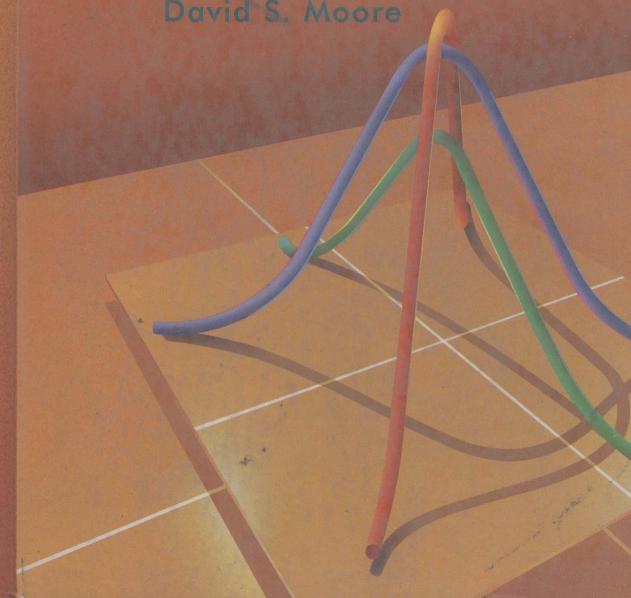
# The BASIC PRACTICE of STATISTICS





C81



# THE BASIC PRACTICE OF STATISTICS

David S. Moore

Purdue University

15

W. H. FREEMAN AND COMPANY New York

## Library of Congress Cataloging-in-Publication Data

Moore, David S.

The basic practice of statistics / David S. Moore.

p. cm.

Includes index.

ISBN 0-7167-2628-9

1. Statistics. I. Title.

QA276.12.M648 1994

519.5—dc20

94-40756

CIP

©1995 by W. H. Freeman and Company

No part of this book may be reproduced by any mechanical, photographic, or electronic process, or in the form of a phonographic recording, nor may it be stored in a retrieval system, transmitted, or otherwise copied for public or private use, without written permission from the publisher.

