

# **BIOPHYSICAL CHEMISTRY**

## **Part III: The behavior of biological macromolecules**

**Cantor and Schimmel**

# **BIOPHYSICAL CHEMISTRY**

**PART**

**III**

## **THE BEHAVIOR OF BIOLOGICAL MACROMOLECULES**

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## Preface

*Biophysical Chemistry* is concerned with biological macromolecules and complexes or arrays of macromolecules. The work deals with the conformation, shape, structure, conformational changes, dynamics, and interactions of such systems. Our goal is to convey the major principles and concepts that are at the heart of the field. These principles and concepts are drawn from physics, chemistry, and biology.

We have aimed at creating a multilevel textbook in three separately bound parts. The material covers a broad range of sophistication so that the text can be used in both undergraduate and graduate courses. It also should be of value to general scientific readers who simply wish to become familiar with the field, as well as to experienced research scientists in the biophysical area. For example, perhaps half of the material requires only the background provided by a one-semester undergraduate course in physical chemistry. A somewhat smaller fraction necessitates the use of concepts and mathematical techniques generally associated with a more sophisticated background, such as elementary statistical thermodynamics and quantum mechanics.

*Biophysical Chemistry* is organized into three parts. The first part deals with the structure of biological macromolecules and the forces that determine this structure. Chapter 1 introduces the fundamental questions of interest to biophysical chemists, Chapters 2–4 summarize the known structures of proteins, nucleic acids, and other biopolymers, and Chapters 5–6 treat noncovalent forces and conformational analysis.

Part II summarizes some of the techniques used in studying biological structure and function. The emphasis is on a detailed discussion of a few techniques rather than an attempt to describe every known technique. Chapters 7–9 cover spectroscopic methods, Chapters 10–12 deal with hydrodynamic methods, and Chapters 13–14 discuss x-ray and other scattering and diffraction techniques.

Part III demonstrates how techniques and principles are used in concert to gain an understanding of the behavior and properties of biological macromolecules. The focus is on the thermodynamics and kinetics of conformational changes and ligand interactions. New techniques are introduced as needed, and a few selected case

histories or systems are discussed in considerable detail. The topics include ligand interactions (Chapters 15–17), the special theories and techniques used to study molecules that are statistical chains rather than definite folded conformations (Chapters 18–19), protein conformational changes (Chapters 20–21), nucleic acid conformational changes (Chapters 22–24), and membranes (Chapter 25).

We have made every effort to keep the chapters as independent as possible, so that the reader has a wide choice of both the material to be covered and the order in which it is to be treated. Extensive cross-references to various chapters are included to help the reader find necessary background material if the parts are not read in sequence. Where possible, examples are taken repeatedly from a small number of systems, so that the reader can have the experience of contrasting information gained about the same protein or nucleic acid from a variety of different approaches.

Within each chapter, we have attempted to maintain a uniform level of rigor or sophistication. Short digressions from this level are segregated into boxes; longer digressions are indicated by a bullet (•) preceding the section or subsection heading. Readers with a less rigorous background in physics, mathematics, and physical chemistry should find helpful the many boxes that review elementary material and make the text fairly self-contained; Appendix A provides a basic review of principles of matrix algebra. Other boxes and special subsections are aimed at advanced readers; in many cases, these discussions attempt to illuminate points that we ourselves found confusing.

In different sections, the level of mathematical sophistication varies quite significantly. We have tried to use the simplest mathematical formulation that permits a clear presentation of each subject. For example, hydrodynamic properties are treated in one dimension only. The form of a number of the fundamental equations is extracted by dimensional analysis rather than through lengthy (and not particularly instructive) solutions of hydrodynamic boundary-value problems. On the other hand, x-ray and other scattering phenomena are treated by Fourier transforms, and many problems in statistical mechanics are treated with matrix methods. These advanced mathematical techniques are used in only a few chapters, and numerous boxes are provided to assist the reader with no previous exposure to such methods. The remaining sections and chapters are self-contained and can be understood completely without this advanced mathematical formalism.

