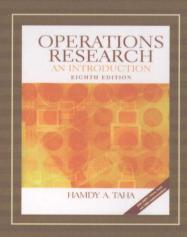


Operations Research An Introduction

初级篇

(英文版・第8版)

[美] Hamdy A. Taha 著





Operations Research: An Introduction

运筹学导论

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内容提要

本书是运筹学方面的经典著作之一,为全球众多高校采用.初级篇共12章,内容包括线性规划建模、单纯形方法和灵敏度分析、对偶性和后最优分析、运输模型及其变型、网络模型、目标规划、整数线性规划、确定性动态规划、确定性库存模型、决策分析和博弈、排队系统等,并附有AMPL建模语言简介.

本书可作为经管类专业、数学专业和计算机专业本科生的教材,也可供相关研究人员参考.

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前 言

本书第8版对内容作了很多的修订,在教材的编排上突出反映运筹学中的应用问题和计算方法.

- 第2章通过城市规划、货币套利交易、投资、生产计划、混合配比、排序以及下料等实际问题的应用,主要介绍了线性规划的建模.新增加的习题也涉及从水质管理和交通控制到军事领域等多个运筹问题.
- 第3章以一种简单和直接的方式介绍了一般性的线性规划灵敏度分析,包括对偶价格和简约费用(reduced cost),作为单纯形表计算部分的直接扩充.
 - •本版的第4章主要讲述基于对偶性进行线性规划最优化后的分析.
- 针对旅行商问题 (Traveling Salesperson Problem), 介绍了一个基于Excel的 组合式最近邻点反向启发式算法.
 - •新增的第17章扩充了马尔可夫链的处理方法.
- 在全新的第24章里,详细介绍了15个实际应用案例. 对这些案例的分析通常涉及多种OR技术(例如启发式算法和线性规划,或者线性整数规划和排队论),用来进行建模、数据采集以及问题的求解计算等. 这些应用问题在相关的各章都有引用,使读者能够充分了解实际生活中如何运用运筹学技术.
 - •新的附录E收录了按照章节排列的约50个小型实用问题的例子.
 - 本书还包含了1000多个节后习题.
 - 每章开始都有本章导读,以帮助读者了解教材内容和有效利用附带的软件程序.
 - 把教材与软件相结合可以让读者对需要深入介绍的概念进行实际检验:
- 1. 全书都用到了Excel程序,包括动态规划、旅行商问题、库存问题、层次分析法、贝叶斯概率、"电子化"统计表、排队问题、模拟、马尔可夫链和非线性规划等.一些程序中的交互式用户输入功能有助于对相应方法的更好理解.
- 2. 对Excel Solver程序的使用扩展到了全书,特别用在线性规划、网络规划、整数规划和非线性规划问题.
- 3. AMPL®是一种强大的商业化建模语言,本书将AMPL结合在大量的例题中,这些例子涉及线性、网络、整数和非线性规划问题. 附录A给出了AMPL的语句规则以及本书例题中所引用的语言素材.
 - 4. 本书中, TORA仍然充当教学软件的重要角色.
- 所有与计算机相关的材料都相对独立,有的作为单独的章节,有的按照标题 AMPL/Excel/Solver/TORA程序作为一小节,以尽量不影响本书的主要内容的介绍.

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带的CD里,作者把运筹学导论课程中不太经常用到的内容截选下来,也放在CD里'. **致 谢**

