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Takeo Oku

SOLAR CELLS AND ENERGY MATERIALS

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Solar Cells and Energy Materials

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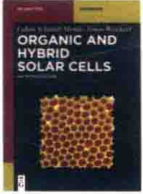
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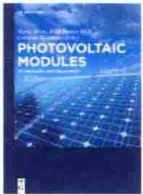


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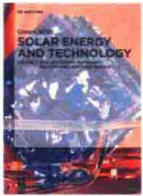


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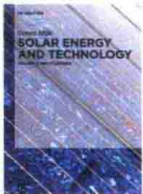


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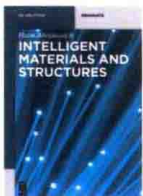


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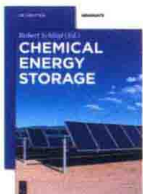
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Preface

“Let there be light”. These words appear at the beginning of Genesis in the Old Testament. Advanced cosmological science has likewise shown that the universe started from a Big Bang 13.7 billion years ago. Light is an elemental root of our universe. The “flow of time” that we feel in what we perceive to be the present is an effect of the close relationship between light and matter, and time does not flow by itself. Quantum teleportation utilizing the connected spins of quantum particles at a distance results from principles that still remain unknown to contemporary scientists. Light has also not yet been entirely clarified by the advances of contemporary science, and several aspects of it remain unexplained.

On the other hand, light is essential to our everyday life in contemporary society. Light contains energy and information simultaneously, and most new electronic apparatuses, such as mobile phones, laptop computers, DVD players or satellite communications, function in ways closely connected to light.

After the big earthquake in Japan in 2011, all nuclear reactors in Japan were stopped, and some of them had already been closed previously. Saving electricity is promoted both in both industries and ordinary homes, and the world’s energy problem has become a very familiar one in our everyday lives. Although Japan’s energy self-sufficiency was 58 % in 1960, it had been significantly reduced to only 4 % by 2014. In other words, 96 % of the energy used in Japan depends on the import of materials such as oil, coal, liquefied natural gas and uranium, a fact that suggests improvements are needed to the current imbalance in supply and demand. Energy problems resulting from dependence on fossil fuels, which are limited energy resources, will soon be an inescapable issue all over the world. The author would be very pleased if the present book is helpful in solving future energy problems.

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November 2016, Takeo Oku

Table for physical constants

Physical constants	Symbol	Values	SI units
Velocity of light	c	2.99792458	10^8 m s^{-1}
Planck constant	h	6.62607	10^{-34} J s
Dirac constant	$\hbar = h/2\pi$	1.05457	10^{-34} J s
Gravitational constant	G	6.67384	$10^{-11} \text{ m}^3 \text{ s}^{-2} \text{ kg}^{-1}$
Electron charge	e	1.60218	10^{-19} A s (C)
Electron mass	m_e, m_0	9.10938	10^{-31} kg
e Proton mass	m_p	1.67262	10^{-27} kg
Neutron mass	m_n	1.67493	10^{-27} kg
Electron energy	$m_e c^2$	0.5110	MeV
Compton wavelength	λ_c	2.4263	10^{-12} m
Boltzmann constant	k, k_B	1.38065	$10^{-23} \text{ J K}^{-1}$
Magnetic permeability	$\mu_0 = 4\pi \times 10^{-7}$	1.25664	$10^{-6} \text{ H m}^{-1} (\text{N A}^{-2})$
Dielectric constant	$\epsilon_0 = 1/\mu_0 c^2$	8.85419	$10^{-12} \text{ F m}^{-1} (\text{N V}^{-2})$
Avogadro constant	N_A	6.02214	10^{23} mol^{-1}
Gas constant	$R = k N_A$	8.31446	$\text{J K}^{-1} \text{ mol}^{-1}$

