

Basic Structures

3rd Edition

Philip Garrison

BSc, MBA, CEng, MICE, MIStructE, MCIHT School of the Built Environment and Engineering Leeds Beckett University

WILEY Blackwell

This edition first published 2016 © John Wiley & Sons, Ltd

First edition published 2005 Second edition published 2011 Third edition published 2016

Registered Office

John Wiley & Sons, Ltd, The Atrium, Southern Gate, Chichester, West Sussex, PO19 8SQ, United Kingdom.

Editorial Offices

9600 Garsington Road, Oxford, OX4 2DQ, United Kingdom. The Atrium, Southern Gate, Chichester, West Sussex, PO19 8SQ, United Kingdom.

For details of our global editorial offices, for customer services and for information about how to apply for permission to reuse the copyright material in this book please see our website at www.wiley.com/wiley-blackwell.

The right of the author to be identified as the author of this work has been asserted in accordance with the UK Copyright, Designs and Patents Act 1988.

All rights reserved. No part of this publication may be reproduced, stored in a retrieval system, or transmitted, in any form or by any means, electronic, mechanical, photocopying, recording or otherwise, except as permitted by the UK Copyright, Designs and Patents Act 1988, without the prior permission of the publisher.

Designations used by companies to distinguish their products are often claimed as trademarks. All brand names and product names used in this book are trade names, service marks, trademarks or registered trademarks of their respective owners. The publisher is not associated with any product or vendor mentioned in this book.

Limit of Liability/Disclaimer of Warranty: While the publisher and author(s) have used their best efforts in preparing this book, they make no representations or warranties with respect to the accuracy or completeness of the contents of this book and specifically disclaim any implied warranties of merchantability or fitness for a particular purpose. It is sold on the understanding that the publisher is not engaged in rendering professional services and neither the publisher nor the author shall be liable for damages arising herefrom. If professional advice or other expert assistance is required, the services of a competent professional should be sought.

Library of Congress Cataloging-in-Publication data applied for

ISBN: 9781118950876

A catalogue record for this book is available from the British Library.

Wiley also publishes its books in a variety of electronic formats. Some content that appears in print may not be available in electronic books.

Set in 9.5/11.5pt Minion by SPi Global, Pondicherry, India Printed and bound in Malaysia by Vivar Printing Sdn Bhd

1 2016

Acknowledgements

Writing a book is largely an individual, and rather solitary, effort. Every photograph in this book was taken by me, every diagram was drawn by me, and every word of text was written by me. However, there have been many who have helped me on the way, including past and present colleagues and family members. My thanks go particularly to the following:

- Katie Bartozzi, Amanda Brown, Andrew Brown, Simon Garrison, Pete Gordon, Paul Hirst and the late Phil Yates.
- Julia Burden and Paul Sayer of Blackwell Publishing.
- My wife Jenny my greatest fan and my fondest critic.
- Nick Crinson, whose encyclopedic knowledge of the London Underground inspired the analogy given in Chapter 7, and his wife Maxine, who drew my attention to a discussion of bridge types in a work of popular fiction!
- Colleagues Matt Peat and Dave Roberts who diligently read the first edition of this book and pointed out the several errors that I, the reviewers and proofreaders had all overlooked.
- Brian Walker, who patiently and with great humour taught mathematics to me and my fellow adolescents at Aberdeen Grammar School back in the early 1970s. (If you ever read this Brian do get in touch. Chapter 27 is down to you.)
- Last but not least Jim Adams, without his inspiration there would have been no book.

And, to parrot that hackneyed catch-all used by all authors at this point, my thanks go to all the others I haven't mentioned, without whom, etc. – they know who they are!

Last but not least, my thanks go to you, the reader, for buying this book. I understand that textbooks are expensive and student resources are stretched to the limit, so thank you for your faith in me and I trust you will not be disappointed.

And thanks to those who bought the previous editions of the book. In the 11 years since this book first appeared I've received countless emails from readers all over the world. It is always gratifying to hear that I've managed to help a complete stranger who I almost certainly will never meet. Keep them coming!

Introduction

When I was 16 years I had a Saturday job as a shelf-stacker at a local supermarket. One day, during a tea break, a co-worker asked me what I did the rest of the week. I explained that I had just done O levels and was going on to do A levels. I told him how many and in which subjects. He then asked me about my career aspirations (not his exact words). I explained that I wanted to become an engineer. His aghast response was: 'What! With all those qualifications?'

