DYNAMIC MODELLING AND CONTROL OF NATIONAL ECONOMIES

J. M. L. JANSSEN L. F. PAU A. J. STRASZAK

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DYNAMIC MODELLING AND CONTROL OF NATIONAL ECONOMIES

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INTRODUCTION

This Conference was the third in the series of IFAC/IFORS conferences on dynamic modelling and control of national economies, following the first in Warwick, United Kingdom (1973), and the second, also sponsored by IIASA, in Vienna, Austria (1977). The third conference was also sponsored by the Society for Economic Dynamics and Control as a participant. According to present plans the fourth conference will be held in the USA in 1983.

On behalf of the Polish National Member Organization of IFAC, the conference was organized by the Systems Research Institute of the Polish Academy of Sciences. As hosts of about 182 participants from 27 countries they made very successful local arrangements.

The wide variety of contributions to the conference, including 2 round-table discussions, some 60 papers divided over plenary sessions and many parallel sessions, and lively discussions, were evidence of the strength and growth in the areas of economic modelling, control techniques; and their use for planning and decision making.

The International Program Committee under the chairmanship of Professor Z. Pawlowski emphasized very strongly that the selected papers should include numerical results and experience of practical implementation.

whereas the individual papers in these proceedings dealing with special subjects may appear to be widely scattered over the whole field, in the round tables and discussions a pattern emerged of what the successes and limitations were of this approach, thus pointing also at areas for further research. This will be summarized below in the sections on

- Interaction between decision making and model building
- Enhancing model credibility and applicability.

The third section gives a summary of the main topics of the conference, since reports of the discussions in the various sessions were not available in full detail. However, thanks to the efforts of Dr. Cichocki and Dr. Owsinski, detailed reports of the two round-table discussions have been included in this volume.

For various administrative and editorial reasons not all papers presented at the conference could be included in the proceedings. Other papers were included after minor or major revision of the text as originally submitted, often complicated by problems of language or channels of communication. The editors very much appreciate the co-operation of the authors in this matter. They sincerely hope that a reasonable balance has been struck between perfection and timeliness.

The papers have been grouped in ... accordance with the sessions of the conference.

INTERACTIONS BETWEEN DECISION MAKING AND MODEL BUILDING.

Decision making is usually a very complex process, of which model building is one of many parts, and model builders are few of many actors. It is their specific responsibility to clarify complex issues by means of formal methods and in this manner to supply the other actors with additional information. In this connection several points were made:

- The buying / selling relationship between the model builders and the others may lead to selling models that provide justification for pre-conceived ideas, rather than models that are well-tested results of scientific investigations under clearly specified assumptions.
- There is a difference in background and perspective between the model builders and those who are responsible for executing the decisions. The question was raised to what extent model builders could become involved in taking the actions, so that they would get personal experience of real-life mechanismes. This would also reduce the danger of building "a big model for the boss", not necessarily agreeable to the rank and file.
- The gap between model builders and others might also be bridged by "interpreters" who derive their credibility from working in responsible

advisory positions close to the decision makers, as well as from being knowledgeable in the process of model building through education and experience. On the one hand their participation in decision and policy generation should expose them to the facts of life. On the other hand, they should keep close contacts with the community of model builders.

- Decision making at a central position in combination with model building with a corresponding degree of aggregation, does not necessarily lead to the expected decentralized actions.

- In decision making, empirical rules of thumb may be used by lack of something better. It is one of the roles of model building to verify or reject these rules, with the hopeful ultimate result of improved designs of qualitative or quantitative instruments for decision making.

ENHANCING MODEL CREDIBILITY AND APPLICABILITY.

In the Scientific community two views prevail, and both are legitimate:

Model building as a scientific activity for its own sake. Then applicability is not the major issue. Credibility requires that models can stand the test of scrutiny by the scientific community.

Thus, it was said that

- * no model should be published without a track record
- * a multiplier analysis should be made
- * the data base should be made available.
- Model building as part of the decision-making process. This type of model building was, in fact, the theme of this conference. Applicability is a major issue, and effectiveness dominates scientific rigour: "the final test of a theory is its ability to solve the problems that originated it" (George Dantzig).

