

′ 学与工程丛书

6

Propagation Dynamics on Complex Networks

Models, Methods and Stability Analysis

英文版

复杂网络传播动力学——模型、方法与稳定性分析

■ 傅新楚 Michael Small 陈关荣 著





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序

随着以互联网为代表的网络信息技术的迅速发展,人类社会已经迈入了复杂网络时代。人类的生活与生产活动越来越多地依赖于各种复杂网络系统安全可靠和有效的运行。作为一个跨学科的新兴领域, "网络科学与工程"已经逐步形成并获得了迅猛发展。现在,许多发达国家的科学界和工程界都将这个新兴领域提上了国家科技发展规划的议事日程。在中国,复杂系统包括复杂网络作为基础研究也已列入《国家中长期科学和技术发展规划纲要(2006—2020年)》。

网络科学与工程重点研究自然科学技术和社会政治经济中各种复杂系统微观性态与宏观现象之间的密切联系,特别是其网络结构的形成机理与演化方式、结构模式与动态行为、运动规律与调控策略,以及多关联复杂系统在不同尺度下行为之间的相关性等。网络科学与工程融合了数学、统计物理、计算机科学及各类工程技术科学,探索采用复杂系统自组织演化发展的思想去建立全新的理论和方法,其中的网络拓扑学拓展了人们对复杂系统的认识,而网络动力学则更深入地刻画了复杂系统的本质。网络科学既是数学中经典图论和随机图论的自然延伸,也是系统科学和复杂性科学的创新发展。

为了适应这一高速发展的跨学科领域的迫切需求,中 国工业与应用数学学会复杂系统与复杂网络专业委员会偕 同高等教育出版社出版了这套"网络科学与工程丛书"。 这套丛书将为中国广大的科研教学人员提供一个交流最新 研究成果、介绍重要学科进展和指导年轻学者的平台,以 共同推动国内网络科学与工程研究的进一步发展。丛书在 内容上将涵盖网络科学的各个方面,特别是网络数学与图 论的基础理论,网络拓扑与建模,网络信息检索、搜索算 法与数据挖掘,网络动力学(如人类行为、网络传播、同 步、控制与博弈),实际网络应用(如社会网络、生物网 络、战争与高科技网络、无线传感器网络、通信网络与互 联网),以及时间序列网络分析(如脑科学、心电图、 音乐和语言)等。

"网络科学与工程丛书"旨在出版一系列高水准的研究专著和教材,使其成为引领复杂网络基础与应用研究的信息和学术资源。我们殷切希望通过这套丛书的出版,进一步活跃网络科学与工程的研究气氛,推动该学科领域知识的普及,并为其深入发展做出贡献。

金芳蓉 (Fan Chung) 院士 美国加州大学圣地亚哥分校 二〇——年元月

Preface

Throughout history, epidemic diseases have been a serious threat to human health and life. In the past few years, many infectious diseases such as dengue, malaria, HIV, and SARS have captured global attention. Many of these, and others, remain a great threat, with potential for new outbreaks – particularly, for example, with a human-transmissible version of the H5N1 avian influenza. Moreover, with the development of globalized transportation, the potential for epidemic transmission has become much greater. Once a disease emerges, it will very likely diffuse globally very rapidly: 2009 H1N1 spread to some 30 countries worldwide in a relatively short period of time leaving more than 800 dead. The continual computer virus attacks on the Internet also illustrate the urgent need for knowledge about modeling, analysis, and control of epidemic dynamics on complex networks. Concerning the advance of techniques, it has become clear that more fundamental knowledge is needed within the context of mathematical and numerical studies on how epidemic dynamical networks can be modeled, analyzed and controlled. The main objective of this book is to present the state-of-the-art and recent progress in the investigation of these important topics and some related issues arising from various epidemic and information systems.

This book covers most emerging topics of epidemic dynamics on complex networks, including models, theories, methods, and global stability analysis. We also extend our discussions to include information propagation dynamics, and address topics such as how information, opinions, and rumors spread in the Internet or social networks. This work has developed from a series of research papers resulting from an on-going collaboration among the three authors and their research groups since 2006.