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Contents

初级篇

Chapter 1	What Is Operations Research? 1
	1.1 Operations Research Models 1
	1.2 Solving the OR Model 4
	1.3 Queuing and Simulation Models 5
	1.4 Art of Modeling 5
	1.5 More Than Just Mathematics 7
	1.6 Phases of an OR Study 8
	1.7 About This Book 10
	References 10
Chapter 2	Modeling with Linear Programming 11
	2.1 Two-Variable LP Model 12
	2.2 Graphical LP Solution 15
	2.2.1 Solution of a Maximization Model 16
	2.2.2 Solution of a Minimization Model 23
	2.3 Selected LP Applications 27
	2.3.1 Urban Planning 27
	2.3.2 Currency Arbitrage 32
	2.3.3 Investment 37
	2.3.4 Production Planning and Inventory Control 42
	2.3.5 Blending and Refining 51
	2.3.6 Manpower Planning 57
	2.3.7 Additional Applications 60
	2.4 Computer Solution with Solver and AMPL 68
	2.4.1 LP Solution with Excel Solver 69
	2.4.2 LP Solution with AMPL 73
	References 80
Chapter 3	The Simplex Method and Sensitivity Analysis 81
	3.1 LP Model in Equation Form 82
	3.1.1 Converting Inequalities into Equations
	with Nonnegative Right-Hand Side 82
	3.1.2 Dealing with Unrestricted Variables 84
	3.2 Transition from Graphical to Algebraic Solution 85
	3.3 The Simplex Method 90
	3.3.1 Iterative Nature of the Simplex Method 90
	3.3.2 Computational Details of the Simplex Algorithm 93

Chapter 4

Chapter 5

	3.3.3 Summary of the Simplex Method 99		
3.4			
	3.4.1 <i>M</i> -Method <i>104</i>		
	3.4.2 Two-Phase Method 108		
3.5	Special Cases in the Simplex Method 113		
	3.5.1 Degeneracy <i>113</i>		
	3.5.2 Alternative Optima 116		
	3.5.3 Unbounded Solution 119		
	3.5.4 Infeasible Solution 121		
3.6			
	3.6.1 Graphical Sensitivity Analysis 123		
	3.6.2 Algebraic Sensitivity Analysis—Changes in the Right- Hand Side 129		
	3.6.3 Algebraic Sensitivity Analysis—Objective Function 139		
	3.6.4 Sensitivity Analysis with TORA, Solver, and AMPL 146		
	References 150		
	3 galleby A 10-12. A.I		
Du	ality and Post-Optimal Analysis 151		
4.1	Definition of the Dual Problem 151		
4.2	Primal-Dual Relationships 156		
	4.2.1 Review of Simple Matrix Operations 156		
	4.2.2 Simplex Tableau Layout 158		
	4.2.3 Optimal Dual Solution 159		
	4.2.4 Simplex Tableau Computations 165		
4.3	Economic Interpretation of Duality 169		
	4.3.1 Economic Interpretation of Dual Variables 170		
	4.3.2 Economic Interpretation of Dual Constraints 172		
4.4	The state of the s		
	4.4.1 Dual Simplex Algorithm 174		
	4.4.2 Generalized Simplex Algorithm 180		
4.5	Post-Optimal Analysis 181		
	4.5.1 Changes Affecting Feasibility 182		
	4.5.2 Changes Affecting Optimality 187		
	References 191		
Tra	nsportation Model and Its Variants 193		
5.1			
5.2			
5.3			
	5.3.1 Determination of the Starting Solution 207		

5.3.2 Iterative Computations of the Transportation

5.3.3 Simplex Method Explanation of the Method

Algorithm 211

of Multipliers 220
5.4 The Assignment Model 221
5.4.1 The Hungarian Method 222

	5.4.2 Simplex Explanation of the Hungarian Method	228
5.5	The Transshipment Model 229	
	Peference 224	

Chapter 6 Network Models 235

- 6.1 Scope and Definition of Network Models 236
- 6.2 Minimal Spanning Tree Algorithm 239
- 6.3 Shortest-Route Problem 243
 - 6.3.1 Examples of the Shortest-Route Applications 243
 - 6.3.2 Shortest-Route Algorithms 248
 - 6.3.3 Linear Programming Formulation of the Shortest-Route Problem 257
- 6.4 Maximal flow model 263
 - 6.4.1 Enumeration of Cuts 263
 - 6.4.2 Maximal Flow Algorithm 264
 - 6.4.3 Linear Programming Formulation of Maximal Flow Mode 273
- 6.5 CPM and PERT 275
 - 6.5.1 Network Representation 277
 - 6.5.2 Critical Path (CPM) Computations 282
 - 6.5.3 Construction of the Time Schedule 285
 - 6.5.4 Linear Programming Formulation of CPM 292
 - 6.5.5 PERT Networks 293
 References 296