Engineers suffer from a lack of public perception of what their profession entails – many people think we spend our days in the suburbs, mending washing machines and televisions. Architects are more fortunate in this respect – the public have a better grasp of their profession: 'They design buildings, don't they?'

Public perceptions aside, careers in both civil engineering and architecture can be extremely rewarding. There are few other careers where individuals can be truly creative, often on a massive scale. The civil engineering profession offers a variety of working environments and a large number of specialisms within civil engineering. Civil engineers have opportunities to work all over the world, on projects large and small, and could come into contact with a wide variety of people, from the lowest worker on a construction site to government officials and heads of state.

In the 21st century there is a huge demand for civil engineers and many young people (and some not so young!) are realising that this is a profession well worth entering.

Traditionally, students embarking on university courses in civil engineering would have A levels in subjects such as mathematics, physics and chemistry. However, for a variety of reasons, many of today's potential students have A levels (or similar) in non-numerate and non-scientific subjects. Moreover, a sizeable number of 'mature' people are entering the profession following a first career in something completely different. As a university admissions tutor, I speak to such people everyday. It is possible, depending on the specialism eventually chosen, to enjoy a successful career in civil engineering without an in-depth mathematical knowledge. However, it is extremely difficult to obtain a degree or Higher National Diploma (HND) in civil engineering without some mathematical proficiency.

Turning to architects – these are creative people! Every building they design has a structure, without which the building would not stand up. Architects, like civil engineers, have to understand the mechanisms which lead to successful structures.

This book is about Structures. Structures is a subject studied as part of all civil engineering degree, HND and Ordinary National Diploma (OND) courses, as well as architecture degree courses, and also on some degree courses in related subjects (e.g. quantity surveying, building surveying, construction management and architecture).

The purpose of this book

I have taught structures to undergraduate civil engineers and architects since 1992. During that time I have noticed that many students find the basic concept of structures difficult to grasp and apply.

This book aims to do the following:

- to explain structural concepts clearly, using analogies and examples to illustrate the points
- to express the mathematical aspects of the subject in a straightforward manner that can be understood by mathematically weak students and placed in context with the concepts involved
- to maintain reader interest by incorporating into the text real-life examples and case histories to underline the relevance of the material that the student is learning.

This book presumes no previous knowledge of structures on the part of the reader. It does, however, presume that the reader has a good general education and a mathematical ability up to at least GCSE standard.

The intended readership

This book is aimed at:

- Ordinary National Certificate (ONC), Ordinary National Diploma (OND), Higher National Certificate (HNC), Higher National Diploma (HND) or first-year degree (BSc, BEng or MEng) students on a civil engineering (or similar) course, who will study a module called structures, structural mechanics, mechanics or structural analysis
- students on a BA degree course in architecture.

The following will also find this book useful:

- students on courses in subjects related to civil engineering and architecture e.g. quantity surveying, building surveying, construction management or architectural technology – who have to do a structures module as part of their studies
- those studying technology at GCE A level, GNVQ or similar
- people working in the construction industry in any capacity.

The following will find the book a useful revision tool:

- a second (or subsequent)-year student on a civil engineering or architecture degree
- a professional in the civil engineering or building industry, and practising architects.

A word about computers

Computer packages are available for every specialism, and structural engineering is no exception. Certainly, some of the problems in this book could be solved more quickly using computer software. However, I do not mention specific computer packages in this book and where I mention computers at all, it is in general terms. There are two reasons for this.

- The purpose of this book is to acquaint the reader with the basic principles of structures.
 Whereas a computer is a useful tool for solving specific problems, it is no substitute for a thorough grounding in the basics of the subject.
- 2) Computer software is being improved and updated all the time. The most popular and up-to-date computer package for structural engineering as I write these words may be dated (at best) or obsolete (at worst) by the time you read this. If you are interested in the

latest software, look at specialist computer magazines or articles and advertisements in the civil and structural engineering and architecture press, or if you are a student, consult your lecturers.

I have set my students assignments where they have to solve a structural problem by hand then check their results by analysing the same problem using appropriate computer software. If the answers obtained by the two approaches differ, it is always instructive to find out whether the error is in the student's hand calculations (most frequently the case) or in the computer analysis (occurs less frequently, but does happen sometimes when the student has input incorrect or incomplete data – the old 'rubbish in, rubbish out'!).