This is mainly a research monograph and also a textbook that can be used as either a research reference book or for a one-semester introductory course on propagation dynamics and epidemic control on complex networks for upper-division undergraduates and first-year graduates in applied mathematics, engineering, computer science, information science, communication systems, biological and life sciences, applied physics, as well as biomedical and social sciences. It covers most basic topics in the field, and therefore can serve well for self-study of these topics by graduate students and researchers interested in network science and engineering.

Throughout the text we often keep the adjective complex to reflect the historical perspective and to emphasize the nature of the subject, which is in line with

ii PREFACE

the common phrases of complex systems and complex dynamics alike, therefore it should not be seen as redundant.

We would like to take this opportunity to express our gratitude to the editor Ms Ying Liu at China Higher Education Press for her invaluable help and support throughout the writing of this book and the subsequent publication processes. We would also like to thank the editors at Wiley for their timely responses to our book proposal and for all their helpful comments aimed at improving the final product.

We would also like to acknowledge and thank Luonan Chen, Zhen Jin, Xiang Li, Zengrong Liu, Zonghua Liu, Jun-an Lu, Robert MacKay, Chi K. Tse, Binghong Wang, Xiaofan Wang, to mention just a few, and also our research group members, for their kind help and support.

Finally, we would like to thank our postgraduate students for their contributions, helpful discussions and useful suggestions during the writing of this book. Their contributions are too many to be listed individually.

The research was supported jointly by the University Grants Council of Hong Kong (HK UGC GRF PolyU5300/09E and CityU1109/12E), the Australian Research Council Future Fellowship scheme (grant number FT110100896), City University of Hong Kong, the NSFC grant 11072136, the Shanghai University Leading Academic Discipline Project "Complex Systems: Theory, Methods and Technology" (2012–2014) (Project No. A.13-0101-12-004), and a grant of "The First-class Discipline of Universities in Shanghai". The publication of this book was supported by the China National Publishing Fund for Academic Books in Science and Technology.

Summary

This book evolved from a series of research papers by the three authors and their students published since 2006. It covers the emerging topics of propagation dynamics on complex networks, including models, methods, and stability analysis. Throughout history, epidemic diseases have always been a serious threat to mankind's health and life, and ongoing serious virus attacks on the Internet also illustrate the emergent need for knowledge about modeling, analysis, and control in epidemic dynamics on complex networks. For advance of techniques, it has become clear that more fundamental knowledge will be needed in mathematical and numerical context about how epidemic dynamical networks can be modeled, analyzed, and controlled. The aim of this book is to report the progress made in these topics and some related issues of various epidemic systems. The book will first present a brief history of mathematical epidemiology, and epidemic modeling on complex networks. Then different epidemic models on complex networks, such as staged progression models, models with population mobility, or effective contacts, models on weighted networks, or directed networks, discrete epidemic models, stochastic SIRS epidemic models, and so on, will be discussed. Some threshold analyses by the direct method and by using spectral properties are given. Networked models for SARS and H1N1 are established by setting up plausible models for propagation of the SARS virus and avian influenza outbreaks, which provides a reality-check for the otherwise abstract mathematical models of this text, and it is shown that such models do match well the reality of current emerging diseases. Furthermore, various infectivity functions, including constant, piecewise-linear, saturated, and nonlinear cases, are considered. This book also concentrates on the cases for SIS models with an infective medium, the roles of human awareness in epidemic control, adaptive mechanism between dynamics and epidemics. Methods for epidemic control and different immunization strategies are summarized. Global stability analysis for several networked epidemic models is demonstrated. Finally, information transmission on complex networks and some differences between information and epidemic spreading are investigated.

This book covers most basic topics in the field, and therefore can serve well for self-study of the subjects by graduate students and researchers interested in network science and dynamical systems, and related interdisciplinary fields.