In connection with the second view several points were made:

 Economic models were said to be notoriously unstable, in the sense that changing economic

- conditions require frequent structural and numerical model changes. Consequently, there are diminishing returns on increasing the size of economic models.
- There may be competing models, on the basis of intuitively equally obvious assumptions, but showing different system behaviour. Model selection by statistical tests is usually not conclusive.
- In forecasting, univariate models may be competitive with economic models. However, univariate models say nothing of causal relations between control actions and responses. Since in day-to-day activities control is to be effected by coherent sequential decisions, development of theory and building tools for short-term causal models needs more attention.
- Models, even competing models, have an educational impact on the organization, even if none of them will eventually be used.
- The importance of the time horizon was stressed. At least the first step should be taken in the right direction; this direction needs to be known within a certain range. In this sense the long-term goals and effects are a crucial factor. Model builders should be aware of possible conflicts between short-term decisions and long-term goals.
- Good data quality is required because of the "garbage in garbage out" rule. The question is to what extent model builders should contribute to the specifications and rules at the data collection level.

The two views can be harmonized by maintaining scientific rigour as far as possible, since nothing is more practical than good theory. To achieve this, a long-term effort is required geared at specific education (graduate and post-graduate) in dynamic modelling and control of economic systems. This education should be offered in economics, engineering and social studies.

Introduction xiii

MAIN TOPICS OF THE CONFERENCE

Theory of modelling

The papers covered a broad class of problems arising in both the theory and the practice of modelling various economic systems.

The main issues discussed were:
- model representations (digraphs,
 two-level control systems, hybrid
 models, subjective information
 modelling);

 solution concepts (experimential solutions, pseudo-inverses, game theory, stochastic solutions and disturbances, general equilibrium models).

National models

The main issues raised were:

- changing model structures;

- modelling of institutional intervention in countries with planned economies;
- choice of weights in the criterion functions;
- use of explicit inequality constraints versus replacement by penalties in the criterion. function;
- effect of data inaccuracies on feed-back control;
- interpretation of residuals and dummy variables in estimated relations;
- estimation of rational expectations and uniqueness of a response to external shocks.

Sectoral Models

Presentations covered such sectors as energy, health care, and agriculture. They addressed mainly the issues of interaction between sectors and decision levels, as well as sector stability.

Regional models

The main emphasis was on:

- the co-ordination between national and regional planning processes;
- the effects of demographic changes and migrations (especially on urban areas);
- the existence of multiple technology levels distributed within the same sectors throughout regions (e.g. agriculture, energy);
- the environmental effects.

The need was stressed for this area to make a larger use of interactive tools, of gaming approaches, and of multiple-criteria planning.

Monetary and fiscal models

This session included three nonlineair aggregate models of the effects of financial controls (monetary, fiscal) on economic activity, with optimization and simulation results. The issues of intermediate targets and causality relations were also discussed.

Econometric forecasting and estimation

Progress was reported on a variety of econometric estimation procedures: regression methods; spectral analysis; forecasting error compensation. A large interest was shown in various uses of adaptive estimation, e.g. by Kalman filtering.

Optimization methods

Besides a presentation of various algorithms, a number of possible criteria were discussed: state trajectories; integral performance indexes; qualitative criteria.

Software tools for macroeconomic models and analysis

Besides a methodological analysis of structural and parametric sensitivity, a number of estimation, optimization and data-base handling packages were described. The discussion went on about ways of designing user-friendly packages for economists.

CONCLUSION

This conference again witnessed the role and importance of bringing together model builders, decision makers, economists, and engineers, from various countries and organizations, for the sake of progress in this important area. Since dynamic modelling and control of national, regional, and sectoral economies is an art built on science, discussion and presentation of a multiplicity of approaches are essential for good decision making and international co-operation.