Physical constants	Symbol	Values and units
Ångström	Å	$0.1 \text{ nm} = 10^{-10} \text{ m}$
Electron volt	eV	$1.60218 \times 10^{-19} \text{ J}$
Wavelength of 1 eV photon	λ	1239.84 nm
Standard atmosphere	atm	$1.01325 \times 10^5 \text{ Pa}$

Periodic table

1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18
1H Hydrogen 1.008																	2He Helium 4.003
3Li Lithium 6.941	4Be Beryllium 9.012											5B Boron 10.81	6C Carbon 12.01	7N Nitrogen 14.01	8O Oxygen 16.00	9F Fluorine 19.00	10Ne Neon 20.18
11Na Sodium 22.99	12Mg Magnesium 24.31											13Al Aluminium 26.98	14Si Silicon 28.09	15P Phosphorus 30.97	16S Sulfur 32.07	17Cl Chlorine 35.45	18Ar Argon 39.95
19K Potassium 39.10	20Ca Calcium 40.08	21Sc Scandium 44.96	22Ti Titanium 47.87	23V Vanadium 50.94	24Cr Chromium 52.00	25Mn Manganese 54.94	26Fe Iron 55.85	27Co Cobalt 58.93	28Ni Nickel 58.69	29Cu Copper 63.55	30Zn Zinc 65.41	31Ga Gallium 69.72	32Ge Germanium 72.64	33As Arsenic 74.92	34Se Selenium 78.96	35Br Bromine 79.90	36Kr Krypton 83.80
37Rb Rubidium 85.47	38Sr Strontium 87.62	39Y Yttrium 88.91	40Zr Zirconium 91.22	41Nb Niobium 92.91	42Mo Molybdenum 95.94	43Tc Technetium (99)	44Ru Ruthenium 101.1	45Rh Rhodium 102.9	46Pd Palladium 106.4	47Ag Silver 107.9	48Cd Cadmium 112.4	49In Indium 114.8	50Sn Tin 118.7	51Sb Antimony 121.8	52Te Tellurium 127.6	53I Iodine 126.9	54Xe Xenon 131.3
55Cs Caesium 132.9	56Ba Barium 137.3	57-71 Lanthanum ♦	72Hf Hafnium 178.5	73Ta Tantalum 180.9	74W Tungsten 183.8	75Re Rhenium 186.2	76Os Osmium 190.2	77Ir Iridium 192.2	78Pt Platinum 195.1	79Au Gold 197.0	80Hg Mercury 200.6	81Tl Thallium 204.4	82Pb Lead 207.2	83Bi Bismuth 209.0	84Po Polonium (210)	85At Astatine (210)	86Rn Radon (222)
87Fr Francium (223)	88Ra Radium (226)	89-103 Lawrencium ♦♦	104Rf Rutherfordium (267)	105Db Dubnium (268)	106Sg Seaborgium (271)	107Bh Bohrium (272)	108Hs Hassium (277)	109Mt Meitnerium (276)	110Ds Darmstadtium (281)	111Rg Roentgenium (280)	112Cn Copernicium (285)	113Nh Nihonium (284)	114Fl Flerovium (289)	115Mc Moscovium (288)	116Lv Livermorium (293)	117Ts Tennessine (294)	118Og Oganesson (294)

Symbol for element
Element

Atomic mass (u)

♦	57La Lanthanum 138.9	58Ce Cerium 140.1	59Pr Praseodymium 140.9	60Nd Neodymium 144.2	61Pm Promethium (145)	62Sm Samarium 150.4	63Eu Europium 152.0	64Gd Gadolinium 157.3	65Tb Terbium 158.9	66Dy Dysprosium 162.5	67Ho Holmium 164.9	68Er Erbium 167.3	69Tm Thulium 168.9	70Yb Ytterbium 173.0	71Lu Lutetium 175.0
♦♦	89Ac Actinium (227)	90Th Thorium 232.0	91Pa Protactinium 231.0	92U Uranium 238.0	93Np Neptunium (237)	94Pu Plutonium (239)	95Am Americium (243)	96Cm Curium (247)	97Bk Berkelium (247)	98Cf Californium (252)	99Es Einsteinium (252)	100Fm Fermium (257)	101Md Mendelevium (258)	102No Nobelium (259)	103Lr Lawrencium (262)