Contents

1	Intr	oductio	n	1
	1.1	Motiva	ation and background	1
	1.2	A brie	f history of mathematical epidemiology	2
		1.2.1	Compartmental modeling	3
		1.2.2	Epidemic modeling on complex networks	4
	1.3	Organi	ization of the book	5
	Refe	rences		6
2	Vari	ous epi	demic models on complex networks	10
	2.1	Multip	ole stage models	10
		2.1.1	Multiple susceptible individuals	11
		2.1.2	Multiple infected individuals	12
		2.1.3	Multiple-staged infected individuals	13
	2.2	Staged	l progression models	13
		2.2.1	Simple-staged progression model	14
		2.2.2	Staged progression model on homogenous networks	14
		2.2.3	Staged progression model on heterogenous networks	15
		2.2.4	Staged progression model with birth and death	16
		2.2.5	Staged progression model with birth and death	
			on homogenous networks	16
		2.2.6	Staged progression model with birth and death	
			on heterogenous networks	16
	2.3	Stocha	astic SIS model	17
		2.3.1	A general concept: Epidemic spreading efficiency	18
	2.4	Model	s with population mobility	19
		2.4.1	Epidemic spreading without mobility of individuals	20
		2.4.2	Spreading of epidemic diseases among different cities	20
		2.4.3	Epidemic spreading within and between cities	21
	2.5	Model	s in meta-populations	22

14.190	CONTRENIES
11	CONTENTS

		2.5.1	Model formulation	22
	2.6	Models	with effective contacts	24
		2.6.1	Epidemics with effectively uniform contact	25
		2.6.2	Epidemics with effective contact in homogenous	
			and heterogenous networks	26
	2.7	Models	with two distinct routes	26
	2.8	Models	with competing strains	28
		2.8.1	SIS model with competing strains	28
		2.8.2	Remarks and discussions	30
	2.9	Models	with competing strains and saturated infectivity	3
		2.9.1	SIS model with mutation mechanism	3
		2.9.2	SIS model with super-infection mechanism	33
	2.10	Models	with birth and death of nodes and links	33
			on weighted networks	34
			Model with birth and death and adaptive weights	36
	2.12		on directed networks	38
	2.13	Models	s on colored networks	4(
		2.13.1	SIS epidemic models on colored networks	4
			Microscopic Markov-chain analysis	42
	2.14	Discret	e epidemic models	44
			Discrete SIS model with nonlinear contagion scheme	44
		2.14.2	Discrete-time epidemic model in heterogenous networks	4.5
		2.14.3	A generalized model	40
	Refe	rences		47
3	Enid	emic th	reshold analysis	5.
	3.1		old analysis by the direct method	5.
		3.1.1	The epidemic rate is β/n_i inside the same cities	6.
		3.1.2	Epidemics on homogenous networks	6.
		3.1.3	Epidemics on heterogenous networks	66
	3.2		nic spreading efficiency threshold and epidemic threshold	69
		3.2.1	The case of $\lambda_1 \neq \lambda_2$	7
		3.2.2	The case of $\lambda_1 = \lambda_2$	74
		3.2.3	Epidemic threshold in finite populations	75
		3.2.4	Epidemic threshold in infinite populations	75
	3.3		nic thresholds and basic reproduction numbers	76
		3.3.1	Threshold from a self-consistency equation	7
		3.3.2	Threshold unobtainable from a self-consistency equation	78
		3.3.3	Threshold analysis for SIS model with mutation	80
		3.3.4	Threshold analysis for SIS model with super-infection	8.
		3.3.5	Epidemic thresholds for models on directed networks	80
		3.3.6	Epidemic thresholds on technological and social networks	8
		3.3.7	Epidemic thresholds on directed networks with immunization	89
		3.3.8	Comparisons of epidemic thresholds for directed networks	
			with immunization	9(