Some techniques and systems are not covered in any fair detail. This represents a biased choice by the authors, not necessarily of which techniques we feel are important, but simply of which are instructive for the beginning student in this field.

Each chapter concludes with a summary of the major ideas covered. In addition, each chapter is heavily illustrated, including some special drawings by Irving Geis. Certainly, much can be learned simply by reading the chapter summaries and by studying the illustrations. Also, we believe the illustrations convey some of the excitement of the field.

Problems are provided at the end of each chapter. These vary in difficulty from relatively simple to a few where the full answer is not known, at least to the authors. Answers to problems are provided in Appendix B.

Detailed literature citations are not included, except to acknowledge the source of published material reproduced or adapted here. However, a list of critical references for each chapter is included. In virtually all cases, these articles will provide an immediate entrée to the original papers needed for more detailed study.

The problem of notation and abbreviations in this field is a difficult one. In drawing together material from so many different types of research, we have had to adapt the notation to achieve consistency and to avoid confusion among similar symbols. Wherever possible, we have followed the recommendations of the American Chemical Society, but inevitably we have had to develop some conventions of our own. A glossary of some of the more frequently used symbols is provided.

At MIT some of this material has been used in an undergraduate course in biophysical chemistry. The course was designed to meet the needs of students wishing a second course in physical chemistry, but developed in a biochemical framework. The idea was to construct a course that covered much of the same material with the same rigor as a parallel, more traditional course. The only preparation required was a one-semester course in undergraduate physical chemistry, which at MIT is largely concerned with chemical thermodynamics.

Over the years graduate courses in biophysical chemistry at MIT and at Columbia have made use of much of the material presented here. In addition, a special-topics course in protein structure has used some of the material. Because a broad range of subjects is covered, its usefulness as a text will hopefully meet a variety of individual teaching tastes and preferences, as well as enable instructors to vary content as needs develop and change.

It is obvious that a work of this complexity cannot represent solely the efforts of its two authors. As we sought to master and explain the wide range of topics represented in biophysical chemistry, we learned why so few books have been written in this field in the past two decades. We owe a great debt to many who helped us in ways ranging from sharing their understanding to providing original research data.

We give special thanks to Irving Geis, for his effort on a number of complex illustrations and for his helpful advice on numerous other drawings; to Wilma Olson, for reading a major portion of the entire manuscript; to Robert Alberty and Gordon Hammes, for their influence, through teaching and discussions, on the material on biochemical equilibria and kinetics; to Richard Dickerson, for providing material and advice that were essential for the preparation of Chapter 13; to Paul Flory, for inspiring our treatment of conformational energies and configurational statistics of macromolecules; to Howard Schachman, whose course at Berkeley inspired parts of several chapters; to R. Wayne Oler, for bringing the authors together for this undertaking, and to Bruce Armbruster, for sealing the commitment; to the helpful people at W. H. Freeman and Company, including Ruth Allen, Arthur Bartlett, Robert Ishi, Larry McCombs, and Pearl Vapnek; to Kim Engel, Karen Haynes, Marie Ludwig, Joanne Meshna, Peggy Nelson, Cathy Putland, and Judy Schimmel, for typing and related work associated with the manuscript; and to Cassandra Smith and to Judy, Kathy, and Kirsten Schimmel, for their patience with the intrusion this work has made on the authors' lives.

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## Glossary of symbols

This glossary includes some of the symbols used extensively throughout the text. In many cases, the same or very similar symbols are used in certain contexts with other meanings; the meaning of a symbol is explained in the text where it is introduced.