Alkali metal	Alkaline earth metal	Lanthanide	Actinide	Transition metal	Post-transition metal	Metalloid		Nonmetal		Unknown chemical properties
						Polyatomic nonmetal	Diatomic nonmetal	Noble gas		

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1 Energy

1.1 What is energy?

The word “energy” can have the following meanings:

1. The capacity for work that a certain system potentially has.
2. The ability to do physical work.
3. A useful resource for human society.
4. A resource required for physical or mental activity.

In the field of physics, energy generally refers to a quantity of work, as in definition (1). Heat, light, electromagnetic waves, and mass are also forms of energy. Within general usage, definitions (2) and (3) are more commonly used. There are many types of energy resources, and exhaustive energy and renewable energy have often been compared. Recently, a transition from exhaustive energy to renewable energy has begun taking place across the world.

The measurement used for energy in the International System of Units (SI unit) is the joule (J). The electron volt (eV) and kilowatt hour (kWh) are also used in the field of solar cells, as is shown in Table 1.1.

Table 1.1: Unit of energy.

Item	Symbol of quantity
Energy	E
Dimension	$\text{kg m}^2 \text{s}^{-2}$
Kind	scalar
SI unit	J (Joule)
CGS unit	$\text{erg} = 10^{-7} \text{ J}$
MKS system of units	kgf m
Planck unit	Planck energy $E_p = 1.956 \times 10^9 \text{ J}$
Atomic unit	Hartree $E_h = 4.360 \times 10^{-18} \text{ J}$
Kilo watt hour (kWh)	3.6 MJ
Electron volt (eV)	$1.602 \times 10^{-19} \text{ J}$

There are many types of energy, including: physical energy, kinetic energy, potential energy, elastic energy, chemical energy, ionization energy, heat energy, light energy, electric energy, acoustic energy, nuclear energy, mass energy and dark energy. Resources that are useful for industry, transportation and human life are generally referred to as “energy resources”, which include oil, coal, natural gas, nuclear power energy, water power, solar heat and so on. Recently, a distinction has been made between energy resources that are exhaustive forms of energy and those that are re-

newable. A development towards the increased use of renewable energy sources is currently in progress.

1.2 Fermions and bosons

An atom consists of a nucleus with positive charge and electrons with negative charge. The nucleus consists of protons with positive charge and electrically neutral neutrons. An electron is believed to be an elementary particle, and measures less than 10^{-18} m in diameter. Elementary particle is a general term for particles that cannot be further divided. Electrons do not orbit around the nucleus in the usual sense of the word, even though textbook figures often illustrate them as if they did. Electron clouds are stochastically distributed around the nucleus, which contributes to the size of the atom (diameter: ~ 0.2 nm). Electron clouds also exist like waves, which can be observed as a particle when measured. However, it is difficult to define the size of electron clouds. When atoms connect through chemical bonding to form molecules, or they are ionized, the size of atomic clouds change naturally and the size of atoms also becomes different.

The nucleus consists of protons and neutrons, and measures $\sim 10^{-15}$ m (1 fm) in diameter. Mesons transmit the force of protons at a minute scale. According to the standard model, protons and neutrons consist of up and down quarks, and there are six types of quarks with three stages of generation in nature.