The website

You will find worked solutions to some of the problems in this book at a website maintained by the publishers: www.blackwellpublishing.com/garrison. In addition, all readers can contact me via the website – your suggestions, comments and criticisms are welcome.

An overview of this book

If you are a student studying a module called structures, structural mechanics or similar, the chapter headings in this book will tie in – more or less – with the lecture topics presented by your lecturer or tutor. I suggest that you read each chapter of this book soon after the relevant lecture or class to reinforce your knowledge and skills in the topic concerned. I advise all readers to have a pen and paper beside them to jot down notes as they go through the book – particularly the numerical examples. In my experience, this greatly aids understanding.

- Chapters 1–5 introduce the fundamental concepts, terms and language of structures.
- Chapters 6–10 build on the basic concepts and show how they can be used, mathematically, to solve simple structural problems.
- Chapter 11 deals with the very important concept of stability and discusses how to ensure structures are stable – and recognise when they're not!
- Chapters 12–15 deal with the analysis of pin-jointed frames, a topic that some students find difficult.
- Chapter 16 covers shear force and bending moment diagrams an extremely important topic.
- Chapters 17–20 deal with stress in its various guises.
- Structural materials are dealt with more fully in other texts, but Chapter 21 provides an
 introduction to this topic.
- Chapter 22 has more on materials, and a word on design standards.
- Chapters 23 and 24 deal, respectively, with the conceptual design of structures and the calculation of loads.
- Chapter 25 is a descriptive introduction to structural design, which should be read before embarking on a structural design module.
- Chapter 26 discusses more unusual types of structures.
- Chapter 27 deals with deflection, and outlines a method whereby deflections can be calculated.
- Chapters 28–34 serve as an easy introduction to several slightly harder topics that students will encounter on the second or third year of a civil engineering degree course.

How to use this book

It is not necessary for all readers to read this book from cover to cover. However, the book has been designed to follow the subject matter in the order usually adopted by teachers and lecturers teaching structures to students on degree and HND courses in civil engineering. If you are a student on such a course, I suggest that you read the book in stages in parallel with your lectures.

- All readers should read Chapters 1–5 as these lay down the fundamentals of the subject.
- Civil engineering students should read all chapters in the book, with the possible exception of Chapters 14 and 15 if these topics are not taught on your course.
- Students of architecture should concentrate on Chapters 1–9, 21–24 and 26, but read certain other chapters as directed by your tutor.
- If you're studying civil engineering and want to know how to get more out of the profession whilst you are a student, see Appendix 6 for inspiration.

Let's keep it simple

James Dyson, the inventor of the dual cyclone vacuum cleaner that bears his name, discusses one of its design features – the transparent plastic cylinder within which the rubbish collects – in his autobiography:

A journalist who came to interview me once asked, 'The area where the dirt collects is transparent, thus parading all our detritus on the outside, and turning the classic design inside out. Is this some post-modernist nod to the architectural style pioneered by Richard Rodgers at the Pompidou Centre, where the air-conditioning and escalators, the very guts, are made into a self-referential design feature?

'No,' I replied. 'It's so you can see when it's full.'

(From Against the Odds by James Dyson and Giles Coren (Texere 2001))

It is my aim to keep this book as simple, straightforward and jargon-free as possible.

Worked solutions to the tutorial questions can be found at www.wiley.com/go/garrison/basicstructures

Contents

	ntroduction		X
1	What is structural engineering?		1
2	Learn the language: a simple explanation of terms used by structural engineers		8
3	How do structures (and parts of structures) behave?	1	1
4	Force, mass and weight	20	5
5	Loading – dead or alive	32	2
6	Equilibrium - a balanced approach	38	
7	More about forces: resultants and components	43	3
8	Moments	54	1
9	Reactions	6	7
0	Different types of support - and what's a pin?	73	3
11	A few words about stability	8	l
12	Introduction to the analysis of pin-jointed frames	93	3
13	Method of resolution at joints	98	3
4	Method of sections	119)
15	Graphical method	127	7
16	Shear force and bending moments	137	7
17	This thing called stress	168	3
8	Direct (and shear) stress	173	3
9	Bending stress	184	1