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CONTENTS

Introduction	хi
PLENARY SESSIONS	
Non-price Control Bela Martos	· 1
Design and Testing of Economic Policy in a Mixed Economy J. Bray	11
Optimization and Balance of National Economy Models K. K. Val* tukh	21
ROUND TABLES	÷
Dynamics and Control of Economic Modelling Chairman: Bela Martos; Reporter: K. Cichocki	31
Interaction between Decision Makers and Model Builders Chairman: J. Bray; Reporter: J. W. Owsinski	35
SPECIAL INTEREST SESSIONS	
NATIONAL MODELS	4°
A Demoeconometric Model of Poland and its Simulations Z. Pawlowski	37
Interplay: A Linked Model for Economic Policy in the EEC J. E. J. Plasmans	43
On Optimal Macro-Economic Control with Inaccurate Data J. A. Eklof	57
An Application of the Generalized Inverse in Input-Output and Macroeconomic Analysis K. P. Vishwakarma	63
Optimal and Suboptimal Controls of a Canadian Model C. L. Sandblom, J. L. Banasik	71
System of Models for Medium Term Planning of National Economy 2. Czerwiński, W. Jurek, E. Panek, W. Sledziński	79
Optimal Control and Policy Analysis with a Model of a Small Open Economy. The Case of Ireland J. Bradley, C. O'Raifeartaigh	85
Rational Expectations and the Scope for an Optimal Fiscal Policy in a Simple Model of an Open Economy: Some Numerical Results S. Holly	91
A Growth Model of the Danish Economy T. V. Rasmussen, N. Kaergård	99
Optimization Techniques in Modelling of Economic Policy K. Cichocki	105

Dynamic Factor Models of the Hungarian National Economy G. Bankovi, J. Veliczky, M. Ziermann	117
Inforum-IIASA System of National Economic Models D. E. Nyhus	123
SECTORAL MODELS	
A Multisectoral Stochastic Optimal Control Model for UK to Derive Future Energy Policies D. R. Basu	129
A Planning Model for the Optimal Development of the Greek Energy Sector $J.\ E.\ Samouilidis$. 141
An Optimal Management in Health Care System M. Bojańczyk	151
Agricultural Policy Planning with Programming Models: Problems of Centralized Planning in Decentralized Decision Situations G. Schiefer	157
Econometric Forecasting by a Fertilizer Sectoral Model S. Mészáros	163
Economic Industry Model Building: The Synthetic Fibres Case A. Alessandroni, C. Leporelli, G. M. Rey	169
Simulation Analysis of Goods Flows Stability in the Food Products Distribution System J. Szumilak, B. Wasik	177
REGIONAL MODELS	
Modelling the Processes of Co-ordinating National Economic and Regional Planning Decisions A. Granberg	187
Modelling of Rural-Urban Development R. Kulikowski	195
Regional Energy Modelling C. Mattsson, J. A. Bubenko	201
A Man-Machine Interactive Sensitivity Analysis Feature for the Kinki	
Regional Model K. Shoji, H. Kamitani, Y. Suzuki, T. Ainai, T. Shiina	207
Modelling of Geographical Distribution of Population in a Region and its Application for Regional Planning H. Ishitani, Y. Kayano, Y. Ohya, N. Hyodo	213
Regional Agricultural Policy Design on the Basis of a Detailed Linear . Economic and Agrotechnical Model M. M. Albegov, J. Kacprzyk, J. W. Owsinski, A. Straszak	221
Imbedding Perceptions of Regional Problems in the Integrated Modelling Framework A. Straszak, J. W. Owsinski	231
MONETARY AND FISCAL MODELS	•
Optimal Instruments for Monetary Control E. Karakitsos, M. B. Zarrop, B. Rustem	247
Monetary and Fiscal Policy in a Small Open Economy G. Chiesa	253
Is There a Stable Demand for Money?: A Critical View of the "Independence Phenomenon"	263

