# THE PHYSICS OF THE STRATOSPHERE

BY

R. M. GOODY

Fellow of St John's College, Cambridge



CAMBRIDGE AT THE UNIVERSITY PRESS 1954

# CAMBRIDGE MONOGRAPHS ON PHYSICS

GENERAL EDITORS

N. FEATHER, F.R.S.

Professor of Natural Philosophy in the University of Edinburgh

D. SHOENBERG, Ph.D., F.R.S.

Fellow of Gonville and Caius College, Cambridge

# THE PHYSICS OF THE STRATOSPHERE

# GENERAL PREFACE

The Cambridge Physical Tracts, out of which this series of Monographs has developed, were planned and originally published in a period when book production was a fairly rapid process. Unfortunately, that is no longer so, and to meet the new situation a change of title and a slight change of emphasis have been decided on. The major aim of the series will still be the presentation of the results of recent research, but individual volumes will be somewhat more substantial, and more comprehensive in scope, than were the volumes of the older series. This will be true, in many cases, of new editions of the Tracts, as these are republished in the expanded series, and it will be true in most cases of the Monographs which have been written since the War or are still to be written.

The aim will be that the series as a whole shall remain representative of the entire field of pure physics, but it will occasion no surprise if, during the next few years, the subject of nuclear physics claims a large share of attention. Only in this way can justice be done to the enormous advances in this field of research over the War years.

N.F.

D. S.

#### AUTHOR'S PREFACE

I wrote this monograph assuming that the reader would be a physicist who was interested to learn something of the progress in a subject outside his own field of study. I should point out therefore that there is a very great difference between the approach to a laboratory problem and the approach to a geophysical (or, for that matter, astronomical) problem. In geophysics, and particularly in atmospheric physics, experiments are either impracticable or of limited value. Controlled conditions are essential for a successful experiment, while with the atmosphere it is only possible to observe and to hope that the conditions relevant to a unique interpretation are either known or can be guessed. It is not surprising that this may lead to incompatible results from two apparently reliable observations, each intelligently interpreted, and there are examples of this kind in the following pages. While the laboratory worker would wisely reject such results as untrustworthy, the atmospheric physicist must often accept them as the only results he is likely to obtain.

Every research has its own difficulties, and atmospheric physics is not unique in the effort, expense and even personal discomfort that may be involved in gathering representative observations. However, once again, it differs from most branches of physics in working with a system which is very far from equilibrium. As a result it is very difficult to specify just how many observations are desirable, and, moreover, when it comes to theoretical interpretation, equilibrium hypotheses, which are normally so valuable, turn out to be useful for a rough superficial examination only.

In presenting this subject to those who have not studied geophysics, I have sought to emphasize characteristic features where they appeared to be instructive, but to avoid issues which seemed to me to be particularly confusing. If this monograph had been written for the geophysicist, I would have had to consider in greater detail the differences of opinion which exist upon nomenclature, the relative importance of different topics, the relative reliability of different observations, etc. The meteorologist,

for example, might well consider that my treatment of dynamical matters is most inadequate. I hope, however, that those who specialize in this subject will derive some of the interest from reading this monograph that I have derived from writing it.

I am indebted to Drs G. K. Batchelor, M. V. Wilkes and T. W. Wormell for commenting upon some sections. Mr C. D. Walshaw read the manuscript with care and found many minor errors and obscurities. Mr H. E. Goody has helped me greatly with his thorough reading of the proofs.

R. M. GOODY

Cambridge 1953

# PUBLISHED BY THE SYNDICS OF THE CAMBRIDGE UNIVERSITY PRESS

London Office: Bentley House, N.W. 1 American Branch: New York

Agents for Canada, India, and Pakistan: Macmillan

Printed in Great Britain at the University Press, Cambridge (Brooke Crutchley, University Printer)

#### CONTENTS

### AUTHOR'S PREFACE

page ix

#### CHAPTER I

#### Introduction

1.1. The discovery of the stratosphere, p. 1. 1.2. Nomenclature, p. 3. 1.3. Scope of the monograph, p. 7. 1.4. Tools of research, p. 9.