Symbol	Meaning	Symbol	Meaning
$A$	Absorbance.	$c_p$	Plateau weight concentration.
$A_{ij}$	Amplitude of kinetic decay.	$\hat{c}_i$	Weight concentration of $i$ th species or component.
$\text{\AA}$	Angstroms.	$\mathbf{c}$	Unit cell basis vector.
$a$	Hyperfine splitting constant. Long semi-axis of ellipse. Persistence length.	$\mathbf{c}^*$	Reciprocal cell basis vector.
$\mathbf{a}$	Unit cell basis vector.	$D$	Debye.
$\mathbf{a}^*$	Reciprocal cell basis vector.	$D$	Translational diffusion constant.
$a_{ij}$	Parameters composed of rate constants.	$D_n$	Dihedral symmetry group element.
$a_z$	Exponent relating sedimentation to chain length.	$D_{\text{rot}}$	Rotational diffusion constant.
$a_\eta$	Exponent relating viscosity to chain length.	$D_{20,w}$	$D$ extrapolated to 20° C, water.
$b$	Short semiaxis of ellipse.	$E_a$	Activation energy.
$\mathbf{b}$	Unit cell basis vector.	$E_d$	Interaction energy between two dipoles.
$\mathbf{b}^*$	Reciprocal cell basis vector.	$E_{kl}$	Nonbonded pair interaction potential.
$C$	Molar concentration.	$E_{\text{tor}}$	Torsional potential energy.
$C_n$	Rotational symmetry group element.	$E(\Phi_i, \Psi_i)$	
$C_\infty$	Limiting characteristic ratio.	$E_i$	Total rotational potential for residue $i$ .
$\Delta C_p^0$	Standard constant pressure heat capacity change per mole.	$\mathbf{E}$	Electric field.
$c$	Velocity of light in vacuum. Ratio of $k_R/k_T$ . Weight concentration.	$e$	Exponential function. Unit of charge on electron.
		$F$	Frictional coefficient ratio.
		$F(S)$	Structure factor.
		$F_H(S)$	Structure factor, heavy-atom contribution.



Symbol	Meaning	Symbol	Meaning
$F_{\text{Tot}}(\text{S})$	Structure factor for an array.	$H_{\text{res}}$	Magnetic field at which resonance occurs.
$F_{\text{m}}(\text{S})$	Molecular structure factor.	$\hat{H}$	Hamiltonian operator.
$F$	Force.	$\Delta H_{\text{loc}}$	Magnetic field generated by local environment.
$\mathcal{F}$	The Faraday.	$h$	Planck's constant.
$f$	Translational frictional coefficient.	$\hbar$	$h/2\pi$
$f_{\text{app}}$	Apparent fractional denaturation.	$I$	Intensity of radiation. Nuclear spin quantum number. Ionic strength.
$f_{\text{D}}$	Fraction in denatured state.	$I(\text{S})$	Scattering intensity relative to a single electron at the origin.
$f_{\text{N}}$	Fraction in native state.	$i$	$\sqrt{-1}$
$f_{\text{min}}$	Translational friction coefficient of anhydrous sphere.	$\hat{i}$	Cartesian unit vector.
$f_{\text{rot}}$	Rotational friction coefficient for sphere.	$J$	NMR coupling constant.
$f_{\text{sph}}$	Translational friction coefficient for sphere.	$J_2$	Solute flux.
$f_{\text{a}}, f_{\text{b}}$	Rotational friction coefficient around $a$ , $b$ axis of ellipse.	$\hat{j}$	Cartesian unit vector.
$G$	Gibbs free energy.	$K_{\text{D}}$	True equilibrium constant for conversion from fully native to fully denatured state.
$\Delta G^0$	Standard Gibbs free energy change per mole.	$K_{\text{p}}$	Michaelis constant for product.
$\Delta \bar{G}^0$	Intrinsic standard free energy change (with statistical component removed).	$K_{\text{s}}$	Michaelis constant for substrate.
$\Delta G_{\text{L},ij}$	Free energy of interaction between two ligands.	$K_{\eta}$	Coefficient relating viscosity to chain length.
$\Delta G_{\text{r}}$	$\Delta G$ per residue.	$K_{\text{s}}$	Coefficient relating sedimentation to chain length.
$\Delta G_{\text{Tot}}$	Total free energy change per mole.	$K_{\text{app}}$	Apparent equilibrium constant for conversion from fully native to fully denatured state.
$\Delta G_{\text{el}}$	Change in electrostatic free energy.	$K_{\text{i}}$	Macroscopic equilibrium constant. Equilibrium constant for forming $i$ th configuration. Equilibrium constant for transition from native state to intermediate state $i$ .
$\Delta \Delta G_{\text{T}}$	Difference in $\Delta G_{\text{T}}$ between two configurations.	$\tilde{K}_{\text{i}}$	Apparent dissociation constant, one-ligand system.
$\Delta \bar{G}_{\text{gr}}$	Average helix growth free energy change per residue pair.	$\tilde{K}_{ij}$	Apparent dissociation constant, two-ligand system.
$g$	$g$ value for free electron, 2.00232.	$k$	Boltzmann's constant. Microscopic equilibrium dissociation constant.
$g_{\text{x}}$ , etc.	Component of $g$ -factor tensor.	$k_{\text{R}}$	Microscopic dissociation constant for $R$ state.
$H$	Enthalpy.	$k_{\text{T}}$	Microscopic dissociation constant for $T$ state.
$H_{\text{xy}}$	Magnetic field in $xy$ plane.	$k_{\text{i}}$	Microscopic equilibrium constant.
$\Delta H$	Enthalpy change per mole.	$\hat{k}$	Cartesian unit vector.
$\Delta H^0$	Standard enthalpy change per mole.		
$\Delta H_{\text{r}}$	$\Delta H$ per residue.		
$\Delta H_{\text{D}}$	Enthalpy change for conversion from fully native to fully denatured state.		
$\Delta H_{\text{app}}$	Apparent enthalpy change for conversion from fully native to fully denatured state.		
$H$	Magnetic field.		

