu et al.	151	
		7.2.12		151	
	7.3		Remaining Literatures		
	1.0	7.3.1		155	
		7.3.1	Shear Strength of Sand	158	
	7.4		Parameters		
			arameters	160	
				101	
8	Modeling of Mechanical Soil Properties				
	8.1		Modulus	167	
		8.1.1	Elastic Shear Modulus	167	
		8.1.2	Bulk Modulus and Poisson's Ratio		
	8.2		ear Model for One-Dimensional Analysis	173	
		8.2.1	Relation Between Cyclic Shear Deformation		
			Characteristics and Mathematical Models	173	

xii Contents

		8.2.2 Hysteresis Rules	175	
		8.2.3 Hyperbolic Model	179	
			182	
			187	
			190	
	8.3		190	
		rearrante de la company de la	190	
			194	
	8.4		198	
	8.5		200	
	Refere	ences	202	
9	Equa	tion of Motion	205	
	9.1		205	
	9.2		207	
	9.3		210	
	9.4		211	
	Refer		213	
10				
10	10.1		215	
	10.1		215 216	
	10.2		216	
			218	
	10.3		219	
	10.4		222	
	10.1		223	
			227	
	10.5		230	
			230	
			231	
			232	
		10.5.4 Integral Points, Volume Locking,		
			234	
	10.6	Initial Conditions	236	
	References			
11	Solut	tion in Time	241	
11	11.1		241	
	11.1	11.1.1 Numerical Integration Scheme	241	
		11.1.2 Stability of Numerical Integral	242	
		11.1.2 Stability of Numerical Integration Scheme	249 252	
	11.2	Frequency Domain Analysis	254	
	11.3	Multiple Reflection Theory	257	
	11.4	Equivalent Linear Method	260	
	A . A . T	11.4.1 Method in SHAKE	261	
		11.4.2 Limitation of SHAKE	263	

Contents xiii

		11.4.3	Improvement of SHAKE	
		11.4.4	Equivalent Linear Analysis in Time Domain	
	D - C	11.4.5	Nonlinear Method and Equivalent Linear Method	
	Refere	ences	************************************	274
12	Evalu		Damping	
	12.1		esis Damping	
	12.2	Velocity	y Proportional Damping	
		12.2.1	2 0 1 0	
		12.2.2	Mode Proportional Damping	282
	12.3	Wave S	cattering	284
	12.4	Radiati	on Damping	290
	12.5	Numeri	ical Damping	290
	12.6	Dampir	ng as Alternative	291
	Refer	ences		292
13	Evalu	ation of	Accuracy and Earthquake Motion Indices	295
	13.1		ration, Velocity, and Displacement	
	13.2		c Intensity Scale.	
	13.3		I Intensity	
	13.4		ım	
	13.5		Quantities	
11.4				
14			f Vertical Arrays	
	14.1		ability of Equivalent Linear Method	
	14.2		nse at Medium Strain	
	14.3		nse at Large Strains	
	14.4		ms in Setting Elastic Modulus	
	14.5		of Layer Thickness and Choice of Property	
15			ious Factors from Case Studies	
	15.1	Scatter	ing of Nonlinear Property	. 329
	15.2		ring of Wave Velocity	
	15.3		lind Tests	
	15.4		Waves as Result of Numerical Integration	
	15.5		llent Linear vs. Truly Nonlinear	
	15.6	Detern	nination of Damping for Deep Bedrock Problem	. 343
	15.7	Role o	f Hysteretic Damping Term	. 344
	15.8	Location	on of Engineering Seismic Base Layer	. 349
		15.8.1	Problem to Separate at Engineering Seismic	
			Base Layer	
		15.8.2	Setting Design Earthquake Motion	
		15.8.3	Remarks	. 361
	References			
Inc	lex	Electrical and Alectrical		363

## Chapter 1 Propagation of Earthquake Waves in the Ground and Fundamentals of Earthquake Motion

Fundamental knowledge on the amplification and the attenuation of the earthquake waves, which is necessary to understand the wave propagation in the ground, is introduced in this chapter.