Printed in the United States of America

Sixth printing 1997

Line       101     19223     95034     05756     28713     96409     12531     42544       102     73676     47150     99400     01927     27754     42648     82425       103     45467     71709     77558     00095     32863     29485     82226       104     52711     38889     93074     60227     40011     85848     48767       105     95592     94007     69971     91481     60779     53791     17297       106     68417     35013     15529     72765     85089     57067     50211       107     82739     57890     20807     47511     81676     55300     94383       109     60040     73034     17669     24043     61700     20656     27064	82853 36290 90056 52573 59335 47487 14893 18883 41979
102     73676     47150     99400     01927     27754     42648     82425       103     45467     71709     77558     00095     32863     29485     82226       104     52711     38889     93074     60227     40011     85848     48767       105     95592     94007     69971     91481     60779     53791     17297       106     68417     35013     15529     72765     85089     57067     50211       107     82739     57890     20807     47511     81676     55300     94383	36290 90056 52573 59335 47487 14893 18883
103     45467     71709     77558     00095     32863     29485     82226       104     52711     38889     93074     60227     40011     85848     48767       105     95592     94007     69971     91481     60779     53791     17297       106     68417     35013     15529     72765     85089     57067     50211       107     82739     57890     20807     47511     81676     55300     94383	90056 52573 59335 47487 14893 18883
104     52711     38889     93074     60227     40011     85848     48767       105     95592     94007     69971     91481     60779     53791     17297       106     68417     35013     15529     72765     85089     57067     50211       107     82739     57890     20807     47511     81676     55300     94383	52573 59335 47487 14893 18883
105     95592     94007     69971     91481     60779     53791     17297       106     68417     35013     15529     72765     85089     57067     50211       107     82739     57890     20807     47511     81676     55300     94383	59335 47487 14893 18883
106     68417     35013     15529     72765     85089     57067     50211       107     82739     57890     20807     47511     81676     55300     94383	47487 14893 18883
107 82739 57890 20807 47511 81676 55300 94383	14893 18883
	18883
100 60040 73034 17060 34043 61700 00666 07064	
108 60940 72024 17868 24943 61790 90656 87964	41979
109 36009 19365 15412 39638 85453 46816 83485	
110 38448 48789 18338 24697 39364 42006 76688	08708
111 81486 69487 60513 09297 00412 71238 27649	39950
112 59636 88804 04634 71197 19352 73089 84898	45785
113 62568 70206 40325 03699 71080 22553 11486	11776
114 45149 32992 75730 66280 03819 56202 02938	70915
115 61041 77684 94322 24709 73698 14526 31893	32592
116 14459 26056 31424 80371 65103 62253 50490	61181
117 38167 98532 62183 70632 23417 26185 41448	75532
118 73190 32533 04470 29669 84407 90785 65956	86382
119 95857 07118 87664 92099 58806 66979 98624	84826
120 35476 55972 39421 65850 04266 35435 43742	11937
121 71487 09984 29077 14863 61683 47052 62224	51025
122 13873 81598 95052 90908 73592 75186 87136	95761
123 54580 81507 27102 56027 55892 33063 41842	81868
124 71035 09001 43367 49497 72719 96758 27611	91596
125 96746 12149 37823 71868 18442 35119 62103	39244
126 96927 19931 36809 74192 77567 88741 48409 127 43909 99477 25330 64359 40085 16925 85117	41903
127     43909     99477     25330     64359     40085     16925     85117       128     15689     14227     06565     14374     13352     49367     81982	36071
129 36759 58984 68288 22913 18638 54303 00795	87209
130 69051 64817 87174 09517 84534 06489 87201	08727 97245
130 09031 04617 67174 09317 64334 00469 87201 131 05007 16632 81194 14873 04197 85576 45195	96565
132 68732 55259 84292 08796 43165 93739 31685	97150
133 45740 41807 65561 33302 07051 93623 18132	09547
134 27816 78416 18329 21337 35213 37741 04312	68508
135 66925 55658 39100 78458 11206 19876 87151	31260
136 08421 44753 77377 28744 75592 08563 79140	92454
137 53645 66812 61421 47836 12609 15373 98481	14592
138 66831 68908 40772 21558 47781 33586 79177	06928
139 55588 99404 70708 41098 43563 56934 48394	51719
140 12975 13258 13048 45144 72321 81940 00360	02428
141 96767 35964 23822 96012 94591 65194 50842	53372
142 72829 50232 97892 63408 77919 44575 24870	04178
143 88565 42628 17797 49376 61762 16953 88604	12724
	00900
145 19687 12633 57857 95806 09931 02150 43163	58636
146 37609 59057 66967 83401 60705 02384 90597	93600
147 54973 86278 88737 74351 47500 84552 19909	67181
148 00694 05977 19664 65441 20903 62371 22725	53340
	88692
150 07511 88915 41267 16853 84569 79367 32337	03316

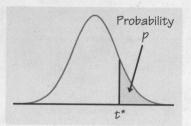


Table entry for p and C is the critical value  $t^*$  with probability p lying to its right and probability C lying between  $-t^*$  and  $t^*$ .