#### CHAPTER II

## Temperature

2.1. Introduction, p. 19. 2.2. The lower stratosphere, p. 22. 2.3. Propagation of sound, p. 30. 2.4. Meteors, p. 36. 2.5. Rockets, p. 41. 2.6. Confirmatory evidence, p. 46.

#### CHAPTER III

# Composition

3.1. General survey, p. 55. 3.2. Water vapour, p. 58. 3.3. Carbon dioxide, p. 70. 3.4. The rare gases, p. 72. 3.5. Other minor constituents, p. 77.

#### CHAPTER IV

#### Ozone

4.1. Introduction, p. 81. 4.2. Methods of measurement, p. 86. 4.3. Systematic ozone measurements, p. 112. 4.4. Theoretical treatment, p. 117.

#### CHAPTER V

#### Winds and Turbulence

5.1. Stratospheric winds, p. 125. 5.2. Turbulence in the stratosphere, p. 136.

#### CHAPTER VI

# Radiation

6.1. Introduction, p. 142. 6.2. Absorption by molecular bands, p. 151. 6.3. Numerical computations, p. 164. 6.4. The thermal structure of the atmosphere, p. 169.

REFERENCES

page 176

INDEX

,, 183

#### CHAPTER I

#### INTRODUCTION

# 1.1. The discovery of the stratosphere

Towards the end of the last century, meteorologists were actively investigating the structure of the atmosphere away from the earth's surface by using kites and balloons carrying thermometers and pressure gauges. It was normally found that the temperature decreased with height at a rate of 5-10° K./km. These results fit in well with the idea of an atmosphere well stirred by winds, since violent mixing in a dry atmosphere should lead to a lapse rate† of 10° K./km. (the dry adiabatic lapse rate). Although the average observed lapse rate is less than the dry adiabatic, the condensation of water vapour would modify the adiabatic lapse rate in just this direction. As a result there was, at this time, a comfortable feeling among meteorologists that there was nothing more to be discovered. Crossley (1934) has attempted to analyse this attitude and has given three reasons why, in those days, it was confidently expected that the temperature of the atmosphere would always decrease with height:

- '(a) As the temperature of the base of the atmosphere is that of the surface of the earth, and as the outer limit of the atmosphere must approach the absolute zero of temperature, the air temperature must, on the whole, decrease from the surface outwards.
- '(b) The temperature is observed to decrease with height up to 10 km. or more according to latitude.
- '(c) There is also a feeling that the temperature should decrease with height because the pressure does.'

Needless to say, these arguments do not bear close examination, but nevertheless the ideas behind them must have had general acceptance.

Despite this apparently satisfactory position the French investigator Teisserenc de Bort started in 1898 to use balloons in an

† According to normal meteorological terminology a 'lapse' is a negative vertical temperature gradient, i.e. temperature decreasing with height. Similarly, an 'inversion' is a positive temperature gradient.

attempt to obtain reliable temperature measurements up to 14 km. Like other workers at this time, he was greatly concerned with the errors of observation, which seemed to fall under three main headings:

- (a) Errors of pressure, and therefore height, measurement.
- (b) Lag of the thermometers.
- (c) Radiation errors, caused by the direct absorption of solar radiation at great heights where the ventilation of the thermometers was inadequate.

It was possible to make estimates of the errors arising from (a) and (b), but (c) was indeterminate, although it was known that it could be large. When it appeared to be indicated in 1898 that above 11 km, the temperature of the atmosphere during daytime ceased to decrease with height and became constant, Teisserenc de Bort naturally concluded that he was faced with radiation errors. Experiments in 1899 showed, however, that this 'isothermal layer', as he named it, still existed at night-time, and two years later enough evidence had been collected for him to be able to announce his discovery as clearly established. By 1904 Teisserenc de Bort was able to publish the results of 581 ascents, 141 of which went to 14 km., and to distinguish some general properties of the layer, e.g. that it is low over depressions but high over anticyclones. Fig. 1 shows seasonal average curves constructed from these early results.