An electron is one of the six particles referred to as leptons. A proton consists of two up quarks and one down quark, and a neutron consists of one up quark and two down quarks, as shown in Fig. 1.1. These quarks are believed to be elementary particles at present, though superstring theory has also been proposed as a further

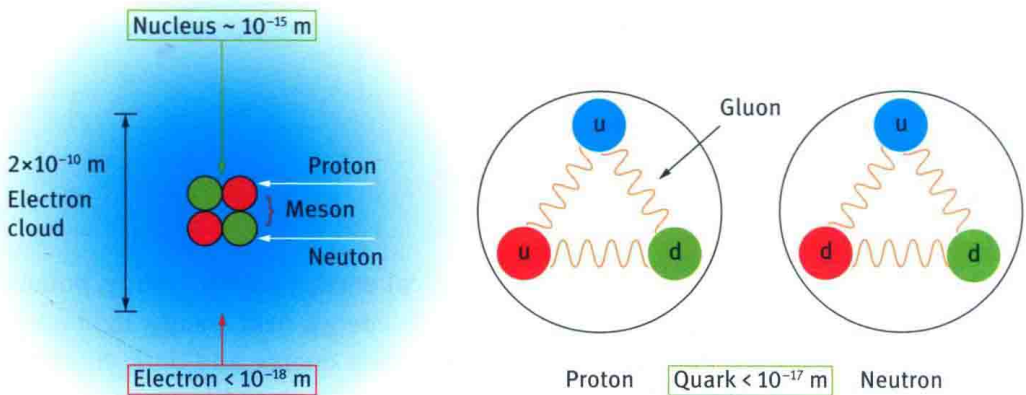


Fig. 1.1: Structure of atom, proton and neutron.

theory. Superstring theory indicates that elementary particles are a certain kind of string, and that quarks and leptons can be formed by the vibration of the strings. This theory is also called the quantum theory of gravity because of its inclusion of gravity.

Fermions are quantum particles with a spin angular momentum of half-integers such as $1/2$, $3/2$ and $5/2$, as listed in Table 1.2. Fermions are guided by the Pauli Exclusion Principle, which indicates that two particles cannot occupy the same quantum state. Fermi-Dirac statistics apply to identical particles with half-integer spins in a system with thermodynamic equilibrium. The particles classified as fermions are quarks and leptons such as electrons, muons and neutrinos.

Table 1.2: Fermions and bosons.

Fermions	First generation			Second generation			Third generation		
	Charge / Spin / Mass			Charge / Spin / Mass			Charge / Spin / Mass		
Quarks	Up u			Charm c			Top t		
	+2/3	+1/2	~ 2.3 MeV	+2/3	+1/2	~ 1.3 GeV	+2/3	+1/2	~ 173 GeV
	Down d			Strange s			Bottom b		
	-1/3	+1/2	~ 4.8 MeV	-1/3	+1/2	~ 95 MeV	-1/3	+1/2	~ 4.2 GeV
Leptons	Electron e^-			Muon μ^-			Tau τ^-		
	-1	+1/2	0.511 MeV	-1	+1/2	106 MeV	-1	+1/2	1.78 GeV
	Electron neutrino ν_e			Muon neutrino ν_μ			Tau neutrino ν_τ		
	0	+1/2	< 2.2 eV	0	+1/2	< 170 keV	0	+1/2	< 16 MeV

Bosons	Force	Charge	Spin	Mass
Photon γ	Electromagnetic	0	1	0
Z boson Z^0	Weak	0	1	91.2 GeV
W boson W^\pm	Weak	± 1	1	80.4 GeV
Gluon g	Strong	0	1	0
Gaviton G	Gravty	0	2	0
Higgs boson H	Mass	0	0	126 GeV

On the other hand, bosons are quantum particles with an integer spin angular momentum, as listed in Table 1.2. A photon is a particle with a spin of 1. Bosons can occupy the same quantum state even in the case of more than one particle in one system. Bose-Einstein statistics apply to identical particles with an integer spin in systems with thermodynamic equilibrium. Examples of bosons include gauge particles, which carry the forces of elementary particles, such as photons, weak bosons and gluons. A graviton is an undiscovered boson with a spin of 2. A Higgs boson, which causes mass

in elementary particles is a boson with a spin of 0. Cooper pairs, which are related to the phenomenon of superconductivity, obey Bose-Einstein statistics.