Chapter 7 Goal Programming 297

- 7.1 A Goal Programming Formulation 298
- 7.2 Goal Programming Algorithms 302
 - 7.2.1 The Weights Method 302
 - 7.2.2 The Preemptive Method 305
 - References 312

Chapter 8 Integer Linear Programming 313

- 8.1 Illustrative Applications 314
 - 8.1.1 Capital Budgeting 314
 - 8.1.2 Set-Covering Problem 318
 - 8.1.3 Fixed-Charge Problem 324
 - 8.1.4 Either-Or and If-Then Constraints 328
 - 8.2 Integer Programming Algorithms 333
 - 8.2.1 Branch-and-Bound (B&B) Algorithm 334
 - 8.2.2 Cutting-Plane Algorithm 343
 - 8.2.3 Computational Considerations in ILP 348
- 8.3 Traveling Salesperson (TSP) Problem 349
 - 8.3.1 Heuristic Algorithms 353
 - 8.3.2 B&B Solution Algorithm 356

	References 367
Chapter 9	Deterministic Dynamic Programming 363
	 9.1 Recursive Nature of Computations in DP 364 9.2 Forward and Backward Recursion 367 9.3 Selected DP Applications 369 9.3.1 Knapsack/Fly-Away/Cargo-Loading Model 369 9.3.2 Work-Force Size Model 377
29% 200	9.3.3 Equipment Replacement Model 380 9.3.4 Investment Model 384 9.3.5 Inventory Models 387 9.4 Problem of Dimensionality 388 References 390
Chapter 10	Deterministic Inventory Models 391
	10.1 General Inventory Model 39110.2 Role of Demand in the Development of Inventory Models 392
	10.3 Static Economic-Order-Quantity (EOQ) Models 394 10.3.1 Classic EOQ model 394 10.3.2 EOQ with Price Breaks 400
	10.3.3 Multi-Item EOQ with Storage Limitation 404 10.4 Dynamic EOQ Models 407 10.4.1 No-Setup Model 409 10.4.2 Setup Model 413 References 425
Chapter 11	Decision Analysis and Games 427
	 11.1 Decision Making under Certainty—Analytic Hierarchy Process (AHP) 428 11.2 Decision Making under Risk 438 11.2.1 Decision Tree-Based Expected Value Criterion 438 11.2.2 Variations of the Expected Value Criterion 444 11.3 Decision under Uncertainty 453 11.4 Game Theory 458 11.4.1 Optimal Solution of Two-Person Zero-Sum Games 459 11.4.2 Solution of Mixed Strategy Games 462 References 468
Chapter 12	Queuing Systems 469
	12.1 Why Study Queues? 470

12.3 Role of Exponential Distribution 473

12.4 Pure Birth and Death Models (Relationship Between the Exponential and Poisson Distributions) 476

8.3.3 Cutting-Plane Algorithm 359

12.4.1 Pure Birth Model 476 12.4.2 Pure Death Model 480 12.5 Generalized Poisson Queuing Model 483 12.6 Specialized Poisson Queues 488 12.6.1 Steady-State Measures of Performance 489 12.6.2 Single-Server Models 493 12.6.3 Multiple-Server Models 502 12.6.4 Machine Servicing Model—(M/M/R): (GD/K/K), R<K 512 12.7 (M/G/1) : (GD/∞/∞)—Pollaczek-Khintchine (P-K) Formula 515 12.8 Other Queuing Models 517 12.9 Queuing Decision Models 517 12.9.1 Cost Models 518 12.9.2 Aspiration Level Model 522 References 524 Appendix A AMPL Modeling Language 525 A.1 Rudimentary AMPL Model 525 A.2 Components of AMPL Model 526 A.3 Mathematical Expressions and Computed Parameters 534 A.4 Subsets and Indexed Sets 537 A.5 Accessing External Files 539 A.5.1 Simple Read Files 539 A.5.2 Using Print or Printf to Retrieve Output 541 A.5.3 Input Table Files 541 A.5.4 Output Table Files 544 A.5.5 Spreadsheet Input/Output Tables 546 A.6 Interactive Commands 546 A.7 Iterative and Conditional Execution of AMPL Commands 548 A.8 Sensitivity Analysis Using AMPL 550 Reference 550