df 1	25 1.000	.20			T.T							
		20		Upper tail probability p								
1	1 000		.15	.10	.05	.025	.02	.01	.005	.0025	.001	.0005
1	1.000	1.376	1.963	3.078	6.314	12.71	15.89	31.82	63.66	127.3	318.3	636.6
2	0.816	1.061	1.386	1.886	2.920	4.303	4.849	6.965	9.925	14.09	22.33	31.60
3	0.765	0.978	1.250	1.638	2.353	3.182	3.482	4.541	5.841	7.453	10.21	12.92
4	0.741	0.941	1.190	1.533	2.132	2.776	2.999	3.747	4.604	5.598	7.173	8.610
5	0.727	0.920	1.156	1.476	2.015.	2.571	2.757	3.365	4.032	4.773	5.893	6.869
6	0.718	0.906	1.134	1.440	1.943	2.447	2.612	3.143	3.707	4.317	5.208	5.959
7	0.711	0.896	1119	1.415	1.895	2.365	2.517	2.998	3.499	4.029	4.785	5.408
8	0.706	0.889	1.108	1.397	1.860	2.306	2.449	2.896	3.355	3.833	4.501	5.041
9	0.703	0.883	1.100	1.383	1.833	2.262	2.398	2.821	3.250	3.690	4.297	4.781
10	0.700	0.879	1.093	1.372	1.812	2.228	2.359	2.764	3.169	3.581	4.144	4.587
11	0.697	0.876	1.088	1.363	1.796	2.201	2.328	2.718	3.106	3.497	4.025	4.437
12	0.695	0.873	1.083	1.356	1.782	2.179	2.303	2.681	3.055	3.428	3.930	4.318
13	0.694	0.870	1.079	1.350	1.771	2.160	2.282	2.650	3.012	3.372	3.852	4.221
14	0.692	0.868	1.076	1.345	1.761	2.145	2.264	2.624	2.977	3.326	3.787	4.140
15	0.691	0.866	1.074	1.341	1.753	2.131	2.249	2.602	2.947	3.286	3.733	4.073
16	0.690	0.865	1.071	1.337	1.746	2.120	2.235	2.583	2.921	3.252	3.686	4.015
17	0.689	0.863	1.069	1.333	1.740	2.110	2.224	2.567	2.898	3.222	3.646	3.965
18	0.688	0.862	1.067	1.330	1.734	2.101	2.214	2.552	2.878	3.197	3.611	3.922
19	0.688	0.861	1.066	1.328	1.729	2.093	2.205	2.539	2.861	3.174	3.579	3.883
20	0.687	0.860	1.064	1.325	1.725	2.086	2.197	2.528	2.845	3.153	3.552	3.850
21	0.686	0.859	1.063	1.323	1.721	2.080	2.189	2.518	2.831	3.135	3.527	3.819
22 23	0.686	0.858	1.061	1.321	1.717	2.074	2.183	2.508	2.819	3.119	3.505	3.792
24	0.685	0.858 0.857	1.060	1.319	1.714	2.069	2.177	2.500	2.807	3.104	3.485	3.768
25	0.684	0.856	1.059	1.318	1.711	2.064	2.172	2.492	2.797	3.091	3.467	3.745
26	0.684	0.856	1.058	1.316	1.708	2.060	2.167	2.485	2.787	3.078	3.450	3.725
27	0.684	0.855	1.057	1.313	1.706	2.056	2.162	2.479	2.779	3.067	3.435	3.707
28	0.683	0.855	1.056	1.313	1.703 1.701	2.052 2.048	2.158	2.473	2.771	3.057	3.421	3.690
29	0.683	0.854	1.055	1.313	1.699	2.045	2.154 2.150	2.467	2.763	3.047	3.408	3.674
30	0.683	0.854	1.055	1.310	1.697	2.042		2.462	2.756	3.038	3.396	3.659
40	0.681	0.851	1.050	1.303	1.684	2.021	2.147 2.123	2.457	2.750	3.030	3.385	3.646
50	0.679	0.849	1.030	1.299	1.676	2.021	2.123	2.423 2.403	2.704 2.678	2.971 2.937	3.307 3.261	3.551
60	0.679	0.848	1.045	1.296	1.671	2.009	2.109	2.403	2.660	2.937		3,496
80	0.678	0.846	1.043	1.292	1.664	1.990	2.099	2.374	2.639	2.915	3.232	3.460
100	0.677	0.845	1.042	1.290	1.660	1.984	2.080	2.364	2.626	2.871	3.195 3.174	3.416 3.390
1000	0.675	0.842	1.037	1.282	1.646	1.962	2.056	2.330	2.581	2.813	3.098	3.300
z*	0.674	0.841	1.036	1.282	1.645	1.960	2.054	2.326	2.576	2.807	3.098	3.291
	50%	60%	70%	80%	90%	95%	96%	98%	99%	99.5%	99.8%	99.9%
					Co	nfiden	e level	С				

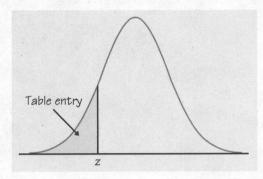


Table entry for z is the area under the standard normal curve to the left of z.