## 1.1 Wave Propagation from Source to the Site

An earthquake occurs at a fault, and the earthquake waves propagate from the fault to the site that an engineer is interested in. Paths that the earthquake waves propagate are schematically shown in Fig. 1.1. Several important features should be noted in this figure. Firstly, the path is separated into three regions. Secondly, there are two types of waves called body wave and surface wave. Finally, the path of the body wave is not linear but curves.

Waveforms of the surface and the body waves are schematically shown in Fig. 1.2 with traces of soil particle for the surface wave case. Concerning the earthquake resistant design, body wave is the most important one, which is again classified into two types of waves termed as P-wave and S-wave.

P-wave is the wave that arrives first at a site; the name "P" indicates primary. As the direction of the propagation and the direction of vibration are parallel, the P-wave is sometimes called as longitudinal wave. Since the density of the medium varies with the propagation, it is also called a compression wave or a compressional wave.

The "S" of S-wave indicates secondary, which means that S-wave arrives at a site secondly after the P-wave arrival. Since the direction of the wave propagation and the direction of the vibration are perpendicular to each other, it is also called as transverse wave. In addition, since it causes shear deformation in the medium, it is also termed as shear wave. When the soil particle vibrates in the plane of the wave

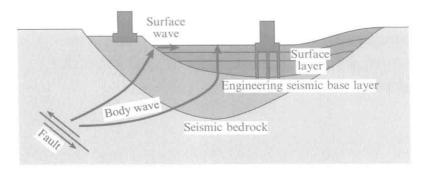


Fig. 1.1 Propagation of earthquake wave

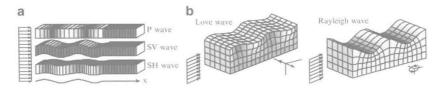


Fig. 1.2 Types of earthquake waves. (a) Body waves. (b) Surface wave

propagation, the S-wave is called as SV wave, and it is called SH wave when the soil particle vibrates out of the plane. Distinction between two waves is not necessary in the one-dimensional analyses although it is frequently called as SH wave. The SV waves are treated in the ordinary two-dimensional analysis.

As described in the next section (Sect. 1.1.2), earthquake wave propagates vertically when it is close to the ground surface. Consequently, the P-wave creates up-down or vertical vibration, and the S-wave causes horizontal vibration. Among these two body waves, the S-wave is the important wave in the earthquake resistant design. Therefore, almost all the content of this book deals with the S-wave; when a term "wave" appears, it refers to the S-wave. If the boundaries between any two layers are not perfectly perpendicular to the direction of the wave propagation, both P- and S-waves are refracted even though the incident wave is either P- or S-wave. These waves are called as PS or SP converted waves. Additionally, perfectly vertical wave propagation is just an approximation to observed wave phenomena. Therefore, vertical motion cannot be considered to be caused only by the P-wave and in exact sense horizontal motion only by the S-wave. However, it is also true that predominant horizontal motion is caused by the S-wave and vice versa. Therefore, for simplicity, the earthquake wave is assumed to propagate in the vertical direction, and the horizontal motion is caused only by the S-wave through this book.

A surface wave is generated by the interference of body waves radiated from the fault with a free surface. As schematically shown in Fig. 1.1, it is usually generated at an edge of a basin and propagates in the horizontal direction. The name "surface

wave" is because it propagates along the ground surface. Similar to the difference between SH and SV waves, there are two kinds of a surface wave. The one vibrates perpendicular to the plane of wave propagation and is called as Love wave, and the other one that vibrates in the plane of wave propagation is called as Rayleigh wave. Wave amplitude of a surface wave is largest at the ground surface and attenuates quickly with depth. Surface waves have another characteristic called dispersion, i.e., wave velocity depends on frequency. Amplitude of the wave is large, but at the same time, wavelength is long. Therefore, acceleration due to surface waves is not significantly considered in the design of ordinary structures. However, in the design of the underground lineal structures, it should be considered because of its large displacement (Committee of gas facility standard 2000). In addition, surface waves travel long distances because of their long wavelengths and may affect ultratall structures that have long natural periods. For example, ultra-tall buildings in Tokyo vibrated and were damaged during the 1983 Nihonkai-chubu earthquake (Kinoshita and Ohtake 2000) (epicentral distance is about 450 km) and during the 1984 Nagano-ken-seibu earthquake (Editorial committee of records of Nagano-kenseibu earthquake 1986) (epicentral distance of about 200 km). Similar phenomena were also reported in Tokyo during the 2000 Tottoriken-seibu earthquake (epicentral distance is about 580 km) and 2003 off Miyagi earthquake (epicentral distance is about 350 km). Likewise, the cause of the oil tank fire at Tomakomai, which is about 200 km far from the epicenter of the 2003 Tokachi-oki earthquake, is resonance due to the long period wave (JSCE Earthquake Committee 2003). Therefore, they require consideration in the earthquake resistant design, but this is not a subject in this book partly because it is not considered in the current design specifications and partly because the analysis is very difficult for practicing engineers.

