

SEEING THROUGH STATISTICS

Jessica M. Utts

Seeing Through Statistics

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University of California, Davis

An Alexander Kugushev Book



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To
Patrick and
his grandmother

Preface

Purpose

Statistics deals with complexity and uncertainty. We are exposed daily to information from surveys and scientific studies concerning our health, behavior, attitudes, beliefs, or scientific and technological breakthroughs. This book's first objective is to help you understand this information and to sort out the useful and the accurate from the useless and the misleading. My aim is to allow you to rely on your own interpretation of results emerging from surveys and studies; you will be able to read them with a critical eye and make your own judgments.

A second purpose of this book is to demystify statistical methods. Traditional statistics courses often place emphasis on how to compute, rather than on how to understand. This book emphasizes statistical ideas and their use in real life.

Finally, the book contains information intended to help you make better decisions when faced with uncertainty. You will learn how psychological influences can keep you from making the best decisions, and new ways to think about coincidences, gambling and other circumstances that involve chance events.

Approach

The focus of this book is on the use of statistical methods in the real world. There are dozens of real, in-depth case studies taken from various media sources as well as scores of additional real examples. The emphasis is on understanding, rather than computing, but there are also examples of how to compute important numbers when necessary.

Although the book is written as a textbook, it is also intended to be readable without the guidance of an instructor. Each concept or method is explained in plain language and supported with numerous examples.

Organization

There are 26 chapters divided into four parts. Each chapter covers material more or less equivalent to a one-hour college lecture. The final chapters of Part 1 and Part 4 consist solely of case studies, and are designed to illustrate the thought process you should follow when you read studies on your own.

Parts 1 and 2 are entitled “Finding Data in Life” and “Finding Life in Data.” By the end of Part 1 you will already have the tools to determine whether or not the results of a study should be taken seriously. You will be able to detect false conclusions and biased results. In Part 2 you will learn how to turn numbers into useful information, and how to quantify relationships between things like aspirin consumption and heart attack rates or meditation and aging. You will also learn how to detect misleading graphs and figures, and how to interpret common economic statistics.

Part 3 is called “Understanding Uncertainty in Life” and is designed to help you do exactly that. We are all required to make decisions in the face of uncertainty on a daily basis. This part of the book will help you understand what probability and chance are all about, and describe some techniques that can help you make better decisions. The material on probability will also be useful for Part 4, “Making Judgments from Surveys and Experiments.”

Part 4 is slightly more technical than the rest of the book, but once you have mastered it you will truly understand the beauty of statistical methods. Henceforth when you read the results of a statistical study, you will be able to tell whether they represent valuable advice, or flawed reasoning. Unless things have changed drastically by the time you read this, you will be amazed at the number of news reports that exhibit flawed reasoning.

Thought Questions: Using Your Common Sense

Each of the chapters, except those consisting solely of case studies, begins with a series of “thought questions.” They are designed to be read and answered *before* you read the chapter. Most of the answers are based on common sense, perhaps combined with knowledge from previous chapters. Answering them in advance of reading the material will reinforce the idea that most of the information in this book is based on common sense. You will find answers to the thought questions, or similar ones, embedded in the chapters.

In the classroom, the thought questions can be used for discussion at the beginning of each class. For relatively small classes, groups of students can be assigned to discuss one question each then report back to the class. If you are taking a class in which one of these formats is used, try to answer the questions on your own before class. By doing so, you will build confidence as you learn that the material is not difficult to understand if you give it some thought.

Case Studies and Examples: Collect Your Own

The book is filled with real case studies and examples covering a very wide range of disciplines. They are intended to appeal to a broad audience. In the rare cases where technical subject matter knowledge is required it is given with the example. Sometimes the conclusion presented in the book will be different from the

conclusion presented in the original news report. This is because many news reports misinterpret statistical results.

While I hope you find the case studies and examples interesting and informative, you will learn the most by finding current examples on topics of interest to you. Follow any newspaper or news magazine for awhile and you are sure to find plenty of illustrations of the use of surveys and studies. Start collecting them now, and you can watch your understanding of them increase as you work your way through this book.

Formulas: It's Your Choice

If you are one of those who dreads mathematical formulas, you should find this book comfortably readable. In most cases where computations are required, they are presented step-by-step rather than in a formula. And the steps are accompanied by worked examples so you can see exactly how to carry them out.

On the other hand, if you prefer to work with formulas, each relevant chapter ends with a section called "For Those Who Like Formulas." The section includes all of the mathematical notation and formulas pertaining to the material in that chapter.

Exercises and Mini-Projects

There are numerous exercises at the end of each chapter. Many of them are similar to the "thought questions" and require an explanation for which there is no one correct answer. Answers to some of those with concise solutions are provided at the back of the book. *Teaching Seeing Through Statistics: An Instructor's Resource Manual* is available to instructors, and explains what is expected for each exercise.

In most chapters the exercises contain many additional real examples. However, with the idea that you learn best by doing, most chapters also contain "Mini-Projects." Some of these ask you to find examples of studies of interest to you. Others ask you to conduct your own small-scale study. If you are reading this book without the benefit of a class or instructor, I encourage you to try some of the projects on your own.

Covering the Book in a Quarter, Semester or on Your Own

This book was written for a one-quarter course taught three times a week at the University of California at Davis, as part of the general education curriculum. My aim was to allow one lecture for each chapter, and in most cases that practice works quite well. A few chapters may spill over into two lectures, still allowing

for completion of the book (and a midterm or two) in the usual 29 or 30 lecture quarter. I do not cover every detail from each chapter; I expect students to read some material on their own.

If the book is used for a semester course it can be covered at a more leisurely pace and in more depth. For instance, two classes a week can be used for covering new material and a third class for discussion, additional examples or laboratory work. Alternatively, with three regular lectures a week some chapters can be covered in two sessions instead of one.

Instructors can obtain a copy of *Teaching Seeing Through Statistics: An Instructor's Resource Manual*, containing additional information on how to cover the material in one quarter or semester. The *Resource Manual* also gives tips on teaching this material, ideas on how to cover each chapter, sample lectures, additional examples and exercise solutions.

Instructors who want to focus on more in-depth coverage of specific topics may wish to exclude others. Certain chapters can be omitted without serious consequences in later chapters. These include Chapter 9, Chapters 13 and 14 (but Chapter 14 relies on Chapter 13), Chapter 17 and Chapter 25. The chapters in Part 3 (15 to 18) rely on each other, but only parts of Chapter 15 are needed in order to understand Part 4 of the book. Thus, Chapters 16 to 18 (as a unit) could be omitted.

If you are reading this book on your own you may find that you want to concentrate on selected topics only. Parts 1 and 3 can be read alone, as can Chapters 9 and 13. Part 4 relies most heavily on Chapters 8, 12 and 15. Although it is the most technically challenging, I strongly recommend reading Part 4, since it is there that you will truly learn the beauty as well as the pitfalls of statistical reasoning. If you get stuck try to step back and reclaim the big picture. Remember, statistical methods are very powerful and are subject to abuse, but they were developed using the collective common sense of researchers who needed to figure out how to find and interpret information to understand the world. They have done the hard work; this book is intended to help you make sense of it all.

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Jessica Utts
Davis, CA

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