Thus, in 1904, the discovery of the isothermal layer had been firmly consolidated, although a number of years were to pass before it was generally accepted. The care with which Teisserenc de Bort unravelled a major discovery from the errors of a very difficult experiment, by means of careful and frequent measurements, makes this research one of the finest in the history of meteorology.

The first man to enter the stratosphere for certain, and to survive, was the Belgian Piccard who ascended to 16 km. in 1931. He might, however, have been preceded. On 5 September 1862 two Englishmen, Glaisher and Coxwell, claimed to have reached a height of 11.3 km. in an open gondola without oxygen apparatus. This may have taken them into the stratosphere, but even if it did, the aeronauts were scarcely fit to make observations, since

Glaisher was unconscious and Coxwell so badly frostbitten that he had to open the release valve with his teeth. This was only one of a long series of ascents which Glaisher and Coxwell made in their 93,000 cu.ft. capacity 'Mammoth' balloon.

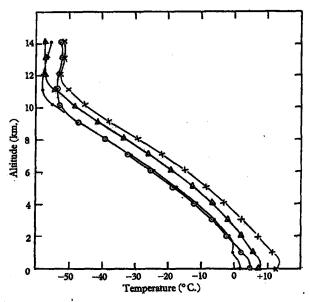


Fig. 1. The first 141 temperature records up to 14 km., grouped according to season. (After Teisserenc de Bort.) (N.B. These do not necessarily correspond exactly with the best modern measurements.) — — spring; — × — summer; — — autumn; — winter.

#### 1.2. Nomenclature

It was soon discovered that the 'isothermal layer' is hardly ever exactly isothermal, and the name dropped out of general use after a decade. The most striking property of the layer was then recognized to be its great hydrostatic stability, suggesting that it might be stratified as opposed to mixed (this being the definition of the meteorological term 'stratification'). This led Teisserenc de Bort himself to suggest the word 'stratosphere' for his discovery and the word 'troposphere' for the underlying atmosphere.† Since much interest would obviously attach itself to the boundary between these regions, and since this boundary appeared to be a

† Greek tropos = turn; troposphere = turning or mixing sphere.

rather definite feature, it was not long before a name was found for it, the 'tropopause', suggested by Hawke and popularized by Napier Shaw.

The problem of upper-atmosphere nomenclature is now one of importance and difficulty. The definition of terms depends upon the definition of measurable features, but unfortunately most upper-atmosphere measurements are made on the limits of observation and frequently can be interpreted in more than one way. Moreover, the atmosphere is not in a steady state and measurements will never be exactly repeatable. Finally, such measurements as exist—even the voluminous records of meteorological services—are at the best only a few spot measurements in a complicated three-dimensional field. Under these circumstances care has to be exercised in the naming of a feature, since merely giving a name may imply a physical significance which later turns out to be illusory.

The difficulties of definition stem from the many different types of feature which may be measured and therefore named: thermal structure, dynamical factors (wind, etc.), concentration of major constituents (oxygen, nitrogen), concentration of minor constituents (water vapour, ozone), visible phenomena (water and ice clouds, aurorae, nightglow emissions) and electron density. There is little reason to expect detailed correspondence between these features, and fortunately there is no reason to give them all equal weight. The cornerstone of studies in atmospheric physics will always be the transformations of energy which take place, and the dynamical and thermal structures of the atmosphere are most indicative of these transformations. Dynamical factors, however, such as wind, are far too variable to be of use in general discussion, and the thermal structure is therefore the obvious choice for the purposes of nomenclature.