## 1.1.1 Path of Wave Propagation and Analysis Region

It is a complicated problem to analyze the whole region shown in Fig. 1.1, i.e., from fault to site, in a single analysis. The problem is not easy partly because computer power is still not sufficient enough and partly because soil data in whole region is not sufficient. This whole region is divided into three subregions by setting two base layers which are called the seismic bedrock and the engineering seismic base layer. The latter is the generally used concept in Japan, but may not be common outside Japan although similar concept is used as explained in Sect. 3.1.

Seismic bedrock is widely known as the base layer. Two following concepts are introduced regarding the definition of seismic bedrock (Toki 1981):

Layer that behaves individually regardless of local site structure
 This definition indicates that the local site conditions have to be excluded in the
 definition of bedrock as the local site condition affects the earthquake motion at

the ground surface significantly. The seismic bedrock in this definition should satisfy the following two conditions:

- (a) The seismic bedrock spreads in certain extent, and mechanical properties in this layer are homogeneous.
- (b) Variation of mechanical properties and structure of the layers below the seismic bedrock is minor than those above it.
- The shallowest layer that can reflect the earthquake motion characteristics at the fault in the earthquake resistant design of structures

This definition comes from the structural design point of view and indicates that the base depth is selected providing that the thickness of the superficial layers is sufficient if the natural period above the base is a little longer than the natural period of structures.

The earthquake motion observed at the interested site R(t), as a function of time t, can be evaluated from the occurrence Q(t) at the source (fault), behavior P(t) from source to the bedrock, and amplification characteristics G(t) from bedrock to the ground surface (AIJ 1987) as

$$R(t) = Q(t) \otimes P(t) \otimes G(t) \tag{1.1}$$

where  $\otimes$  indicates convolution. Here, G(t) is separated into two parts as shown in Fig. 1.1, i.e., a path from the seismic bedrock to the engineering seismic base layer and a path above it. It is noted that Eq. (1.1) holds when there is no interaction between each part. In other words, earthquake motion is assumed as propagating in one way from seismic bedrock to the engineering seismic base layers, and reflected wave from the surface layer does not alter the incident wave to the surface layer. This definition is compatible with the first definition of the seismic bedrock described above. It is, however, noted that this assumption does not always hold (Yoshida et al. 2005), which will be discussed in Sect. 15.8.

It is necessary to understand the general feature of the S-wave velocity structure in order to understand the earthquake wave propagation. Earthquakes occur at a fault in the earth crust above the upper mantle. The representative value of the S-wave velocity is about 3.5 km/s in the upper earth crust (Kinoshita and Ohtake 2000). The seismic bedrock is mainly composed of granite for which the S-wave velocity is about 3 km/s (Irikura 1978). The S-wave velocity of the engineering seismic base layer is defined to be between 300 and 700 m/s in Japan and will be explained in detail in Sect. 3.1.

The S-wave velocity decreases in the superficial layers. It is about 100 m/s in the soft soil sites in the urban area. Since man activities densify the subsurface layers, 100 m/s may be the minimum value in the urban area, but it can have much smaller values in the country or undeveloped areas. In general, S-wave velocity becomes smaller as the depth becomes shallower partly because the soil is consolidated and solidified more at greater depths and partly because the elastic modulus as well as the wave velocity depends on the confining stress.