20	Combined bending and axial stress	205
21	Structural materials: concrete, steel, timber and masonry	218
22	More on materials	229
23	How far can I span?	235
24	Calculating those loads	242
25	An introduction to structural design	252
26	More on structural types and forms	291
27	An introduction to deflection	310
28	Shear stress	324
29	Buckling and torsion	333
30	Frames and three-pinned arches	344
31	Virtual work	356
32	Squares and circles of stress: An introduction to Mohr's Circle	363
33	Trusses (no numbers)	380
34	Plastic analysis	388
Further reading		402
	pendix 1: Weights of common building materials	403
		405
Appendix 2: Conversions and relationships between units		407
Appendix 3: Mathematics associated with right-angled triangles		407
Appendix 4: Symbols		
	pendix 5: A checklist for architects	410 411
Appendix 6: Getting more out of civil engineering		
'ndex		413

1 What is structural engineering?

Introduction

In this chapter you, the reader, are introduced to structures. We will discuss what a structure actually is. The professional concerned with structures is the structural engineer. We will look at the role of the structural engineer in the context of other construction professionals. We will also examine the structural requirements of a building and will review the various individual parts of a structure and the way they interrelate. Finally you will receive some direction on how to use this book depending on the course you are studying or the nature of your interest in structures.

Structures in the context of everyday life

There is a new confidence evident in major British cities. Redundant Victorian industrial structures are being converted to luxury apartments. Tired old 1960s shopping centres are being razed to the ground, and attractive and contemporary replacements are appearing. Public housing estates built over 40 years ago are being demolished and replaced with more suitable housing. Social shifts are occurring: young professional people are starting to live in city centres and new services such as cafés, bars and restaurants are springing up to serve them. All these new uses require new buildings or converted old buildings. Every building has to have a structure. In some of these new buildings the structure will be 'extrovert' – in other words the structural frame of the building will be clearly visible to passers-by. In many others, the structure will be concealed. But, whether seen or not, the structure is an essential part of any building. Without it, there would be no building.

What is a structure?

The structure of a building (or other object) is the part which is responsible for maintaining the shape of the building under the influence of the forces, loads and other environmental factors to which it is subjected. It is important that the structure as a whole (or any part of it) does not fall down, break or deform to an unacceptable degree when subjected to such forces or loads.

The study of structures involves the analysis of the forces and stresses occurring within a structure and the design of suitable components to cater for such forces and stresses.

As an analogy, consider the human body, which comprises a skeleton of 206 bones. If any of the bones in your body were to break, or if any of the joints between those bones were to disconnect or seize up, your injured body would 'fail' structurally (and cause you a great deal of pain).



Fig. 1.1 Lower Manhattan skyline, New York City.

This is one of the largest concentrations of high-rise buildings in the world: space limitations on the island of Manhattan meant that building construction had to proceed upwards rather than outwards, and the presence of solid rock made foundations for these soaring structures feasible.

Examples of structural components (or 'members', as structural engineers call them) include the following:

- steel beams, columns, roof trusses and space frames
- · reinforced concrete beams, columns, slabs, retaining walls and foundations
- timber joists, columns, glulam beams and roof trusses
- masonry walls and columns.

For an example of a densely packed collection of structures, see Fig. 1.1.

What is an engineer?

As mentioned in the introduction, the general public is poorly informed about what an engineer is and what he or she does. 'Engineer' is not the correct word for the person who comes round to repair your ailing tumble dryer or office photocopier – nor does it have much to do with engines! In fact, the word 'engineer' comes from the French word *ingénieur*, which refers to someone who uses their ingenuity to solve problems. An engineer, therefore, is a problem-solver.

When we buy a product – for example, a bottle-opener, a bicycle or a loaf of bread – we are really buying a solution to a problem. For instance, you would buy a car not because you wish to have a tonne of metal parked outside your house but rather because of the service it can offer you: a car solves a transportation problem. You could probably think of numerous other examples:

- A can of baked beans solves a hunger problem.
- Scaffolding solves an access problem.
- Furniture polish solves a cleaning problem.
- A house or flat solves an accommodation problem.
- A university course solves an education problem.

A structural engineer solves the problem of ensuring that a building – or other structure – is adequate (in terms of strength, stability, cost, etc.) for its intended use. We shall expand on this later in the chapter. A structural engineer does not usually work alone: he is part of a team of professionals, as we shall see.