TABL	E A St	andard	normal	probabil	lities					
z	.00	.01	.02	.03	.04	.05	.06	.07	.08	.09
-3.4	.0003	.0003	.0003	.0003	.0003	.0003	.0003	.0003	.0003	.0002
-3.3	.0005	.0005	.0005	.0004	.0004	.0004	.0004	.0004	.0004	.0003
-3.2	.0007	.0007	.0006	.0006	.0006	.0006	.0006	.0005	.0005	.0005
-3.1	.0010	.0009	.0009	.0009	.0008	.0008	.0008	.0008	.0007	.000
-3.0	.0013	.0013	.0013	.0012	.0012	.0011	.0011	.0011	.0010	.0010
-2.9	.0019	.0018	.0018	.0017	.0016	.0016	.0015	.0015	.0014	.001
-2.8	.0026	.0025	.0024	.0023	.0023	.0022	.0021	.0021	.0020	.0019
-2.7	.0035	.0034	.0033	.0032	.0031	.0030	.0029	.0028	.0027	.002
-2.6	.0047	.0045	.0044	.0043	.0041	.0040	.0039	.0038	.0037	.003
-2.5	.0062	.0060	.0059	.0057	.0055	.0054	.0052	.0051	.0049	.004
-2.4	.0082	.0080	.0078	.0075	.0073	.0071	.0069	.0068	.0066	.006
-2.3	.0107	.0104	.0102	.0099	.0096	.0094	.0091	.0089	.0087	.008
-2:2	.0139	.0136	.0132	.0129	.0125	.0122	.0119	.0116	.0113	.011
-2.1	.0179	.0174	.0170	.0166	.0162	.0158	.0154	.0150	.0146	.014
-2.0	.0228	.0222	.0217	.0212	.0207	.0202	.0197	.0192	.0188	.018
-1.9	.0287	.0281	.0274	.0268	.0262	.0256	.0250	.0244	.0239	.023
-1.8	.0359	.0351	.0344	.0336	.0329	.0322	.0314	.0307	.0301	.029
-1.7	.0446	.0436	.0427	.0418	.0409	.0401	.0392	.0384	.0375	.036
-1.6	.0548	.0537	.0526	.0516	.0505	.0495	.0485	.0475	.0465	.045
-1.5	.0668	.0655	.0643	.0630	.0618	.0606	.0594	.0582	.0571	.055
-1.4	.0808	.0793	.0778	.0764	.0749	.0735	.0721	.0708	.0694	.068
-1.3	.0968	.0951	.0934	.0918	.0901	.0885	.0869	.0853	.0838	.082
-1.2	.1151	.1131	.1112	.1093	.1075	.1056	.1038	.1020	.1003	.098
-1.1	.1357	.1335	.1314	.1292	.1271	.1251	.1230	.1210	.1190	.117
-1.0	.1587	.1562	.1539	.1515	.1492	.1469	.1446	.1423	.1401	.137
-0.9	.1841	.1814	.1788	.1762	.1736	.1711	.1685	.1660	.1635	.161
-0.8	.2119	.2090	.2061	.2033	.2005	.1977	.1949	.1922	.1894	.186
-0.7	.2420	.2389	.2358	.2327	.2296	.2266	.2236	.2206	.2177	.214
-0.6	.2743	.2709	.2676	.2643	.2611	.2578	.2546	.2514	.2483	.245
-0.5	.3085	.3050	.3015	.2981	.2946	.2912	.2877	.2843	.2810	.277
-0.4	.3446	.3409	.3372	.3336	.3300	.3264	.3228	.3192	.3156	.312
-0.3	.3821	.3783	.3745	.3707	.3669	.3632	.3594	.3557	.3520	.348
-0.2	.4207	.4168	.4129	.4090	.4052	.4013	.3974	.3936	.3897	.385
-0.1	.4602	.4562	.4522	.4483	:4443	.4404	.4364	.4325	.4286	.424
-0.0	.5000	.4960	.4920	.4880	.4840	.4801	.4761	.4721	.4681	.464

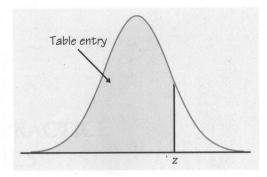


Table entry for z is the area under the standard normal curve to the left of z.

