

海外优秀数学类教材系列丛书

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Advanced Engineering Mathematics

(Fifth Edition)

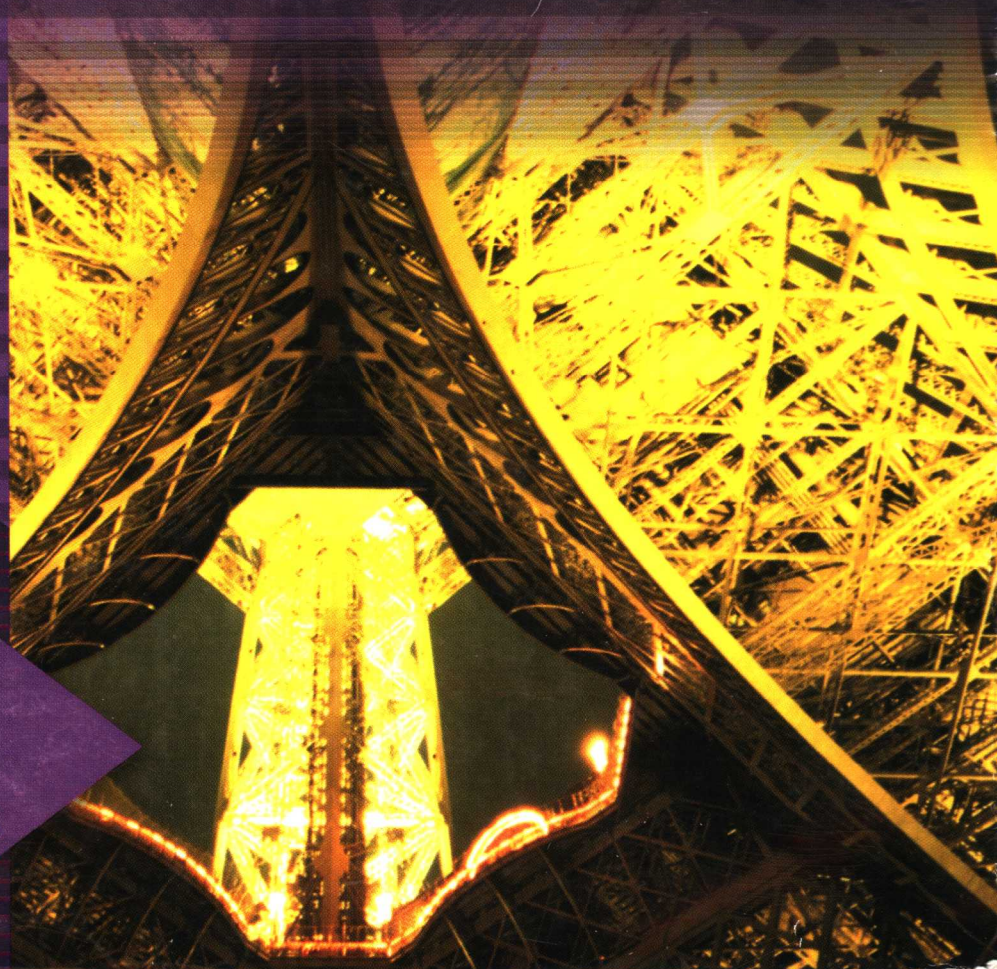
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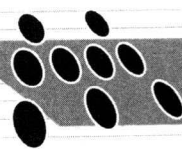
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□ Peter V. O'Neil



高等教育出版社
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Advanced Engineering Mathematics

(5th Edition)

高等工程数学 (第5版)(下册)

Peter V. O'Neil

University of Alabama at Birmingham



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Peter V. O' Neil

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出版者的话

在我国已经加入 WTO、经济全球化的今天,为适应当前我国高校各类创新人才培养的需要,大力推进教育部倡导的双语教学,配合教育部实施的“高等学校教学质量与教学改革工程”和“精品课程”建设的需要,高等教育出版社有计划、大规模地开展了海外优秀数学类系列教材的引进工作。

高等教育出版社和 Pearson Education, John Wiley & Sons, McGraw-Hill, Thomson Learning 等国外出版公司进行了广泛接触,经国外出版公司的推荐并在国内专家的协助下,提交引进版权总数 100 余种。收到样书后,我们聘请了国内高校一线教师、专家、学者参与这些出版教材的评入工作,并参考国内相关专业的课程设置和教学实际情况,从中遴选出了这套优秀教材组。

这批教材普遍具有以下特点:(1)基本上是近 3 年出版的,在国际上广泛使用,在同类教材中具有相当的权威性;(2)高版次,历经多年教学实践检验,内容翔实准确、反映时代要求;(3)各种教学资源配套整齐,为师生提供了极大的便利;(4)插图精美、丰富,图文并茂,与正文相辅相成;(5)语言简练、流畅、可读性强,比较适合非英语国家的学生阅读。

本系列丛书中,有 Finney、Weir 等编的《托马斯微积分》(第 10 版, Pearson)其特色可用“呈传统特色、富革新精神”概括,本书自 20 世纪 50 年代第 1 版以来,每隔四年就有一个新版面世,长在 50 余年始终盛行于西方教坛,作者既有相当高的学术水平,又热爱数学,长期在教学第一线,其中,年近 90 的 G.B.Thomas 教授长年在 MIT 工作,具有丰富的教学经验,Finney 教授也在 MIT 工作达 10 年;Weir 是美国数学建模竞赛委员会主任。Stewart 编的立体化教材《微积分》(第 5 版, Thomson Learning)配备了丰富的教学资源,是国际上最畅销的微积分原版教材,2003 年全球销量约 40 余万册,在美国,占据了约 50%~60%的微积分教材市场,其用户包括耶鲁等名牌院校及众多一般院校 600 余所。本系列丛书还包括 Anton 编的经典教材《线性代数及其应用》(第 8 版, Wiley); Jay L. Devore 编的优秀教材《概率论与数理统计》(第 5 版, Thomson Learning)等。在努力降低引进教材售价方面,高等教育出版社做了大量和细致的工作,这套引进的教材体现了一定的权威性、系统性、先进性和经济性等特点。

通过影印、翻译、编译这批优秀教材,我们一方面要不断地分析、学习、消化吸收国外优秀教材的长处,吸取国外出版公司的制作经验,提升我们自编教材的立体化配套标准,使我国高校教材建设水平上一个新的台阶;与此同时,我们还将尝试组织海外作者和国内作者合编外文版基础课数学教材,并约请国内专家改编部分国外优秀教材,以适应我国实际教学环境。

这套教材出版后,我们将结合各高校的双语教学计划,开展大规模的宣传、培训工作,及时地将本套丛书推荐给高校使用。在使用过程中,我们衷心希望广大高校教师和同学提出宝贵的意见和建议,如有好的教材值得引进,请与高等教育出版社高等理科分社联系。

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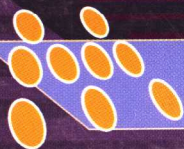
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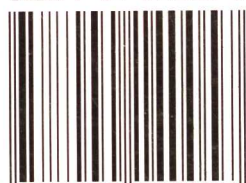
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