ECONOMETRIC	PORFCASTING	AND	ESTIMATION

Adaptive Models in Econometric Forecasting A. Badach	271
Forecasting and Simulation by Controlled Dynamic Factors of Open Economies G. Posta, J. Velicsky	279
Comparative Analysis of Dynamic Factor Models of Current and Constant Prices E. Berde	285
Estimation of Econometric Models by Kalman Filtering and Iterative Instrumental Variables R. Aagaard-Svendsen	291
Assessing the Quality of Prediction Baykal: Bayesian Prediction by Kalman-Filtering G. Paass	297
Identification and Estimation of Linear (Economic) Systems, Operating under Linear Cloosed-Loop Control P. W. Otter	305
Standard Errors of Multipliers and Forecasts from Structural Coefficients with Block-Diagonal Covariance Matrix C. Bianchi, G. Calsolari, P. Corsi	311
Using Kalman Filtering for Energy Forecasting C. S. Mitropoulos, J. E. Samouilidis, E. N. Protonotarios	317
OPTIMIZATION THEORY	
The Qualitative Design of Economic Policies and Planner-Model Interaction A. J. H. Hallet	325
A Non-Terminal Control Approach to Dynamic Economic Modelling in Non-Compact Space V. Rupnik, S. Strmönik, R. Karba, F. Bremšak	333
On Some Advantages of the Application of Newton's Method for the Solution of Nonlinear Economic Models G. Bock von Wilfingen	339
A Newton-Type Algorithm for a Class of N-Player Dynamic Games Using Nonlinear Econometric Models B. Rusten, M. B. Zarrop	349
THEORY OF MODELLING	
Qualitative Hierarchies Among Variables of a Macroeconomic Decision Model D. Royer	355
Stochastic Optimal Control by Pseudoinverse. An Application A. S. Lazaridis and D. R. Basu	361
Planning Model with Decentralized Structure of Decision Making B. Tolwiński, J. Sosnowski	367
Formal Designing of Stochastic Control Linear Systems 2. H. Hellwig	375
Hybrid Models of Statistical Economics M. A. Yagolniteer	379
The Principle of a Guaranteed Result in Problems of Economic Control A. G. Mikhailov, V. V. Tokarev	383
SOFTWARE TOOLS	
Econometric Input-Output Tables Data Base A. Diediw, D. Nudds	387

Contents

Combining an Optimal Control Program with the Time Series Processor System A. Drud	399
Moduleco: An Integrated, Modular Computer System for Economists A. Tarabout, F. Rechenmann, B. Sefsaf	405
Parameter and Structural Sensitivity of Econometric Models P. J. Vermeulen	411

NON-PRICE CONTROL Report on a Research Trend

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Abstract. The paper reports on a line of studies conducted by 8 Hungarian researchers. Their work deals with simple (vegetative) control mechanisms of a multi-agent economy with the following characteristics: control signals are mostly of the non-price type (stocks, orders), norms or normal paths are used as command signals, linear feedback control is applied. The 20 models are analysed with respect to stability and viability of the system as well as to the degree of decentralization of information flow and decision structure. The differences among the approaches lie in the control signals, the response functions, time lags, deterministic vs stochastic behaviour, constant vs variable parameters, etc.

<u>Keywords.</u> Economics; models; multivariable control systems; stock-control; stability; decentralized control.

INTRODUCTION

In this paper a sketchy overview of a research trend is given dealing with different control mechanisms of the economy. The purpose of the research is to lay foundations to the study of some components of the economic control systems - more or less neglected in the literature, where prices were considered as the typical information source on which economic decisions are based.

The contributors to this research are:
A. Bródy, I. Dancs, E. Hunyadi,
Zs. Kapitány, J. Kornai, B. Martos,
A. Simonovits, J. Sivák.

The results are being published in the forthcoming book; J. Kornai and B. Martos (Editors): Non-Price Control (1981) Akadémiai Kiadó, Budapest and North-Holland Publ. Co. Amsterdam. The present paper is essentially a digest of this book.

THEORETICAL BACKGROUND

Antecedents

The four lines of thinking which preceded and influenced our research are depicted in Fig. 1. The drawback of this foursome inspiration is that

we must often apply many unrealistic assumptions inherited from these various disciplines.

Some Basic Concepts and Characteristics

Real sphere vs control sphere. Following Kornai (1971) we always make a clear distinction, separation of the real processes of the economy (as production, transfer of goods, consumption) and the control processes accompanying them (as information processing, decision making, fiscal and monetary processes etc.). Accordingly from an organizational point of view we assume each organization to include a <u>real unit</u> in which the real processes take place and a <u>control</u> unit which directs the real processes within the organization and may be in an informational connection with control units of other organizations Moreover organizations are classified in two groups: real organizations whose, main activity is to perform real tasks (as productive firms, households, etc.) and control organizations whose real activity is negligible and are organized to perform control functions (as a statistical office, a planning office, a bank, a ministry, etc.).