TAI	BLE A	Standar	d norma	l probab	oilities (	continue	d)			
z	.00	.01	.02	.03	.04	.05	.06	.07	.08	.09
0.0	.5000	.5040	.5080	.5120	.5160	.5199	.5239	.5279	.5319	.5359
0.1	.5398	.5438	.5478	.5517	.5557	.5596	.5636	.5675	.5714	.5753
0.2	.5793	.5832	.5871	.5910	.5948	.5987	.6026	.6064	.6103	.6141
0.3	.6179	.6217	.6255	.6293	.6331	.6368	.6406	.6443	.6480	.6517
0.4	.6554	.6591	.6628	.6664	.6700	.6736	.6772	.6808	.6844	.6879
0.5	.6915	.6950	.6985	.7019	.7054	.7088	.7123	.7157	.7190	.7224
0.6	.7257	.7291	.7324	.7357	.7389	.7422	.7454	.7486	.7517	.7549
0.7	.7580	.7611	.7642	.7673	.7704	.7734	.7764	.7794	.7823	.7852
0.8	.7881	.7910	.7939	.7967	.7995	.8023	.8051	.8078	.8106	.8133
0.9	.8159	.8186	.8212	.8238	.8264	.8289	.8315	.8340	.8365	.8389
1.0	.8413	.8438	.8461	.8485	.8508	.8531	.8554	.8577	.8599	.8621
1.1	.8643	.8665	.8686	.8708	.8729	.8749	.8770	.8790	.8810	.8830
1.2	.8849	.8869	.8888	.8907	.8925	.8944	.8962	.8980	.8997	.9015
1.3	.9032	.9049	.9066	.9082	.9099	.9115	.9131	.9147	.9162	.9177
1.4	.9192	.9207	.9222	.9236	.9251	.9265	.9279	.9292	.9306	.9319
1.5	.9332	.9345	.9357	.9370	.9382	.9394	.9406	.9418	.9429	.9441
1.6	.9452	.9463	.9474	.9484	.9495	.9505	.9515	.9525	.9535	.9545
1.7	.9554	.9564	.9573	.9582	.9591	.9599	.9608	.9616	.9625	.9633
1.8	.9641	.9649	.9656	.9664	.9671	.9678	.9686	.9693	.9699	.9706
1.9	.9713	.9719	.9726	.9732	.9738	.9744	.9750	.9756	.9761	.9767
2.0	.9772	.9778	.9783	.9788	.9793	.9798	.9803	.9808	.9812	.9817
2.1	.9821	.9826	.9830	.9834	.9838	.9842	.9846	.9850	.9854	.9857
2.2	.9861	.9864	.9868	.9871	.9875	.9878	.9881	.9884	.9887	.9890
2.3	.9893	.9896	.9898	.9901	.9904	.9906	.9909	.9911	.9913	.9916
2.4	.9918	.9920	.9922	.9925	.9927	.9929	.9931	.9932	.9934	.9936
2.5	.9938	.9940	.9941	.9943	.9945	.9946	.9948	.9949	.9951	.9952
2.6	.9953	.9955	.9956	.9957	.9959	.9960	.9961	.9962	.9963	.9964
2.7	.9965	.9966	.9967	.9968	.9969	.9970	.9971	.9972	.9973	.9974
2.8	.9974	.9975	.9976	.9977	.9977	.9978	.9979	.9979	.9980	.9981
2.9	.9981	.9982	.9982	.9983	.9984	.9984	.9985	.9985	.9986	.9986
3.0	.9987	.9987	.9987	.9988	.9988	.9989	.9989	.9989	.9990	.9990
3.1	.9990	.9991	.9991	.9991	.9992	.9992	.9992	.9992	.9993	.9993
3.2	.9993	.9993	.9994	.9994	.9994	.9994	.9994	.9995	.9995	.9995
3.3	.9995	.9995	.9995	.9996	.9996	.9996	.9996	.9996	.9996	.9997
3.4	.9997	.9997	.9997	.9997	.9997	.9997	.9997	.9997	.9997	.9998

# THE BASIC PRACTICE OF STATISTICS

## **PREFACE**

The Basic Practice of Statistics is an introduction to statistics for students in two-year and four-year colleges and unversities that emphasizes working with data and statistical ideas. In this preface I describe the book in order to help teachers judge whether it is right for their students.