In fig. 2 is shown the approximate temperature distribution in the atmosphere up to 120 km. in temperate latitudes; methods of measurement will be discussed in the next chapter. Nearest to the earth's surface is the layer [a], where temperature decreases with height at about 6.5° K./km.; this is universally known as the 'troposphere'. The troposphere ends at the 'tropopause', [x], or if doubts exist as to whether this really is a well-defined feature the

term 'tropopause layer' may be introduced. We will adhere to the use of the word 'tropopause', implying thereby a belief that a rather sudden change of temperature gradient at this point is the normal state of the atmosphere. The word 'stratosphere' was originally introduced to indicate the approximately isothermal region above the tropopause. We shall use the word in a wider sense, to mean that part of the atmosphere between the tropopause

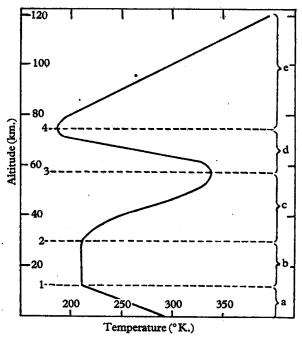


Fig. 2. Approximate vertical temperature distribution in the atmosphere in temperate latitudes.

and the inversion which starts near 75 km., [4]. By analogy with the tropopause, the feature [4] has been called the 'stratopause'. The stratosphere can conveniently be divided into the approximately isothermal region [b], or 'lower stratosphere', and the rest [c+d], or the 'upper stratosphere'. Above the stratopause lies a region whose thermal properties are not well understood, and which has mainly been investigated by means of radio techniques which have established the existence of large electron densities. It seems reasonable, therefore, that at present this region should

be named after the various ionized layers which have been discovered (viz. D, E,  $F_1$  and  $F_2$ ), and that the whole region up to at least 400 km. should be called the 'ionosphere'. It has also been suggested that the upper layers of the atmosphere above 600 km., where collisions are extremely rare, should be called the 'exosphere'.

In Table I the nomenclature adopted here is compared with suggestions which have been made by Chapman (1950) and Flöhn and Penndorf (1950). Chapman gives three forms, based upon thermal properties, homogeneity (the atmosphere is believed to be thoroughly mixed below the stratopause, see Chapter III)

Chapman Refer This book Flöhn and Penndorf ence ΪĬ ш Advection layer Troposphere Troposphere Tropopause layer Isothermal Tropopause Tropopause b Stratosphere Lower layer Stratopause Homo-Neutro-Warm laver Mesosphere sphere Strato-Stratoincline sphere sphere Meso-peak Meso-Upper Ozonopause Meso-3 sphere Upper mixing ď decline. layer Upper tropopause Stratopause Neutropause Ionosphere Mesopause Homopause Ionosphere Thermosphere Ionosphere Heterosphere

TABLE I. Atmospheric nomenclature

and electrical properties. He distinguishes therefore between a 'mesopause', a 'homopause' and a 'neutropause'; but since experiment cannot distinguish clearly between the heights of these features there seems little object at present in introducing this degree of complication.

The nomenclature of Flöhn and Penndorf, although less complicated than Chapman's, is not very appropriate. The 'isothermal layer', as we have seen, is hardly ever isothermal. The 'warm layer' includes only half of the feature which might deserve this name. Finally, experiment indicates slow mixing throughout the stratosphere, and therefore the name 'upper mixing layer' conveys no useful meaning.

It is not suggested that the nomenclature adopted in this monograph has any particular physical significance.† Its main merits are that it introduces no unusual terms, so that those familiar with

<sup>†</sup> In fact Chapman's use of the word 'stratosphere' is correct physically.

the literature will recognize the meanings of terms without formal definition, and that it conveys no more than the experimental evidence justifies.

# 1.3. Scope of the monograph

In the following chapters we will discuss briefly the main physical properties of the stratosphere, only considering the troposphere and the ionosphere where it is essential to preserve continuity. Work upon this region of the atmosphere has mainly been concerned with measurements and calculation of the temperature, the composition, the dynamical structure and the radiation balance. With regard to temperature, we require to know not only the general vertical structure but also the variations which take place daily, seasonally, and from one latitude to another, for such information gives a valuable guide to underlying processes. Atmospheric composition is of interest from many points of view: most methods of measuring temperature depend upon a knowledge of the mean molecular mass of air; the extent to which gases separate out under gravity indicates the degree of mixing which is taking place; the radiation balance at levels below the stratopause, which creates the sources and sinks of energy necessary to maintain the atmospheric motions, is almost entirely controlled by the concentrations of three minor atmospheric constituents, viz. ozone, water vapour and carbon dioxide, which present many interesting problems of measurement; ozone is created and destroyed in situ, and its concentration is so intimately bound up with atmospheric conditions that the study of this gas is almost a branch of geophysics in its own right. Finally, the dynamical structure of the atmosphere is one of the clearest indications of the transformations of energy which continually take place, and the theory of radiation transfer is required to link together such studies with information upon temperatures and composition.