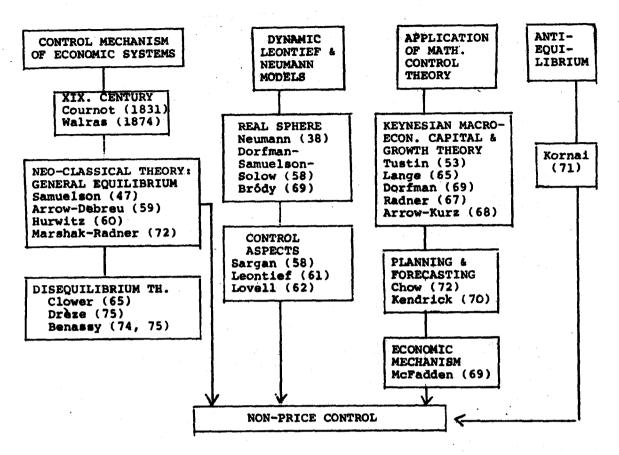


Fig. 1. Antecedents

Off-line vs on-line control. In many models of the real sphere (e.g. Walras, Neumann) control variables (e.g. prices) appear as byproducts which have no effect whatsoever on real processes. If we consider the tatonnement process of the Walrasian auctionnaire or the interpretation of the decomposition algorithms of linear programming as abstract control processes, then we observe that the time stops as long as these control processes run their course. The nonequilibrium or non-optimal prices and production programs which are consecutively produced in this process do not influence the real processes, they control off-line. In our models the control is on-line, the clocks are not stopped, real and control processes run simultaneously and influence each other whether they are on the equilibrium/optimum level or not.

Secular vs historically limited dynamics. We deal with systems differing in the institutional framework, behavioural characteristics,

normal states but for each of them all these are fixed. This means that the dynamic framework of each model is a historically limited one. We ask only the question, how the systems operate under given conditions, and neglect the secular dynamics, i.e. how the institutions, behavioural rules, norms develop in the historical time, where learing, self-adjustment and self-organization also exert effect on the economic-social system.

Control by norms vs optimal control. In our models control by norm is the basic approach. This includes the assumptions that for some state and/or control variables there exist norms (or normal paths, if variable in time) as the accepted or customary value of a variable, around which the actual value is taken on the effect of the operating control. The behaviour of the participants are assumed to show up some regularity, but it is not required that this behaviour should be an optimising one. This is why we do not rely on the more modern and fashionable theory of optimal processes.

Descriptive theory vs normative theory. Our purpose is to describe the functioning of the economy (or more modestly: some aspects thereof) and analyse models which reflect possible representations of this functioning, rather then tell, how the economic agents and institutions should behave, what rules are desirable to follow. This is also connected with another dichotomy: we deal with economic mechanism and not with finding a satisfactory (or optimal) economic policy, to which the most effort in the application of control theory to economics has been directed in the past.

Centralization vs Decentralization

We found the usual dichotomy between decentralized and centralized control inadequate to the classification of systems. Therefore a more detailed classification scheme has been elaborated by Kornai and Martos.

Elementary processes. The part of a complex control process which is not further divided into parallel or subsequent subprocesses is an elementary process. From the point of view of the signal formation an elementary process may be

- isolated, if the signal is formed by the control unit of a single real organization
- interactive, if it is formed jointly by control units of several real organizations
- centralized, if it is formed by one or more control organizations. (A common name for interactive or centralized processes is: coordinated.)

From the point of view of signal transfer the elementary process may be

- non-communicative, if the signal does not leave the organization where it originated
- transactionally communicative, if the signal is transmitted between a pair of real organizations and refers to an actual or potential real-transaction (usually transfer of goods or services) between this pair. (E.g. price offers, bills, orders, etc.)
- non-transactionally communicative in any other case (especially if a control organization is involved).

Combining signal formation with transfer some combinations are incompatible as Table 1. shows.

Classification of Elementary TABLE 1 Control Processes

Signal forma- tion transfer	Iso- lated	Coordinated		
		Inter- active	Cen- tralized	
Non-commu- nicative	+	Ø	+	
Transactional- ly commu- nicative	+	+	ø	
Non-trans- actionally commu- nicative	+	+	+	

Complex control processes are composed of elementary processes possibly belonging to different classes of the above classification. Thus it is not generally possible to tell if a complex process is more or less centralized than another. Still we formed 5 stages of typical forms in growing order of centralization.