Symbol	Meaning
$L_c$	Contour length.
$L, L'$	Equilibrium constant for $R_0 \rightleftharpoons T_0$ .
$L$	Angular momentum.
$l$	Length of one polymer bond.
$l_s$	Length of statistical segment.
$M$	Molecular weight.
$\bar{M}_n$	Number-average molecular weight.
$\bar{M}_w$	Weight-average molecular weight.
$\bar{M}_i$	Molecular weight of $i$ th macromolecular species.
$M_{ij}$	Species with $i$ bound $L_1$ and $j$ bound $L_2$ .
$M^{(j)}$	Set of all species with $j$ bound $L_2$ .
$M$	Magnetization.
$M_{xy}$	Magnetization in $xy$ plane.
$\underline{M}$	Statistical weight matrix.
$m$	Colligative molality. Mass of object.
$m_e$	Mass of electron.
$m_i$	Molality of $i$ th species.
$m_s$	Quantum number of electron spin along $z$ axis.
$m_l$	Quantum number of nuclear spin along $z$ axis.
$m'$	Total molality.
$\mu$	Magnetic dipole operator.
$N_0$	Avogadro's number.
$N_C$	Number of carbons in amphiphile $R$ chain.
$N'_C$	Number of carbons in amphiphile that are imbedded in hydrocarbon core of micelle.
$N_s$	Number of statistical segments.
$N_{Ch}$	Number of chains in micelle.
$N_{hg}$	Number of head groups in micelle.
$n$	Refractive index. Number of sites. Number of bonds in polymer.
$n_i$	Number of moles of component $i$ . Number of sites of certain type.
$n_w$	Weight-average degree of polymerization.
$P$	Pitch of helix. Pressure. Patterson function.
$P_0$	Solvent vapor pressure.
$P_v$	Solvent vapor pressure in presence of solute.