The structural engineer in the context of related professions

If I were to ask you to name some of the professionals involved in the design of buildings, the list you would come up with would probably include the following:

- architect
- structural engineer
- quantity surveyor.

Of course, this is not an exhaustive list. There are many other professionals involved in building design (e.g., building surveyors and project managers) and many more trades and professions involved in the actual construction of buildings, but for simplicity we will confine our discussion to the three named earlier.

The architect is responsible for the design of a building with particular regard to its appearance and environmental qualities such as light levels and noise insulation. His starting point is the client's brief. (The client is usually the person or organisation that is paying for the work to be done.)

The structural engineer is responsible for ensuring that the building can safely withstand all the forces to which it is likely to be subjected, and that it will not deflect or crack unduly in use.

The quantity surveyor is responsible for measuring and pricing the work to be undertaken – and for keeping track of costs as the work proceeds.

So, in short:

- 1) The architect makes sure the building looks good.
- The (structural) engineer ensures that it will stand up.
- 3) The quantity surveyor ensures that its construction is economical.

Of course, these are very simplistic definitions, but they'll do for our purposes.

Now I'm not an architect and I'm not a quantity surveyor. (My father is a quantity surveyor, but he's not writing this book.) However, I am a structural engineer and this book is about structural engineering, so in the remainder of this chapter we're going to explore the role of the structural engineer in a little more detail.

Structural understanding

The basic function of a structure is to transmit loads from the point at which the load is applied to the point of support and thus to the foundations in the ground. (We'll be looking at the meaning of the word 'load' more fully in Chapter 5, but for the time being consider a load as being any force acting externally on a structure.)

Any structure must satisfy the following criteria:

- Aesthetics it must look nice.
- 2) Economy it mustn't cost more than the client can afford; and less if possible.
- 3) Ease of maintenance.
- Durability this means that the materials used must be resistant to corrosion, spalling (pieces falling off), chemical attack, rot and insect attack.

5) Fire resistance – while few materials can completely resist the effects of fire, it is important for a building to resist fire long enough for its occupants to be safely evacuated.

In order to ensure that a structure behaves in this way, we need to develop an understanding and awareness of how the structure works.

Safety and serviceability

There are two main requirements of any structure: it must be **safe** and it must be **serviceable**. 'Safe' means that the structure should not collapse – either in whole or in part. 'Serviceable' means that the structure should not deform unduly under the effects of deflection, cracking or vibration. Let's discuss these two points in more detail.

Safety

A structure must carry the expected loads without collapsing – either as a whole or even just a part of it. Safety in this respect depends on two factors:

- 1) The loading that the structure is designed to carry has been correctly assessed.
- 2) The strength of the materials that are used in the structure has not deteriorated.

From this it is evident that we need to know how to determine the load on any part of a structure. We will learn how to do this later in the book. Furthermore, we also know that materials deteriorate over time if they are not properly maintained: steel corrodes, concrete may spall or suffer carbonation, and timber will rot. The structural engineer must consider this when designing any particular building.

Serviceability

A structure must be designed in such a way that it doesn't deflect or crack unduly in use. It is difficult or impossible to completely eliminate these things – the important thing is that the deflection and cracking are kept within certain limits. It must also be ensured that vibration does not have an adverse effect on the structure – this is particularly important in parts of buildings containing plant or machinery.

If, when you walk across the floor of a building, you feel the floor deflect or 'give' underneath your feet, it may lead you to be concerned about the integrity of the structure. Excessive deflection does not necessarily mean that the floor is about to collapse, but because it may make people feel unsafe, deflection must be 'controlled'; in other words, it must be kept within certain limits. To take another example, if a lintel above a doorway deflects too much, it may cause warping of the door frame below it and, consequently, the door itself may not open or close properly.

Cracking is ugly and may or may not be indicative of a structural problem. But it may, in itself, lead to problems. For example, if cracking occurs on the outside face of a reinforced concrete wall, then rain may penetrate and cause corrosion of the steel reinforcement within the concrete, which in turn leads to spalling of the concrete.

The composition of a building structure

A building structure contains various elements, the adequacy of each of which is the responsibility of the structural engineer. In this section we briefly consider the form and function of each. These elements will be considered in more detail in Chapter 3.



Fig. 1.2 Roof structure of Quartier 206 shopping mall, Berlin. Quite a 'muscular' roof structure!