			CONTENTS	iii
		3.3.9	Thresholds for colored network models	93
			Thresholds for discrete epidemic models	96
		3.3.11	Basic reproduction number and existence of a	
		5.5.11	positive equilibrium	97
	Refe	rences	positive equinorium	98
	ICIC	renees		
4	Netv	vorked	models for SARS and avian influenza	101
	4.1		rk models of real diseases	101
	4.2	Plausit	ole models for propagation of the SARS virus	102
	4.3		ring model for SARS transmission: Application to epidemic	
			l and risk assessment	108
	4.4		world and scale-free models for SARS transmission	114
	4.5		spreaders and the rate of transmission	118
	4.6		free distribution of avian influenza outbreaks	124
	4.7		ed model of ordinary influenza	130
		rences	ed model of ordinary mindenza	136
	recre	Terrees	ÿ.	DIRE IN
5	Infe	ctivity f	functions	139
	5.1		lel with nontrivial infectivity function	140
		5.1.1	Epidemic threshold for SIS model with piecewise-linear	
			infectivity	141
		5.1.2	Piecewise smooth and nonlinear infectivity	142
	5.2		ted infectivity	143
	5.3		near infectivity for SIS model on scale-free networks	143
	0.0	5.3.1	The epidemic threshold for SIS model on scale-free	
		5.5.1	networks with nonlinear infectivity	144
		5.3.2	Discussions and remarks	148
	Refe	rences	Discussions and Terrario	148
	rere	Teffees		
6	SIS	models	with an infective medium	150
	6.1		odel with an infective medium	150
		6.1.1	Homogenous complex networks	151
		6.1.2	Scale-free networks: The Barabási–Albert model	152
		6.1.3	Uniform immunization strategy	156
		6.1.4	Optimized immunization strategies	157
	6.2		lified SIS model with an infective medium	159
	0.2	6.2.1	The modified model	159
		6.2.2	Epidemic threshold for the modified model with an	
		0.2.2	infective medium	160
	6.3	Enider	mic models with vectors between two separated networks	162
	0.5	6.3.1	Model formulation	162
		6.3.2	Basic reproduction number	164
		6.3.3	Sensitivity analysis	166
	6.4		mic transmission on interdependent networks	167
	0.4	6.4.1	Theoretical modeling	168

iv	(CONTEN	ITS	
		6.4.2 6.4.3	Mathematical analysis of epidemic dynamics Numerical analysis: Effect of model parameters on the	172
		0.4.5	basic reproduction number	174
		6.4.4	Numerical analysis: Effect of model parameters on	
		0	infected node densities	177
	6.5	Discus	sions and remarks	179
		rences	3.0.10	181
7	Epid	lemic co	ontrol and awareness	184
	7.1		odel with awareness	184
		7.1.1	Background	185
		7.1.2	The model	186
		7.1.3	Epidemic threshold	190
		7.1.4	Conclusions and discussions	191
	7.2	Discret	te-time SIS model with awareness	192
		7.2.1	SIS model with awareness interactions	193
		7.2.2	Theoretical analysis: Basic reproduction number	195
		7.2.3	Remarks and discussions	197
	7.3	Spread	ling dynamics of a disease-awareness SIS model on complex	
		networ		198
		7.3.1	Model formulation	198
		7.3.2	Derivation of limiting systems	200
		7.3.3	Basic reproduction number and local stability	201
	7.4	Remar	ks and discussions	201
	Refe	erences		203
8	Ada	ptive m	echanism between dynamics and epidemics	207
	8.1		ive mechanism between dynamical synchronization and	
		epiden	nic behavior on complex networks	207
		8.1.1	Models of complex dynamical network and epidemic	
			network	209
		8.1.2	Models of epidemic synchronization and its analysis	210
		8.1.3		212
		8.1.4	Global stability of epidemic synchronization	214
	8.2	Interpl	lay between collective behavior and spreading dynamics	216
		8.2.1	A general bidirectional model	217
		8.2.2	Global synchronization and spreading dynamics	218
		8.2.3	Stability of global synchronization and spreading dynamics	220
		8.2.4	Phase synchronization and spreading dynamics	226
		8.2.5	Control of spreading networks	227
		8.2.6	Discussions and remarks	227
	Refe	erences		228
9	Epi		ontrol and immunization	231
	9.1	SIS m	odel with immunization	231