Symbol	Meaning
$P_r$	Axial ratio.
$pK_a$	$-\log_{10} K_a$ .
$pO_2$	Partial pressure of oxygen.
$(pO_2)_{1/2}$	Partial pressure of oxygen at half saturation.
$\hat{p}$	Momentum operator.
$Q$	Configurational partition function.
$R$	Gas constant.
$R_G$	Radius of gyration.
$\langle R_G^2 \rangle_0$	Unperturbed mean square radius of gyration.
$\bar{R}$	Fraction of molecules in $R$ state.
$\hat{R}$	Nuclear position operator.
$\underline{R}(\alpha, \beta)$	Coordinate transformation matrix.
$r$	Distance of separation.
$r_D$	Donnan ratio.
$r_e$	Radius of equivalent sphere.
$\langle r^2 \rangle_0$	Unperturbed mean square end-to-end distance.
$r$	Polymer end-to-end vector.
$\hat{r}$	Electron position operator.
$S$	Svedberg (unit of sedimentation coefficient).
$S_A$	Partial molal entropy.
$S'_A$	Unitary part of $S_A$ .
$\Delta S_r$	$\Delta S$ per residue.
$\Delta S^0$	Standard entropy change.
$\Delta S_u^0$	Unitary standard entropy change.
$S$	Scattering vector.
$s$	Sedimentation coefficient. Statistical weight. Equilibrium constant for helix growth. Equilibrium constant for base-pair formation.
$s_{20,w}$	Sedimentation coefficient corrected to 20° C, water.
$\hat{s}$	Unit vector along scattered radiation.
$\hat{s}_0$	Unit vector along incident radiation.
$T$	Temperature (in degrees Kelvin usually).
$T_m$	Melting temperature.
$T_1$	Longitudinal relaxation time.
$T_2$	Transverse relaxation time.
$\underline{T}_i$	Transformation matrix.
$t$	Time.

Symbol	Meaning
$U_{\text{mic}}^0$	Attractive part of $\mu_{\text{mic}}^0$ .
$u$	Component of $M_{xy}$ in phase with $H_{xy}$ . Electrophoretic mobility.
$V$	Volume.
$V_b$	Hydrated volume.
$\bar{V}_i$	Partial specific volume of component $i$ .
$V_p$	Maximum reaction velocity in reverse direction.
$V_s$	Maximum reaction velocity in forward direction.
$v$	Speed (also called velocity). Component of $M_{xy}$ out of phase with $H_{xy}$ .
$v_i$	Initial reaction velocity.
$\langle v_2 \rangle$	Effective average solute velocity.
$\bar{v}$	Partial molar volume.
$\bar{v}_s$	Partial molar volume of pure solvent.
$v$	Velocity.
$W(r)$	Radial distribution function of end-to-end distance.
$W(x,y,z)$	End-to-end distance distribution function.
$W_{\text{mic}}^0$	Repulsive part of $\mu_{\text{mic}}^0$ .
$(X_i)$	Equilibrium concentration.
$\Delta(X_i)$	Difference between temporal and equilibrium concentration.
$x_b$	Bottom of cell.
$x_m$	Meniscus position.
$y$	General physical property.
$y_D$	Physical property of denatured state.
$y_N$	Physical property of native state.
$\bar{y}$	Fractional saturation of site.
$\bar{y}_F$	Fractional saturation with ligand F.
$z$	Charge on macromolecule or ion in units of $e$ .
$z_i$	Ionic valence of $i$ th ion.
$\alpha$	Degree of association. Dimensionless binding parameter like $(F)/k_R$ .
$\alpha_H$	Hill constant.
$\beta$	Dimensionless binding parameter.
$\beta_e$	Bohr magneton.
$\beta_n$	Nuclear magneton.
$\beta_s$	Mandelkern-Flory-Scheraga parameter.
$\beta'$	Scheraga-Mandelkern parameter.