A roof protects people and equipment in a building from weather. An example of a roof structure is shown in Fig. 1.2.

If you plan on buying a house in the United Kingdom, be wary of buying one which has a flat roof. Some roofing systems used for waterproofing flat roofs deteriorate over time, leading to leaking and potentially expensive repairs. The same warning applies to flat-roofed additions to houses, such as porches or extensions.

Walls can have one or more of several functions. The most obvious one is **load-bearing** – in other words, supporting any walls, floors or roofs above it. But not all walls are load-bearing. Other functions of a wall include the following:

- partitioning, or dividing, rooms within a building and thus defining their shape and extent
- weatherproofing
- thermal insulation keeping heat in (or out)
- noise insulation keeping noise out (or in)
- fire resistance
- security and privacy
- resisting lateral (horizontal) loads such as those due to retained earth, wind or water.

Consider the wall closest to you as you read these words. Is it likely to be load-bearing? What other functions does this wall perform?

A *floor* provides support for the occupants, furniture and equipment in a building. Floors on an upper level of a building are always *suspended*, which means that they span between supporting walls or beams. Ground floor slabs may sit directly on the ground beneath.

Staircases provide for vertical movement between different levels in a building. Figure 1.3 shows a concrete staircase in a multi-storey building. Unusually, the staircase is fully visible from outside the building. How is this staircase supported structurally?

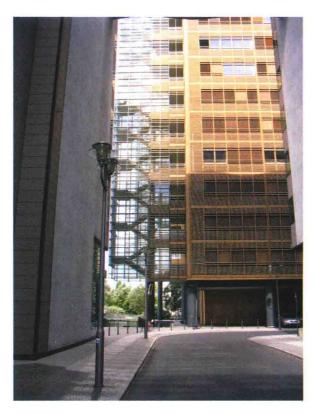


Fig. 1.3 A very visible staircase. How is it supported? You'll learn more about cantilevers later in the book.

Foundations represent the interface between the building's structure and the ground beneath it. A foundation transmits all the loads from a building into the ground in such a way that settlement (particularly uneven settlement) of the building is limited, and failure of the underlying soil is avoided.

On a small sandy island in the Caribbean, a low-rise hotel was being constructed as part of a larger leisure resort. The contractor for the hotel (a somewhat maverick individual) thought he could save money by not constructing foundations. He might have got away with it were it not for an alert supervising engineer, who spotted that the blockwork walls did not appear to be founded on anything more rigid than sand.

A furious argument ensued between the design team and the contractor, who not only readily admitted that no foundations had been built but also asserted that, in his opinion, none were required. In a developed country the contractor would have been dismissed instantly and probably prosecuted, but things were a little more free and easy in this corner of the Caribbean.

But nature exacted its own retribution. That night, a tropical storm blew up, the sea washed over the island ... and the partly built structure was entirely washed away.

In a building it is frequently necessary to support floors or walls without any interruption or division of the space below. In this case, a horizontal element called a *beam* will be used. A beam transmits the loads it supports to columns or walls at the beam's ends.



Fig. 1.4 A conventional building enclosed in a glazed outer structure. The two structures appear to be completely independent of each other.

A *column* is a vertical load-bearing element which usually supports beams and/or other columns above. Laymen often call them pillars or poles or posts. Individual elements of a structure, such as beams or columns, are often referred to as *members*.

See Fig. 1.4 for an unusual pairing of two separate structures.

A few words for students on architecture courses

If you are studying architecture, you may be wondering why you need to study structures at all. It is not the purpose of this book to make you a fully qualified structural engineer, but, as an architect, it is important that you understand the principles of structural behaviour. Moreover, with some basic training there is no reason why architects cannot design simple structural members (e.g. timber joists supporting floors) themselves. On larger projects architects work in inter-disciplinary teams which usually include structural engineers. It is therefore important to understand the role of the structural engineer and the language and terms that the structural engineer uses.

How does the study of structures impinge on the training of an architect?

If you are on a degree course in architecture, you will have formal lectures in structures throughout your course. You will also be assigned projects involving the architectural design of buildings to satisfy given requirements. It is essential to realise that all parts of the building need to be supported. Always ask yourself the question: 'How will my building stand up?' Remember – if you have difficulty in getting a model of your building to stand up, it is unlikely that the real thing will stand up either!