By limiting discussion to the stratosphere we shall not be considering many important atmospheric phenomena. As far as is known, a number of changes take place just above the stratopause. The atmosphere becomes ionized and therefore conducting, and there have been many interesting studies upon the reflexion of radio waves and short-period variations of the earth's magnetic

field. Also, approximately at this level, most molecules except nitrogen begin to be dissociated by the ultra-violet radiation from the sun, leading to uncertainties in our knowledge of the mean molecular mass for air, and therefore to uncertainties in temperature measurement (see Chapter II). Further, atomic and molecular mean free paths become so great that diffusive transfer begins to predominate over mixing processes. Aurorae practically never penetrate into the stratosphere, and although some night-glow emissions are now considered to be located near 70 km., they are still generally associated with higher levels.

All these extremely interesting topics will be only briefly mentioned where they lead to information about the atmosphere near the stratopause. The reader who is interested in these problems is, however, fortunate in the recent publication of a number of books and reviews dealing with them, which are listed at the end of this monograph.

Going to the other extreme, the stratosphere is just above the levels involved in the important and complicated phenomena of weather. There is a tendency now for meteorologists to include the lower stratosphere in their dynamical considerations, although marked reactions of stratospheric conditions upon weather have yet to be demonstrated. The extremely important subject of cloud and rain formation is almost entirely restricted to the troposphere, though the highest layers of cirrus and cumulo-nimbus lie only just below the tropopause.

The remaining portion of the atmosphere, which will be described in this monograph, is neither so close that mistakes in the computation of minor perturbations are a subject for discussion in the press and on the radio, nor yet so remote that it is necessary to work with techniques akin to astronomy. It is a region whose main features can be measured and explained by fairly straightforward physical methods, and it is the application of these methods to a field problem of great complication which will be the main concern of this book.

Finally, there will only be passing reference to the important subject of atmospheric oscillations, not because it is inappropriate, but because it has already been discussed in a monograph in this series (Wilkes, 1949).

# 1.4. Tools of research

Much of our knowledge of the upper atmosphere is based upon measurements made at ground level, and owing to the care and accuracy possible in the laboratory such measurements will always be of great importance. There is little in common between various ground-level experiments, except perhaps that most make use of some section of the electromagnetic spectrum, and they all need to be described individually in their context in later chapters.

In recent years it has become more and more common to attempt to make direct measurements by transporting instruments into the stratosphere on various types of vehicle. The limitations of such experiments are often imposed by the characteristics of the vehicle itself; and therefore it is worth while to discuss the important features of the three possibilities available, viz. balloons, aircraft and rockets.

# 1.41. Balloons

The first attempts to make measurements of the upper atmosphere employed kites and balloons. Balloons soon proved their superiority by ascending to much greater heights. The techniques of manned and unmanned balloon ascents differ very greatly, and the former have now fallen into disuse, though in the past much useful information has been gained by this method of investigation.

The main characteristic of the manned balloon ascent is the great weight that has to be carried. The observer is a considerable load, particularly since he must be protected against the low pressures of altitudes greater than 10 km., and such ascents are justifiable only if a quantity of apparatus is carried. The last great ascent was by the American helium-filled Explorer II (1938). It reached a record height of 22 km. In order to lift the weights involved, the capacity of the balloon was 3,750,000 cu.ft., although only a small fraction of this could be filled with helium at ground level since the pressure at the ceiling was only  $\frac{1}{28}$  atmosphere, and a really elastic balloon is not acceptable for a manned ascent. The Explorer II had a spherical aluminium gondola in which three men could be carried. The total flight time was 8 hours 13 minutes, during which time many observations were taken, including