Although both density and wave velocity are necessary in discussing the wave propagation characteristics, bedrock is defined only by the wave velocity since the densities of the rock and soil are similar to each other, of the order of 2 t/m<sup>3</sup>.

## 1.1.2 Path of Body Wave Propagation

One of the important features shown in Fig. 1.1 is that the path from the fault to the site is not straight but curved. This behavior is strongly related to the aforementioned wave velocity structure.

A boundary between two layers with different S-wave velocities  $V_1$  and  $V_2$  is schematically shown in Fig. 1.3a. Snell's law indicates the relationship between the incident angle  $\theta_1$  and the refraction angle  $\theta_2$  as follows:

$$\frac{\sin \theta_2}{\sin \theta_1} = \frac{V_2}{V_1} \tag{1.2}$$

This law can be applied not only to the earthquake waves but also to other waves such as sea waves and lights. As a comprehensive example, let us consider the situation shown in Fig. 1.3b. You are sitting at point A in the shore and see a drowning person at B in the sea. The problem here is that which path is the fastest to arrive at. A straight line AB is not an optimal path because distance in the sea (very low speed) is longest. Although the distance in the sea is shortest in the rectangular path ACB, distance in the shore is the longest. Therefore this path is again not an optimal path. The optimal path ADB lies between these two ultimate paths, and it can be found from Eq. (1.2).

Change of the refracted angle evaluated from Eq. (1.2) is shown in Fig. 1.4 by two different expressions. For example, setting  $V_1 = 3,000$  m/s (seismic bedrock),  $V_2 = 150$  m/s (soft ground), and  $\theta_1 = 45^\circ$ , refracted angle is computed as  $\theta_2 = 2^\circ$ , which indicates that the wave propagates nearly in the vertical direction. This can be demonstrated again by adapting to sea waves.

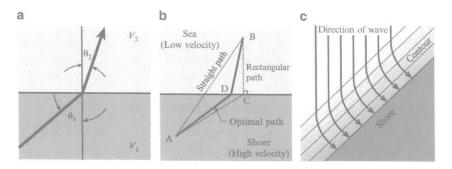
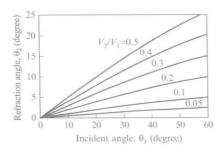


Fig. 1.3 Refraction of waves. (a) Refraction of wave. (b) Action near shore. (c) Sea waves at shore



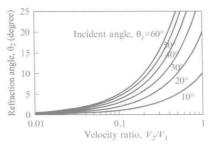


Fig. 1.4 Incident angle vs. refraction angle

When you see sea waves coming toward you on the shore, you feel that the wave front is parallel to the shore line. According to the wave theory, the wave velocity is obtained by  $\sqrt{gh}$  where g is the acceleration of gravity and h is the depth of the seabed; wave velocity becomes smaller as closer to the shore. Therefore, as shown in Fig. 1.3c, the path curves are perpendicular to the shore when the waves come close to the shore since equi-depth contours are parallel to the shore. As a conclusion, phenomena that earthquake waves propagate in vertical direction as they approach the surface and that sea waves travel perpendicular to the shore are the same mechanism.

## 1.2 Amplification of Earthquake Wave

There are significantly different wave propagation characteristics between the path from the fault to the seismic bedrock and the path from the engineering seismic base layer to the ground surface. The wave radiates in all directions in the former case, whereas it propagates in one direction in the latter case.

When the wave radiates in all directions, the amplitude becomes smaller as the wave front expands, while the distance from the fault increases. This phenomenon is known as attenuation of the earthquake waves, and an example is shown in Fig. 1.5. Here PGA and PGV in the ordinate denote the peak ground acceleration and velocity, respectively.

On the other hand, attenuation of this kind does not occur when the wave propagates in one direction, but different mechanisms work and as a result amplification and/or attenuation (deamplification) occurs. The mechanisms that cause amplification are explained in this section, and the rest is shown in the next section. There are four mechanisms that amplify the earthquake wave.

## 1.2.1 First Mechanism: Change of Wave Velocity

Let us consider the sea wave case again to understand this mechanism. When the sea wave propagates toward the shore, wave velocity becomes smaller as explained