高级篇

Chapter 13 Advanced Linear Programming 551

- 13.1 Simplex Method Fundamentals 552
 - 13.1.1 From Extreme Points to Basic Solutions 554
 - 13.1.2 Generalized Simplex Tableau in Matrix Form 557
- 13.2 Revised Simplex Method 560
- 13.2.1 Development of the Optimality and Feasibility Conditions 561
 - 13.2.2 Revised Simplex Algorithm 563
- 13.3 Bounded-Variables Algorithm 569
- 13.4 Duality 575
 - 13.4.1 Matrix Definition of the Dual Problem 576
 - 13.4.2 Optimal Dual Solution 576
- 13.5 Parametric Linear Programming 580
 - 13.5.1 Parametric Changes in C 581
 - 13.5.2 Parametric Changes in **b** 584
 - References 586

Chapter 14 Review of Basic Probability 587

- 14.1 Laws of Probability 587
 - 14.1.1 Addition Law of Probability 588
 - 14.1.2 Conditional Law of Probability 589
- 14.2 Random Variables and Probability Distributions 591
- 14.3 Expectation of a Random Variable 593
 - 14.3.1 Mean and Variance (Standard Deviation) of a Random Variable 594
 - 14.3.2 Mean and Variance of Joint Random Variables 596
- 14.4 Four Common Probability Distributions 599
 - 14.4.1 Binomial Distribution 599
 - 14.4.2 Poisson Distribution 600
 - 14.4.3 Negative Exponential Distribution 601
 - 14.4.4 Normal Distribution 602
- 14.5 Empirical Distributions 605 A

Chapter 15 Probabilistic Inventory Models 613

- 15.1 Continuous Review Models 614
 - 15.1.1 "Probabilitized" EOQ Model 614
 - 15.1.2 Probabilistic EOQ Model 616
- 15.2 Single-Period Models 621
 - 15.2.1 No-Setup Model (Newsvendor Model) 621
 - 15.2.2 Setup Model (s-S Policy) 625
- 15.3 Multiperiod Model 627 References 630

	딱 가는 나를 됐는데, 가는 맛이 가게 돼요. 이렇게 하는 것이 같은 그 생각을 내려왔다. 그렇게 돼요?
	Content
Chapter 16	Simulation Modeling 631
	16.1 Monte Carlo Simulation 631
	16.2 Types of Simulation 636
	16.3 Elements of Discrete-Event Simulation 637 16.3.1 Generic Definition of Events 637
	16.3.2 Sampling from Probability Distributions 639
	16.4 Generation of Random Numbers 648
	16.5 Mechanics of Discrete Simulation 650
	16.5.1 Manual Simulation of a Single-Server Model 650
	16.5.2 Spreadsheet-Based Simulation of the Single-Server Model 656
	16.6 Methods for Gathering Statistical Observations 659
	16.6.1 Subinterval Method 660
	16.6.2 Replication Method 661
	16.6.3 Regenerative (Cycle) Method 662
	16.7 Simulation Languages 664
	References 666 MOST SOUSSAA DAIVOM T. A.
Chapter 17	Markov Chains 667
	17.1 Definition of a Markov Chain 667
	17.2 Absolute and <i>n</i> -Step Transition Probabilities 670
	17.3 Classification of the States in a Markov Chain 672
	17.4 Steady-State Probabilities and Mean Return Times of Ergodic Chains 675
	17.5 First Passago Time 600