Symbol	Meaning
$\Gamma$	Parameter affecting relaxation amplitudes.
$\gamma$	Magnetogyric ratio. $(A)/K_{AB}$ binding parameter. Velocity gradient $dv_x/dz$ .
$\lambda_1, \lambda_2$	Parameters composed of rate constants.
$\delta$	Chemical shift parameter. Phase shift.
$\delta(x)$	Dirac delta function of argument $x$ .
$\delta_1$	Hydration (in grams per gram).
$\delta_{ij}$	Kronecker delta.
$\epsilon$	Dielectric constant. Molar decadic or residue extinction coefficient.
$\Delta\epsilon$	Circular dichroism ( $\epsilon_L - \epsilon_R$ ).
$\eta$	Solution viscosity.
$\eta_0$	Solvent viscosity.
$\eta_{\text{rel}}$	Relative viscosity.
$\eta_{\text{sp}}$	Specific viscosity.
$[\eta]$	Intrinsic viscosity.
$\Theta_i$	Fractional saturation of $i$ th site.
$\theta$	Scattering angle. Fractional helicity.
$[\theta]$	Molar ellipticity.
$\hat{\Lambda}$	Matrix of $\lambda_i$ 's.
$\lambda$	Eigenvalue. Wavelength. Kinetic decay time.
$\lambda_j$	$j$ th kinetic decay time of $j$ th eigenvalue.
$\mu_i$	Chemical potential per mole.
$\mu_i^0$	Standard chemical potential per mole.
$\hat{\mu}_i$	Chemical potential per gram.
$\hat{\mu}_i^0$	Standard chemical potential per gram.
$\mu_{\text{mic}}^0$	Standard chemical potential of amphiphile in micelle.
$\mu_w^0$	Standard chemical potential of amphiphile in aqueous phase.
$\mu_m$	Magnetic moment.
$\hat{\mu}$	Electric dipole moment operator.
$\nu$	Frequency. Simha factor in viscosity.
$\nu_N$	Moles of ligand bound per mole of macromolecule.
$\nu_N$	Saturation density for lattice with $N$ units.
$\pi$	Osmotic pressure.
$\rho$	Mass density (in grams per $\text{cm}^3$ ).
$\rho(r)$	Electron density.
$\sigma$	Nucleation constant.

Symbol	Meaning
$\sigma_h$	Superhelix density.
$\tau$	Number of supercoils.
$\tau_F$	Fluorescence decay time.
$\tau_a, \tau_b$	Rotational relaxation time for $a$ -, $b$ -axis orientation.
$\tau_c$	Rotational correlation time.
$\tau_r$	Rotational relaxation time of sphere.
$\tau, \tau_j$	Reaction relaxation times.
$\Phi$	Electrical potential. Voltage difference.
$\Phi_c$	Universal constant for random coils $2 \cdot 1 \times 10^{23}$ .
$\phi$	N-C' torsional angle. Phase of complex number.
$\phi_{1a}, \phi_{2a}$ etc	Monomer wave functions.
$\phi_F$	Fluorescence quantum yield.
$\phi_p$	Practical osmotic coefficient.
$\phi', \phi''$	Nucleic acid backbone torsional angles.
$[\phi]$	Molar rotation per residue.
$\chi$	Mole fraction of all solute species.
$\chi_i$	Mole fraction of $i$ th component.
$\chi_A$	Mole fraction of $A$ th component.
$\chi_{gc}$	Mole fraction G + C.
$\chi$	Glycosidic bond torsional angle.
$\psi$	C'-C torsional angle.
$\psi', \psi''$	Nucleic acid backbone torsional angles.
$\Omega_{jk}$	Number of ways of putting $k$ helical units into $j$ separated sequences.
$\Omega_k$	$(n - k + 1)$ number of ways of placing $k$ helical units in one sequence within chain of $n$ residues.
$\Omega_{n,i}$	Number of ways of assorting $i$ items (ligands) in $n$ boxes (sites).

Symbol	Meaning
$\omega$	Circular frequency or angular velocity.
$\omega_0$	Larmor frequency.
$\omega', \omega''$	Nucleic acid backbone torsional angles.
$\Delta\omega_{1/2}$	Line width.
$\omega$	Angular velocity.
imag	Imaginary part of.
$\langle \rangle$	Average.
$\langle   \rangle$	Overlap integral.
$\langle    \rangle$	Expectation value integral.
*	Superscript, complex conjugate, as in $F^*$ .
$\ $	Amplitude of complex number or length of vector, as in $ F $ .
$\nabla$	Vector differential.
( )	Molar concentration, as in (A).
$\dagger$	Superscript, transpose of matrix, as in $A^\dagger$ .
$\sim$	Superscript, convolution product, as in $\hat{A}B$ .

