

Bioinspired Legged Locomotion

Models, Concepts, Control and Applications



Edited by

Maziar A. Sharbafi and André Seyfarth



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André Seyfarth



Butterworth-Heinemann
An imprint of Elsevier

Butterworth-Heinemann is an imprint of Elsevier
The Boulevard, Langford Lane, Kidlington, Oxford OX5 1GB, United Kingdom
50 Hampshire Street, 5th Floor, Cambridge, MA 02139, United States

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Library of Congress Cataloging-in-Publication Data

A catalog record for this book is available from the Library of Congress

British Library Cataloguing-in-Publication Data

A catalogue record for this book is available from the British Library

ISBN: 978-0-12-803766-9

For information on all Butterworth-Heinemann publications
visit our website at <https://www.elsevier.com/books-and-journals>



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Publisher: Joe Hayton
Acquisition Editor: Sonnini R. Yura
Editorial Project Manager: Mariana Kuhl
Production Project Manager: Kiruthika Govindaraju
Designer: Vitoria Pearson

Typeset by VTeX

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List of Contributors

Maziar A. Sharbafi:

*To my wife, Aida, for her devotion and endless support;
her selflessness will always be remembered.*

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List of Contributors

Aaron D. Ames

Mechanical and Civil Engineering and Control and Dynamical Systems,
California Institute of Technology (Caltech), United States

Maziar A. Sharbafi

School of Electrical and Computer Engineering, College of Engineering,
University of Tehran, Iran

Lauf Labor Locomotion Laboratory, TU Darmstadt, Germany

Mahesh M. Bandi

Collective Interactions Unit, OIST Graduate University, Tancha, Okinawa,
Japan

Pranav Bhounsule

Department of Mechanical Engineering, The University of Texas at San
Antonio, San Antonio, TX, United States

Thiago Boaventura

ADRL, ETH Zürich, Zürich, Switzerland

Jonas Buchli

ADRL, ETH Zürich, Zürich, Switzerland

Charles Capaday

Universitätsmedizin Göttingen, Institute for Neurorehabilitation Systems,
Georg-August University Göttingen, Göttingen, Germany

Chien Chern Cheah

School of Electric and Electronic Engineering, Nanyang Technological
University, Singapore

Jonathan E. Clark

Department of Mechanical Engineering, FAMU/FSU College of Engineering, Tallahassee, FL, United States

Steven H. Collins

Department of Mechanical Engineering, Carnegie Mellon University, United States

Robotics Institute, Carnegie Mellon University, United States

Hartmut Geyer

Robotics Institute, Carnegie Mellon University, Pittsburgh, PA, United States

Simon Gosgnach

Neuroscience and Mental Health Institute, University of Alberta, Edmonton, AB, Canada

Kevin W. Hollander

SpringActive, Inc.

Koh Hosoda

Department of System Innovation, Graduate School of Engineering Science, Osaka University, Toyonaka, Japan

Yue Hu

Optimization, Robotics & Biomechanics, ZITI, IWR, Heidelberg University, Heidelberg, Germany

Auke Ijspeert

Biorobotics Laboratory, EPFL – Ecole Polytechnique Fédérale de Lausanne, Lausanne, Switzerland

Tim Kiemel

School of Public Health, University of Maryland, United States

Matthew Kvalheim

Electrical Engineering and Computer Science, University of Michigan, Ann Arbor, MI, United States

David Lee

School of Life Sciences, University of Nevada, Las Vegas, United States

Dirk Lefeber

Department of Mechanical Engineering, Vrije Universiteit Brussel,
Brussels, Belgium

Shreyas Mandre

School of Engineering, Brown University, Providence, RI, United States

Katja Mombaur

Optimization, Robotics & Biomechanics, ZITI, IWR, Heidelberg
University, Heidelberg, Germany

Ioannis Poulakakis

Department of Mechanical Engineering, University of Delaware, Newark,
DE, United States

Arthur Prochazka

Neuroscience and Mental Health Institute, University of Alberta,
Edmonton, AB, Canada

Shai Revzen

Electrical Engineering and Computer Science, University of Michigan,
Ann Arbor, MI, United States

Christian Rode

Department of Motion Science, Friedrich-Schiller-Universität Jena, Jena,
Germany

Justin Seipel

Purdue University, West Lafayette, IN, United States

André Seyfarth

Lauflabor Locomotion Laboratory, TU Darmstadt, Germany

Tobias Siebert

Institute of Sport and Motion Science, University of Stuttgart, Stuttgart,
Germany

Thomas G. Sugar

Fulton Schools of Engineering, The Polytechnic School, Arizona State
University, AZ, USA

Heike Vallery

Faculty of Mechanical, Maritime and Materials Engineering, Delft
University of Technology, Delft, The Netherlands

Bram Vanderborght

Department of Mechanical Engineering, Vrije Universiteit Brussel,
Brussels, Belgium

Madhusudhan Venkadesan

Department of Mechanical Engineering & Materials Science, Yale
University, New Haven, CT, United States

Jeffrey Ward

SpringActive, Inc.

Maarten Weckx

Department of Mechanical Engineering, Vrije Universiteit Brussel,
Brussels, Belgium

Patrick M. Wensing

Department of Aerospace and Mechanical Engineering, University of
Notre Dame, Notre Dame, IN, United States

Juanjuan Zhang

Department of Mechanical Engineering, Carnegie Mellon University,
United States

School of Electric and Electronic Engineering, Nanyang Technological
University, Singapore

About the Editors

Maziar A. Sharbafi

Maziar A. Sharbafi is an assistant professor in Electrical and Computer Engineering Department of University of Tehran. He is also a guest researcher at the Locomotion Laboratory, TU Darmstadt. He studied control engineering at Sharif University of Technology and University of Tehran (UT) where he has received his Bachelor and Master's degrees, respectively. He started working on bipedal robot control during his PhD studies at University of Tehran which ended in 2007, and worked more on bio-inspired control approaches since he entered Lauflabor in 2011. His current research interests include bio-inspired locomotion control based on conceptual and analytic approaches, postural stability, and the application of dynamical systems and nonlinear control to hybrid systems (e.g., for legged locomotion).

André Seyfarth

André Seyfarth is a full professor for Sports Biomechanics at the Department of Human Sciences of TU Darmstadt and head of the Lauflabor Locomotion Laboratory. After his studies in physics and his PhD in the field of biomechanics, he went as a DFG "Emmy Noether" fellow to the MIT LegLab (Prof. Herr, USA) and the ParaLab at the university hospital Balgrist in Zurich (Prof. Dietz, Switzerland). His research topics include sport science, human and animal biomechanics and legged robots. Prof. Seyfarth was the organizer of the Dynamic Walking 2011 conference ("Principles and Concepts of Legged Locomotion") and the AMAM 2013 conference ("Adaptive Motions in Animals and Machines").

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