References 689 **Chapter 18 Classical Optimization Theory**

17.6 Analysis of Absorbing States 684

18.1 Unconstrained Problems 691

18.1.1 Necessary and Sufficient Conditions 692 18.1.2 The Newton-Raphson Method 696 18.2 Constrained Problems 698 18.2.1 Equality Constraints 699 18.2.2 Inequality Constraints—Karush-Kuhn-Tucker (KKT) Conditions 711 References 716

Chapter 19 Nonlinear Programming Algorithms 717

19.1 Unconstrained Algorithms 717 19.1.1 Direct Search Method 717 19.1.2 Gradient Method 721 19.2 Constrained Algorithms 725 19.2.1 Separable Programming 725 19.2.2 Quadratic Programming 734 19.2.3 Chance-Constrained Programming 739 19.2.4 Linear Combinations Method 744

19.2.5 SUMT Algorithm 747 References 748

Chapter 20 Additional Network and LP Algorithms 749

20.1 Minimum-Cost Capacitated Flow Problem 749
20.1.1 Network Representation 750

20.1.2 Linear Programming Formulation 752

20.1.3 Capacitated Network Simplex Algorithm 757

20.2 Decomposition Algorithm 764

20.3 Karmarkar Interior-Point Method 773
20.3.1 Basic Idea of the Interior-Point Algorithm 773
20.3.2 Interior-Point Algorithm 775
References 784

Chapter 21 Forecasting Models 785

- 21.1 Moving Average Technique 785
- 21.2 Exponential Smoothing 789
- 21.3 Regression 790 References 794

Chapter 22 Probabilistic Dynamic Programming 795

- 22.1 A Game of Chance 795
- 22.2 Investment Problem 798
- 22.3 Maximization of the Event of Achieving a Goal 802
 References 805

Chapter 23 Markovian Decision Process 807

- 23.1 Scope of the Markovian Decision Problem 807
- 23.2 Finite-Stage Dynamic Programming Model 809

23.3 Infinite-Stage Model 813

- 23.3.1 Exhaustive Enumeration Method 813
- 23.3.2 Policy Iteration Method Without Discounting 816
- 23.3.3 Policy Iteration Method with Discounting 819
- 23.4 Linear Programming Solution 822 References 826

Chapter 24 Case Analysis 827

- Case 1: Airline Fuel Allocation Using Optimum Tankering 828
- Case 2: Optimization of Heart Valves Production 835
- Case 3: Scheduling Appointments at Australian Tourist
 Commission Trade Events 838
- Case 4: Saving Federal Travel Dollars 842
- Case 5: Optimal Ship Routing and Personnel Assignment for Naval Recruitment in Thailand 846
- Case 6: Allocation of Operating Room Time in Mount Sinai Hospital 852

Case 7: Optimizing Trailer Payloads at PFG Building Glass 856
Case 8: Optimization of Crosscutting and Log Allocation at
Weyerhaeuser 862
Case 9: Layout Planning for a Computer Integrated Manufacturing
(CIM) Facility 867
Case 10: Booking Limits in Hotel Reservations 874
Case 11: Casey's Problem: Interpreting and Evaluating a
New Test 877
Case 12: Ordering Golfers on the Final Day of Ryder Cup
Matches 880
Case 13: Inventory Decisions in Dell's Supply Chain 882
Case 14: Analysis of an Internal Transport System in a
Manufacturing Plant 885
Case 15: Telephone Sales Manpower Planning at Qantas
Airways 888

Statistical Tables 895

Appendix B Statistical Tables 895

Appendix C Partial Solutions to Answers Problems 899

Appendix D Review of Vectors and Matrices 949

- D.1 Vectors 949
 - D.1.1 Definition of a Vector 949
 - D.1.2 Addition (Subtraction) of Vectors 949
 - D.1.3 Multiplication of Vectors by Scalars 950
 - D.1.4 Linearly Independent Vectors 950
- D.2 Matrices 950
 - D.2.1 Definition of a Matrix 950
 - D.2.2 Types of Matrices 950
 - D.2.3 Matrix Arithmetic Operations 951
 - D.2.4 Determinant of a Square Matrix 952
 - D.2.5 Nonsingular Matrix 954
 - D.2.6 Inverse of a Nonsingular Matrix 954
 - D.2.7 Methods of Computing the Inverse of Matrix 955
 - D.2.8 Matrix Manipulations Using Excel 960
- D.3 Quadratic Forms 961
- D.4 Convex and Concave Functions 963

Problems 963

Selected References 964

Appendix E Case Studies 965

CHAPTER 1

What Is Operations Research?