Guiding principles

The American Statistical Association and the Mathematical Association of America recently formed a joint committee to study the teaching of introductory statistics. Here are their main recommendations:<sup>1</sup>

- · Emphasize statistical thinking.
- More data and concepts; less theory, fewer recipes.
- Foster active learning.

I was a member of the ASA/MAA committee, and I agree with their conclusions. Fostering active learning is the business of the teacher (though an emphasis on working with data helps). The first two recommendations are the guiding principles of this text. Although the book is elementary in the level of mathematics required and in the statistical procedures presented, it aims to give students both an understanding of the main ideas of statistics and useful skills for working with data. Examples and exercises, though intended for beginners, use real data and give enough background to allow students to consider the meaning of their calculations. I often ask for conclusions that are more than a number (or "reject H<sub>0</sub>"). Some exercises require judgement in addition to right-or-wrong calculations and conclusions. Both students and teachers should recognize that not every part of every exercise has a single correct answer. I hope that teachers will encourage further discussion of results in class.

Chapters 1 and 2 present the methods and unifying ideas of data analysis. Students appreciate the usefulness of data analysis, and the fact that

they can actually do it relieves a bit of their anxiety about statistics. I hope that they will grow accustomed to examining data and will continue to do so even when formal inference to answer a specific question is the ultimate goal. Chapter 3 discusses random sampling and randomized comparative experiments. These are among the most important ideas in statistics, and are often unjustly neglected in beginning instruction. Chapter 4 builds on the ideas of Chapter 3 and the data-analytic tools of Chapter 1 to present the central idea of a sampling distribution and (informally) the language of probability. Chapter 5 is the cornerstone of the rest of the book. It describes the reasoning of statistical inference. The remaining chapters present methods of inference for various settings, with a strong emphasis on practical aspects of using these methods. Chapters 6 and 7 discuss basic one-sample and two-sample procedures. Chapters 8, 9, and 10 (which can be read independently of each other in any order) offer a choice of somewhat more advanced topics.

Technology

Automating calculations increases students' ability to complete problems, reduces their frustration, and helps them concentrate on ideas and problem recognition rather than mechanics. This book requires that students have a *calculator* that will do statistical calculations through correlation and simple linear regression. As I write, several makers sell such calculators for less than \$18. Because students have calculators, the text doesn't discuss "computing formulas" for the sample standard deviation or least-squares regression line. Exercises assume that students will use a "two-variable statistics" calculator rather than a more rudimentary model. Many scientific calculators are even more capable, offering simulation and some graphics as well as more statistical procedures. Course-wide use of a graphing calculator is somewhat similar to using software, and will probably require specific instruction.

Statistical software has considerable advantages over calculators: easier data entry and editing, much better graphics, more statistical procedures. I encourage the use of software whenever time and facilities permit. This book does not, however, assume that students will use software. Output from four statistical software packages appears in the text, with Minitab most common. Students should be able to interpret output and use it for further work. Because of the great variety of software used for statistics, from spreadsheets to SAS, I have avoided instruction on how to use any one program. A supplementary Minitab handbook is available for teachers who want to introduce Minitab in a way closely tied to the text. Data sets for examples and exercises are available on a data disk, from which they can be read into any statistical software.

Although *video* is a poor medium for exposition, actually seeing statistics at work in a variety of settings is a powerful means of changing student attitudes about statistics. I show one of the short on-location documentary segments from the Annenberg/Corporation for Public Broadcasting telecourse *Against All Odds: Inside Statistics* about once a week. Because I was the content developer for this video series, it fits the style and sequence of this book closely. The Instructor's Guide contains suggestions about using video, a list of recommended excerpts, and information on how to obtain *Against All Odds*.

**Probability** 

The difficult issue of how to present probability in a first course on statistical methods deserves separate comment. Experienced teachers recognize that students find probability difficult. Research on learning confirms our experience. I recommend the survey article "Difficulties in learning basic concepts in probability and statistics: implications for research," by Joan Garfield and Andrew Ahlgren. Garfield and Ahlgren document the fragility of probability concepts even among students who can work formal probability problems. They conclude that "teaching a conceptual grasp of probability still appears to be a very difficult task, fraught with ambiguity and illusion." They recommend exploring "how useful ideas of statistical inference can be taught independently of technically correct probability."