#### General Rules

$K$	Macroscopic equilibrium constant.
$k$	Microscopic equilibrium constant or rate constant.
$C$	Molar concentration.
$c$	Weight concentration.
$\underline{M}$	All matrices and operators.
$\hat{e}$	All unit vectors.
$R_G$	Radius of gyration.
$\chi$	Mole fraction.
$\Phi$	Voltage or electrical potential.

PART III

## THE BEHAVIOR OF BIOLOGICAL MACROMOLECULES

The first two Parts emphasize the structure of biological molecules (Part I) and the techniques available for determining their structure and behavior (Part II). Part III focuses on the relationship between structure and behavior, and on the mechanisms that lie at the heart of biological function. The physiological function of proteins and nucleic acids commonly is manifested through interactions with specific ligands; Chapters 15, 16, and 17 treat equilibrium and kinetic aspects of ligand interactions, including (in Chapter 17) a discussion of control mechanisms that modulate biological activity. Much of the treatment is applicable to interactions of biological macromolecules in general, although most examples are drawn from systems of proteins.

After this treatment, attention shifts to the conformational behavior of biological polymers. For example, Chapter 18 takes up polymer configuration statistics, with emphasis on the statistics of polypeptides in relation to chain conformation. Chapter 19 outlines how the hydrodynamic properties of double-stranded DNA in solution reveal that it is a wormlike coil. In Chapters 20 and 21, we consider conformational changes of proteins and polypeptides, including the well-studied polypeptide helix-coil transition (Chapter 20) and the problem of the reversible folding of proteins (Chapter 21).

The emphasis shifts to nucleic acids in Chapters 22 through 24, where we take up the ligand interactions, conformational changes, and tertiary structural organization

of certain nucleic acids. Some of these issues parallel those of the preceding chapters, where more emphasis was placed on proteins and polypeptides. The book concludes in Chapter 25 with a shift to the important subject of membrane equilibria and the structure and behavior of lipid bilayers.

Of course, much of the material in Part III is tied closely to the discussion in Parts I and II. In appropriate places, reference is made to the earlier chapters. However, many readers will find it possible to read a good portion of this Part without having read the other Parts, particularly if the appropriate section of an earlier chapter is consulted when needed.

## Contents in detail of Part III

Contents in Brief of Parts I and II xvii

Preface xxi

Glossary of Symbols xxv

### PART III THE BEHAVIOR OF BIOLOGICAL MACROMOLECULES 847

#### Chapter 15 Ligand Interactions at Equilibrium 849

15-1 Importance of Ligand Interactions 849

15-2 Ligand Equilibria 850

Macroscopic and microscopic constants 850

15-3 Identical Independent Sites 852

Calculating the number of microscopic species 852

Calculation of  $\nu$  853

A simple derivation 856

Scatchard plot 856

15-4 Multiple Classes of Independent Sites 856

Curved Scatchard plots 856

Decomposition of a biphasic Scatchard plot 858

15-5 Interaction Between Sites 859

Some general considerations 859

Prevalence of cooperative interactions 862

Statistical effects and interaction energy 862

A semiempirical approach: the Hill constant 863

• 15-6 Binding of Two Different Ligands: Linked Functions 866

• Formalism 867

• Two ligands and a basic linkage relationship 868

• Another equation for the linkage effect 869

Box 15-1 Cross-differentiation 869

*Box 15-2 The chain rule 870*

## • An additional relationship 871

- 15-7 Linkage of Ligand Binding from an Energetic Viewpoint 874
  - Coupling free energy 874
  - Effect of coupling energy on distribution of bound ligands 876
  - Coupling free energies found in biological systems 877
- 15-8 Interaction of Large Ligands with Lattice-like Chains 878
  - The homogeneous lattice: statistical features 878
  - Calculation of ligand-binding behavior 879
  - Nonlinear Scatchard plots resulting from statistical effects 880
  - Some results on a real system 881
  - Lattices of finite length and end effects 882
  - Ligand–ligand interactions 883