The term vegetative in these definitions refers to systems consisting of elementary processes which are all isolated and either non-communicative or transactionally communicative. The five stages are then:

- Vegetative, non-communicative
- II. Vegetative, communicative (transactionally)
- III. Interactive
- IV. Partially centralized (Policentric)
 - V. Monocentric

Points of View of the Analysis

Our models will be analysed according to the following criteria:

- Stability Analysis
 Viability Analysis (usually nonnegativity of some variables)
- Structural Analysis
- Comparative Analysis (Similarity, Equivalence)

Notation

n = No, of sectors or products

q(t) = output stock vector

V(t) = input stock matrix

r(t) = production vector

Y(t) = commodity transfer matrix

c(t) = consumer's demand vector
 (observable, uncontrollable)

A(t) = input coefficient matrix, $<math>\rho(A) \le 1$. A is indecomposable

p(t) = price vector

1 = [1,1,...,1]', the summation
 vector.

MODELS WITH CONSTANT NORMS: STOCK, PRICE, PROFIT

This chapter deals with linear control models where the real sphere is an open or closed Leontief economy, the control is based on stock signals or intermediate signals derived from them, and the controller is of the integrating or integrating plus proportional type. Some of the models work with continuous time and without lag, some with discrete time and uniform lags.

Models of Kornai and Martos (1971, 1973)

The first attempts to establish models of vegetative control resulted in two models. Here we give simplified versions of them, a more complete analysis can be found in Kornai and Martos (1973). An open Leontfef model $f_{\rho}(A) < 11$ is controlled here by two types of control.

The real process

$$\dot{q} = r - Y_1 - c$$
 (Output stock balance) (1)

$$\dot{V} = Y-A < r > (Input stock balance), (2)$$

where $\langle r \rangle$ is the diagonal matrix formed from vector r.

The control process

$$\dot{r} = \dot{Y}_1 + \dot{c} + \gamma^2 (q^4 - q) - 2\beta \gamma \dot{q}$$
 (Production control)

$$\dot{Y} = A < \dot{r} > + \dot{A} < \dot{r} > + \dot{\gamma}^2 (\dot{V}^* - \dot{V}) - 2\beta \dot{\gamma} \dot{V}$$
 (Control of transfers)

where $^{\pm}$ arterisk refers to the normal value of a variable. For $\beta=0$ the scheme represents an integrating control, while for $\beta\neq0$ we have an additional proportional term.

Stability analysis. The pure integral control is Ljapunov-stable but not assymptotically stable, the integral plus proportional control is asymptotically stable for β , γ > 0.

Viability analysis. q > 0, V > 0 and r > 0 if (sufficient conditions)

$$0 < \beta < 1$$

 $\gamma > \frac{1}{\sqrt{1-\beta^2}} \phi ((r^0, Y^0, q^0, V^0))$

$$c_{\mathbf{i}}(t) > \frac{1}{\sqrt{1-\beta^2}} |r_{\mathbf{i}}^{\mathsf{O}} - \Sigma \mathbf{A}_{\mathbf{i}j}^{\mathsf{O}} r_{\mathbf{j}}^{\mathsf{O}} - c_{\mathbf{i}}^{\mathsf{O}}|$$
for $i=1,2,\ldots,n$ and $t \stackrel{>}{=} 0$,

where the superscript orefers to the initial values at t=0 and or is a complicated function of the initial values.

Structural analysis. The system is vegetative and non-communicative.

The main lesson drawn from this analysis is the existence of a vegetative and non-communicative control scheme which can be constructed in such a way that the system is stable and viable.

Models of Dancs, Hunyadi and Sivák (1973)

They studied discrete variants of the Kornai-Martos models replacing simply the differential operators by difference operators and hereby introducing one unit time lag in the Control process.

The analysis showed that the discrete variant of the integral control became unstable, while the stability domain for the values of β , γ in the discrete variant of the integral plus proportional control is more restricted than in the continuous case. (See Fig. 2.)

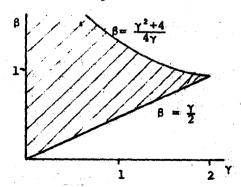


Fig. 2. Stability domain for the discrete variant of the integral plus proportional control