Probability is a noble and useful subject. Attempting to present a substantial introduction to probability in a data-oriented statistics course for students who are not mathematically trained, however, is in my opinion unwise. Formal probability does not help these students master the ideas of inference (at least not as much as we teachers imagine), and it depletes reserves of mental energy that might better be applied to essentially statistical ideas.

I have therefore presented very little formal probability in the core of the text. The central idea is that of the sampling distribution of a statistic. Sampling distributions answer a question that leads to the heart of statistical inference, "What would happen if I repeated this random process many times?" Moreover, students can use tools from data analysis to understand distributions. Normal distributions appear already in Chapter 1 as models for the overall pattern of some distributions of data. In Section 1 of Chapter 4, sampling distributions motivate a brief and quite informal introduction to the language of probability. Sections 4.3 and 4.5 look at the sampling distributions of sample proportions and sample means in more detail. Such important probability facts as the central limit theorem and

the law of large numbers appear in this context. A few additional probability ideas, particularly independence, are treated informally when needed. This is the approach I recommend.

Instructors who want more depth in the study of probability distributions will find it in the optional Sections 4.2 and 4.4. Even these sections avoid the formal notation of set theory and general probability. *Introduction to the Practice of Statistics* offers more, and more traditionally presented, probability. I confess that when teaching from that text I omit most of its probability material in favor of additional statistics. Sections 4.1, 4.3, and 4.5 of this book (with the optional Section 4.6 on control charts) contain what I actually teach students without calculus.

#### What about that other book?

The Basic Practice of Statistics is kin to Introduction to the Practice of Statistics (IPS).<sup>3</sup> It shares both its guiding principles and some details (especially exercises) with the larger book. But this is not an abridgement of IPS. Much of the material, including all of Chapters 7 to 10, is completely new. I have omitted most of the optional material in IPS, as well as a number of topics that were not optional. The result is a shorter book.

I have also endeavored to make this book considerably easier to read. The language, the length of the exposition, the organization of exercises, and the choice of topics have been rethought throughout for a less advanced audience. Each main idea is followed by a short section of exercises for immediate reinforcement. Each chapter review includes a list of specific skills against which students may check their learning. An index of symbols (note that it isn't long—the density of symbols is as low as I could efficiently manage) and an index of procedures are placed ahead of the usual index. There is a removable gatefold insert that includes essential formulas and tables for easy reference and use in testing.

Instructors who appreciate the data-and-ideas approach of *IPS*, but found it hard going for their students, should like this book. Conversely, instructors who wish to present such topics as normal quantile plots, transformations of variables, formal probability, or brief introductions to multiple regression and two-way analysis of variance should consider *IPS*.

### Supplements

A full range of supplements is available to help teachers and students use *The Basic Practice of Statistics*. In the *Instructor's Guide* I give an overview and teaching suggestions for each chapter, comments on the use of video, and sample examinations. I also present additional examples for classroom use, with data on the data disk. These helps are followed by complete solutions

(not just answers) for all exercises, prepared by Darryl Nester of Bluffton College. William Notz and Becky Busam of Ohio State University have prepared a *Student Study Guide* and a *Test Bank* for instructors. A set of *Transparency Masters* is available from the publisher. A *Data Disk*, available in both DOS/Windows and Macintosh formats, enables instructors to easily enter the data from examples and exercise sets into their software. Betsy Greenberg of the University of Texas has written a *Minitab Handbook* that gives detailed instruction about the Minitab statistical software linked to the sequence and examples of the text.

Acknowledgments

I am grateful to many colleagues from two-year and four-year colleges and universities who commented on successive drafts of the manuscript:

Douglas M. Andrews Wittenberg University

Rebecca Busam
The Ohio State University

Michael Butler College of the Redwoods

Carolyn Pillers Dobler Gustavus Adolphus College

Joel B. Greenhouse Carnegie Mellon University

Larry Griffey Florida Community College at Jacksonville

Brenda Gunderson
The University of Michigan

Catherine Cummins Hayes University of Mobile

Tim Hesterberg Franklin & Marshall College Ronald La Porte Macomb Community College

Ken McDonald Northwest Missouri State University

William Notz The Ohio State University

Mary Parker Austin Community College

Calvin Schmall Solano Community College

Frank Soler De Anza College

Linda Sorensen Algoma University

Tom Sutton Mohawk College

I am also grateful to the excellent editorial and design professionals at W. H. Freeman and Company. Diane Cimino Maass and Carol Pritchard-Martinez in particular contributed a great deal to this book.