Neutrino is a general name for electrically neutral leptons, and neutrinos come in three flavors: electron neutrinos, muon neutrinos and tau neutrinos, associated with the electron, muon and tau, respectively. Although several quadrillion neutrinos pass through the human body each second, nobody feels them as they pass. Neutrinos almost never interact with matter, and it is quite difficult to observe them.

1.3 Important physical constants in the universe

The most important physical constants in our universe are the following:

- Velocity of light c ($3.00 \times 10^8 \text{ m s}^{-1}$)
- Planck constant h ($6.63 \times 10^{-34} \text{ J s}$)
- Gravitational constant G ($6.67 \times 10^{-11} \text{ m}^3 \text{ S}^{-2} \text{ kg}^{-1}$)

The Planck constant is a universal constant at the quantum scale. The energy of light (E) is proportional to the frequency (ν) of light, and the proportionality constant is a Planck constant.

$$E = h\nu \quad (1.1)$$

The velocity of light and the gravitational constant are large-scale constants valid across the universe, while the Planck constant is a constant at an extremely small scale.

1.4 Four fundamental forces of nature

- Gravity: The universal gravitation (F) between m_1 and m_2 at a distance of r is expressed as follows:

$$F = G \frac{m_1 m_2}{r^2} \quad (1.2)$$

Although gravitation interacts at a distance in a similar way to the electromagnetic force, gravitational force is very weak. Stars with high mass density attract and confine light, and can potentially form black holes.

- Electromagnetic force: The electrostatic force (F) between q_1 and q_2 with a distance of r is expressed by Coulomb's law as follows:

$$F = \frac{1}{4\pi\epsilon_0} \frac{q_1 q_2}{r^2} \quad (1.3)$$

ϵ_0 is a dielectric constant of a vacuum. Magnetic force functions similarly, and gravitational and electromagnetic forces depend on r^2 . Various forms of energies central to life depend on the electromagnetic force, such as chemical reactions or bioenergy.

- Weak force: The weak force found by Fermi works at the elementary particle scale (10^{-18} m) and causes radioactive decay such as beta decay, in which a beta-ray (an electron) and an associated neutrino are emitted from an atomic nucleus.
- Strong force: The strong force is about 100 times stronger than electromagnetic force according to the theory of nucleus force and mesons. The interaction range of the strong force extends to about the size of nucleus (10^{-15} m) and its potential is expressed as follows:

$$U(r) \sim -\frac{g^2}{4\pi} \frac{e^{-r/\lambda}}{r} \quad (1.4)$$

Where m is the mass of a meson, a particle has a Compton wavelength ($\lambda = h/mc$), and $g^2/4\pi$ is a bonding constant. As expressed by the exponential $e^{-r/\lambda}$, the force only acts at a close distance and other repulsive forces also act around the center of the nucleus.

These are the four forces that exist in the universe and their interaction ranges are different, as listed in Table 1.3. The forces interact through the distortion of fields and the exchange of particles. Gravitational and electromagnetic forces act over an infinite range. These four forces can be used in various ways as energy resources.

Table 1.3: The four fundamental forces as gauge bosons.

Particles mediating	Photon γ	Weak boson W, Z	Gluon g	Graviton G
Transmission force	Electromagnetic force	Weak force	Strong force	Gravitation
Strength scale ratio	10^{-2}	10^{-5}	1	10^{-40}
Spin	1	1	1	2
Mass	0	80, 91GeV	0	0
Acts on	Electric charge	Flavor	Color charge	Mass, energy
Functional ranges	Infinite	10^{-18} m	10^{-15} m	Infinite
Functional places	Atoms and molecules	Inside of nucleus	Inside of nucleus	Universal space
Energy source	Fossil fuels	Geothermal energy	Sun, nuclear energy	Hydropower, tide power