**Chapter 16 Kinetics of Ligand Interactions 887**

- 16-1 Biochemical Kinetic Studies 887
- 16-2 Unimolecular Reactions 888
  - One-step reactions 888
  - Two coupled reactions 889
  - A series of sequential reactions 890
- 16-3 Simple Bimolecular Reaction 892
- 16-4 Simple Michaelis–Menten Mechanism 892
  - Solution to the rate equations for a special case 892
  - Condition for steady-state approximation 894
- 16-5 Multiple Intermediates 895
- 16-6 Steady-State Kinetics 896
  - Single-substrate-to-single-product mechanism with one intermediate 896
  - Obtaining steady-state parameters from experimental data 897
  - A more general solution: the Haldane relationship 898
  - Relationship between Michaelis constants and equilibrium constants 899
  - Multiple-intermediate form of the steady-state rate equation 899
  - Lower bounds to rate constants 900
  - Turnover numbers 901
  - pH dependence of enzyme reactions 901
  - Box 16-1 Catalytic efficiency 903*
  - Understanding the pH dependence 904
  - Determination of ionization constants 906
  - Limitations of steady-state kinetics 907
- 16-7 Relaxation Spectrometry 907
  - Thermodynamic principle 908
  - Relaxation kinetics 910
  - Linearized rate equations for a two-step enzymatic mechanism 912
  - Simplified relaxation-time expressions for the two-step mechanism 913
  - Another derivation of relaxation-time expressions for the two-step mechanism 914



Spectrum of relaxation times for an  $n$ -intermediate mechanism 915  
 Some conclusions from fast-reaction studies 916

*Box 16-2* A matrix approach to linearized rate equations 918

*Box 16-3* Bimolecular rate constant  
 for a diffusion-controlled reaction 920

#### 16-8 Ribonuclease as an Example 923

Multiple intermediates in kinetic studies 923

Chemical modification studies 925

Implications of effect of subtilisin on ribonuclease 926

Active dimers of ribonuclease 926

The four histidines resolved and studied by NMR 926

X-ray structure 929

### Chapter 17 Regulation of Biological Activity 939

#### 17-1 Biological Regulation 939

Feedback inhibition 939

The pyrimidine pathway and aspartate transcarbamoylase 940

Allosteric proteins 940

#### 17-2 Some Features and Properties of Allosteric Enzymes 941

Sigmoidal curves 941

Effect of an allosteric inhibitor 941

*Box 17-1* Competitive inhibition 943

Effect of a competitive inhibitor 944

#### 17-3 Monod-Wyman-Changeux (MWC) Model for Allosteric Proteins 945

Four main assumptions 945

Homotropic and heterotropic interactions 946

Algebraic treatment of the MWC model 946

Behavior of  $\bar{Y}_F$ : effects of  $L$  and  $c$  949

Comparison of the parameters  $\bar{R}$  and  $\bar{Y}_F$  951

Effects of allosteric activators and inhibitors 952

#### 17-4 Experimental Tests of the MWC Model 953

Explanation of some data on ligand interactions 953

Relation between conformational change and fractional saturation 954

#### 17-5 Alternative Models for Allosteric Proteins 956

A sequential model 957

A more general scheme 958

#### 17-6 Hemoglobin 959

Cooperative oxygen binding 959

Treatment of oxygenation equilibrium: the Adair scheme 960

Estimates of microscopic constants for oxygen binding 961

Concentrations of hemoglobin species during oxygenation 961

The Hill constant and site-site interaction energy 962

Bohr effect 963

Estimating  $pK$  values of oxygen-linked ionizations 966

Influence of organic phosphates on the oxygenation curve 967

#### 17-7 Interaction of Carbon Dioxide with Hemoglobin 970

#### 17-8 Hemoglobin Structure in Relation to Mechanism 971