More generally, I am indebted to many statistics teachers with whom I have discussed the teaching of our subject over many years; to people from diverse fields with whom I have worked to understand data; and especially to students whose compliments and complaints have changed and improved my teaching. Working with teachers, colleagues in other disciplines, and students has reminded me of the importance of handson experience with data and of statistical ideas in an era when computer routines and professional advice quickly handle statistical details.

David S. Moore

#### Notes

- 1. George Cobb, "Teaching statistics," in L.A. Steen (ed.), *Heeding the Call for Change: Suggestions for Curricular Action*, MAA Notes No. 22, Mathematical Association of America, Washington D.C., 1992, pp. 3–43.
- 2. Joan Garfield and Andrew Ahlgren, "Difficulties in learning basic concepts in probability and statistics: implications for research," *Journal for Research in Mathematics Education*, 19 (1988), pp. 44–63.
- 3. David S. Moore and George P. McCabe, *Introduction to the Practice of Statistics*, 2d ed., W. H. Freeman, New York, 1993.

# **CONTENTS**

	Prefa	ace	xiii
i	Intro	duction: What Is Statistics?	1
PART 1	UNDERSTA	ANDING DATA	6
	CHA	PTER 1 Examining Distributions	8
		Introduction	10
	1.1	<b>Displaying Distributions with Graphs</b> Categorical variables 13	12
		Drawing histograms 14 Interpreting histograms 17 Stemplots 23	
		Time plots 26 Summary 28	
		Section 1.1 exercises 29	
	1.2	Describing Distributions with Numbers Measuring center: the mean 36	34
		Measuring center: the median 38 Comparing the mean and the median 40	
		Measuring spread: the quartiles 41	
		The five-number summary and boxplots 43 Measuring spread: the standard deviation 46 Summary 51 Section 1.2 exercises 52	

<sup>\*</sup>Starred sections are optional

1.3	The Normal Distributions	54
	Density curves 54  The median and mean of a density curve 57  Normal distributions 60  The standard normal distribution 64  Normal distribution calculations 66  Finding a value given a proportion 71  Assessing normality* 73  Summary 75  Section 1.3 exercises 76	
	Chapter Review Chapter 1 review exercises 81	79
СНА	PTER 2 Examining Relationships	90
	Introduction	92
2.1	Scatterplots Interpreting scatterplots 98 Adding categorical variables to scatterplots 102 Summary 105 Section 2.1 exercises 106	96
2.2	CorrelationThe correlation $r$ 111Facts about correlation114Summary117Section 2.2 exercises117	111
2.3	Least-Squares Regression The least-squares regression line 120 Facts about least-squares regression 125 Residuals 129 Influential observations 134 Summary 137 Section 2.3 exercises 138	119
2.4	Interpreting Correlation and Regression  Extrapolation 142  Lurking variables 143  Using averaged data 145  Association is not causation 146  Summary 148  Section 2.4 exercises 149	142

2.5 Relations In Categorical Data*  Marginal distributions 151  Describing relationships 153  Simpson's paradox 157  Summary 161  Section 2.5 exercises 162		150
Chapter Review Chapter 2 review exercises 167		165
CHAPTER 3 Producing Data		176
Introduction		178
3.1 Designing Samples Simple random samples 182 Other sampling designs 187 Cautions about sample surveys 189 Inference about the population 193 Summary 194 Section 3.1 exercises 194		180
3.2 Designing Experiments  Comparative experiments 202  Completely randomized experiments 203  The logic of experimental design 208  Cautions about experimentation 210  Other experimental designs 213  Summary 217  Section 3.2 exercises 218  Chapter Review  Chapter 3 review exercises 221		198
Chapter 3 review exercises 221		
PART 2 UNDERSTANDING INFERENCE		226
CHAPTER 4 Sampling Distributions an Probability	ıd	228
Introduction		230
<b>4.1 Sampling Distributions</b> Sampling variability 232		230