

Graduate Texts in Mathematics

David Eisenbud

Commutative Algebra with a View Toward Algebraic Geometry

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David Eisenbud

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with a View Toward Algebraic Geometry

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**To Leonard, Ruth-Jean, Monika:
For capacity, passion, endurance**

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¹The selected exercises are marked with a *

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