Chapter Guide. The first formal activities of Operations Research (OR) were initiated in England during World War II, when a team of British scientists set out to make scientifically based decisions regarding the best utilization of war materiel. After the war, the ideas advanced in military operations were adapted to improve efficiency and productivity in the civilian sector.

This chapter will familiarize you with the basic terminology of operations research, including mathematical modeling, feasible solutions, optimization, and iterative computations. You will learn that defining the problem correctly is the most important (and most difficult) phase of practicing OR. The chapter also emphasizes that, while mathematical modeling is a cornerstone of OR, intangible (unquantifiable) factors (such as human behavior) must be accounted for in the final decision. As you proceed through the book, you will be presented with a variety of applications through solved examples and chapter problems. In particular, Chapter 24 (on the CD) is entirely devoted to the presentation of fully developed case analyses. Chapter materials are cross-referenced with the cases to provide an appreciation of the use of OR in practice.

1.1 OPERATIONS RESEARCH MODELS

Imagine that you have a 5-week business commitment between Fayetteville (FYV) and Denver (DEN). You fly out of Fayetteville on Mondays and return on Wednesdays. A regular round-trip ticket costs \$400, but a 20% discount is granted if the dates of the ticket span a weekend. A one-way ticket in either direction costs 75% of the regular price. How should you buy the tickets for the 5-week period?

We can look at the situation as a decision-making problem whose solution requires answering three questions:

- 1. What are the decision alternatives?
- 2. Under what **restrictions** is the decision made?
- 3. What is an appropriate objective criterion for evaluating the alternatives?

2 Chapter 1 What Is Operations Research?

Three alternatives are considered:

- 1. Buy five regular FYV-DEN-FYV for departure on Monday and return on Wednesday of the same week.
- 2. Buy one FYV-DEN, four DEN-FYV-DEN that span weekends, and one DEN-FYV.
- 3. Buy one FYV-DEN-FYV to cover Monday of the first week and Wednesday of the last week and four DEN-FYV-DEN to cover the remaining legs. All tickets in this alternative span at least one weekend.

The restriction on these options is that you should be able to leave FYV on Monday and return on Wednesday of the same week.

An obvious objective criterion for evaluating the proposed alternative is the price of the tickets. The alternative that yields the smallest cost is the best. Specifically, we have

Alternative 1 cost = $5 \times 400 = 2000

Alternative 2 cost = $.75 \times 400 + 4 \times (.8 \times 400) + .75 \times 400 = 1880

Alternative $3 \cos t = 5 \times (.8 \times 400) = 1600

Thus, you should choose alternative 3.

Though the preceding example illustrates the three main components of an OR model—alternatives, objective criterion, and constraints—situations differ in the details of how each component is developed and constructed. To illustrate this point, consider forming a maximum-area rectangle out of a piece of wire of length L inches. What should be the width and height of the rectangle?

In contrast with the tickets example, the number of alternatives in the present example is not finite; namely, the width and height of the rectangle can assume an infinite number of values. To formalize this observation, the alternatives of the problem are identified by defining the width and height as continuous (algebraic) variables.

Let

w =width of the rectangle in inches

h =height of the rectangle in inches

Based on these definitions, the restrictions of the situation can be expressed verbally as

- 1. Width of rectangle + Height of rectangle = Half the length of the wire
- 2. Width and height cannot be negative

These restrictions are translated algebraically as

1.
$$2(w+h) = L$$

2.
$$w \ge 0, h \ge 0$$