				CONTENTS	V
		9.1.1	Proportional immunization		231
		9.1.2	Targeted immunization		232
		9.1.3	Acquaintance immunization		233
		9.1.4	Active immunization		234
	9.2	Edge ta	argeted strategy for controlling epidemic sprea-	ding on	
		scale-fi	ree networks	O	235
	9.3	Remarl	ks and discussions		237
	Refe	erences			239
10	Glol	hal stahi	lity analysis		240
			stability analysis of the modified model with a	ın.	240
	10.1		e medium	.11	240
	10.2		dynamics of the model with vectors between t	WO	270
			ed networks	WO	241
			Global stability of the disease-free equilibrium	n and	211
			existence of the endemic equilibrium	ii diid	243
		10.2.2	Uniqueness and global attractivity of the ende	emic	
			equilibrium		245
	10.3	Global	behavior of disease transmission on interdeper	ndent	
		network			247
		10.3.1	Existence and global stability of the endemic	equilibrium	
			for a disease-awareness SIS model	-	248
	10.4	Global	behavior of epidemic transmissions		250
			Stability of the model equilibria		250
		10.4.2	Stability analysis for discrete epidemic model	S	252
			Global stability of the disease-free equilibrium	n	256
			Global attractiveness of epidemic disease		257
	10.5		attractivity of a network-based epidemic SIS n	nodel	260
			Positiveness, boundedness and equilibria		260
			Global attractivity of the model		262
			Remarks and discussions		263
	10.6		stability of an epidemic model with birth an	d death and	
			e weights		264
			Global dynamics of the model		264
	10.5		Discussions and remarks		266
	10.7		dynamics of a generalized epidemic model		268
			Model formulation		268
			Global dynamics of the model		270
	D C		Discussions and remarks		273
	Kete	rences			274
11	Infor	mation	diffusion and pathogen propagation		277
			tion diffusion and propagation on complex net	works	277
		11.1.1	Information diffusion on complex networks		278

	CONTENTS
V1	CONTENIO

	11.1.2 Some essential differences between information	
	propagation and epidemic spreading	280
11.2	Interplay between information of disease spreading and	
	epidemic dynamics	281
	11.2.1 Preliminaries	281
	11.2.2 Theoretical analysis of the model	282
11.3	Discussions and remarks	284
Refe	rences	286
		289
	ix A Proofs of theorems	209
A.1	Transition from discrete-time linear system to continuous-time	200
	linear system	289
A.2	Proof of Lemma 6.1	291
A.3	Proof of Theorem 10.4	291
A.4	Proof of Theorem 10.3	292
A.5	Proof of Theorem 10.42	296
Append	ix B Further proofs of results	302
B.1	Eigenvalues of the matrix \tilde{F} in (6.27)	302
B.2	The matrix Γ in (6.32)	304
B.3	Proof of (7.6) in Chapter 7	305
B.4	The positiveness of σ' : proof of $\sigma' > 0$ in Section 9.1.2	306
B.5	The relation between Λ and κ in Section 9.1.3	308
Inde	ov.	311

Introduction

In this chapter we provide a brief introduction to the remainder of the book.

The uninitiated may require a broader background to the topic of complex networks. Rather than overburden out current presentation, we refer interested readers to some good introductory books and papers [1-14] for more background information on complex networks and network science.

1.1 Motivation and background

Throughout history, infectious diseases have always been a serious threat to human health and life. It is therefore of great practical significance to study epidemic transmission and then to take effective measures to prevent and control them. Toward this end, much research has fallen within the field of epidemiology, which uses mathematical modeling as an analytical approach. Traditionally, epidemic models were based on uniformly mixing populations, which are unable to characterize epidemic propagation in large-scale social contact networks with disparate heterogeneity. However, the fact that most population-based epidemics spread through physical interactions raises contact networks as a basic tool for mathematical description of contagion dynamics. In the last decade, spurred by the availability of real data and the maturation of network theory, there has been a burst of research on network-based epidemic transmission [15–26].

Beyond ordinary infection diseases, recurring computer virus attacks (as well as computer worms and other malware vectors) on the Internet also illustrate the urgent need for knowledge about modeling, analysis and control of epidemic dynamics on complex networks.

The World Health Organization (WHO) announced in 2012 [27] that some time in the next couple of years Guinea worm will become only the second known

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