

P R O C E E D I N G S

DATA COMPRESSION

C O N F E R E N C E

March 30 - April 2, 1993 • Snowbird, Utah

Edited by
James A. Storer
Martin Cohn

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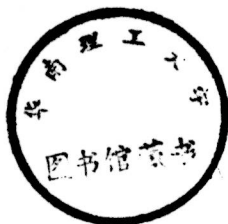
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DCC '93 DATA COMPRESSION CONFERENCE

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James A. Storer
Martin Cohn*



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Technical Sessions

Combining Image Classification and Image Compression Using Vector Quantization

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Abstract

We describe a technique for combining compression and low-level classification of images. The goal is to produce codes with implicit classification information, where the compressed image incorporates classification information without further signal processing. This technique can provide direct low level classification or provide an efficient front end to more sophisticated full-frame recognition algorithms. Vector quantization (VQ) is a natural choice because two of its design components, clustering and tree-structured classification methods, have obvious applications to the pure classification problem as well as to the compression problem. Here we explicitly incorporate a Bayes risk component into the distortion measure used for code design in order to permit a tradeoff of mean squared error with classification error. This method is used to analyze simulated data, identify tumors in computerized tomography (CT) lung images, and identify man-made regions in aerial images.

1 Introduction

Image compression and classification play very important roles in making digital images useful. Because lossless compression (compression without error) can typically provide a compression ratio of only 2 - 4, lossy compression techniques become necessary for further compression. VQ is a common method of lossy compression that applies statistical techniques to optimize distortion/bit rate tradeoffs [1, 2, 3].

In many scientific and medical applications, images are used by human experts to make specific decisions or inferences. The actions of human experts can sometimes be mimicked by sophisticated computer algorithms, typically requiring large amounts of computer processing on entire images in order to reach decisions. Simple low-level local classification involving only small regions of an image, however, can assist human observers by highlighting special areas of interest and can simplify future classification/analysis algorithms by incorporating pre-processing into the digital representation. The approach described here is applicable to classification tasks where the goal is to classify fairly small regions in an image, for example, to identify

lung nodules in a CT lung scan, microcalcifications in mammograms, or manmade objects in an aerial photograph. Our goal is to combine such local classification with the compression process to obtain a single code that does a good job of both, with an adjustable relative importance weighting of the two aspects. VQ provides a natural means to this end because two of its design components, clustering and tree-structured classification methods, have obvious applications to the pure classification problem as well as to the compression problem.

2 Vector Quantization

Vector quantization operates on individual image subblocks or vectors (e.g. blocks of 2 pixels \times 2 pixels). For each vector, the VQ encoder determines the nearest codeword and outputs the chosen codeword's index. The sequence of indices so generated can then be stored or transmitted. The VQ decoder reverses this process as it inputs each index and outputs the appropriate codeword by simple table lookup. A clear advantage of VQ is the low complexity decoding process. As the input vectors mapping into a particular codeword will generally have much in common, they are likely to belong to the same class. By attaching class significance to the codewords, we can obtain both classification and compression with a single encoding step.

The accuracy of the classifier is measured by the Bayes risk, which reduces to a simple error probability if unit costs are chosen. The more general form allowing varying costs for different error types is useful for many applications (such as classifying tissue as tumor or healthy) and our algorithm provides a convenient means of including these costs. This Bayes risk term can be incorporated into the distortion measure, and the resulting codebook is then designed to determine class membership when the image is decompressed. Our method explicitly incorporates the performance of optimal (Bayes) classifiers operating on the vector quantized data, both through the form of the distributions (which are learned by training and do not require an a priori model), and through the explicit incorporation of a Bayes risk term into the average distortion that is minimized by the design algorithm. The extra complexity is almost entirely in the code design phase; the implemented code is only slightly more complicated than an ordinary vector quantizer. The classification requires no more bits to describe than the bits required for compression alone, an important feature in low memory or low bandwidth situations. As the classification information is entirely contained in the selected codeword, it can be easily displayed with the decompressed image. For example, a physician could select either a monochrome decompressed image or one with all the suspected anomalies colored pink for highlighting.

There have been several papers devoted to the related topic of designing a classifier that uses a VQ encoder. Kohonen [4, 5, 6] proposed a variety of "likelihood vector quantizers" or LVQ to perform classification using a VQ encoder and codebook, where the encoder operates as an ordinary minimum mean squared error selection of a representative from the codebook, but the codebook is designed in a manner that attempts to reduce classification error implicitly rather than reducing mean squared error. His general goal is to imitate a Bayes classifier with less complexity than

other neural network approaches, but there is no explicit minimization of Bayes risk in the code design. The Kohonen approach differs from ours in many ways. First, our approach considers mean squared error in the optimization and his does not. As we allow a weighting of relative importance, his goal can be considered as an extreme point of ours. Compression ability is not explicitly considered in LVQ. His encoder uses only minimum mean squared error, even within the learning set, while we explicitly apply an empirical Bayes classifier as part of the encoding, balancing minimum squared error with empirical Bayes risk. We explicitly incorporate the Bayes risk into the average distortion measure being minimized, while Kohonen uses a heuristic to argue that moving centroids according to nearby class membership should asymptotically have the effect of approximating a Bayes risk.

3 Approach

Given a n -dimensional vector $X = (x_1, \dots, x_n)^T$, a full search (unconstrained) VQ maps each input vector onto a set of codewords called the codebook: $q(X) = \hat{Y}_i$, where $\hat{Y}_i \in \{\hat{Y}_1, \dots, \hat{Y}_N\}$. Denote the partition of input vector space induced by q by $\mathcal{P} = \{\mathcal{A}_1, \dots, \mathcal{A}_N\}$ where $X \in \mathcal{A}_i$ if $q(X) = \hat{Y}_i$. Then $\alpha(X) = i$ if $X \in \mathcal{A}_i$ is the encoder and $\beta(i) = \hat{Y}_i$ is the decoder for the VQ q . Hence $q(X) = \beta(\alpha(X))$. Because there are many more possible input vectors than codewords, the quantizer compresses the data.

Suppose we have a collection of classes $\mathcal{H} = \{H_1, H_2, \dots, H_M\}$. To perform a classification, we associate a class label with each cell \mathcal{A}_i in the partition or, equivalently, with each index i produced by the encoder α , for $i \in \{1, \dots, N\}$. The index can then be used to decompress the vector using the codebook and to classify the vector using the decision rule. Let $\delta(i) \in \mathcal{H}$, $i = 1, \dots, N$, denote the decision function.

Codebook construction requires a labeled learning set $\mathcal{S} = \{X_1, \dots, X_L\}$. Each training vector X_i is assigned to a specific class in \mathcal{H} . The samples provide the empirical distribution of X , used to train the vector quantizer.

The average ordinary distortion corresponding to (α, β) is

$$D(\alpha, \beta) = E[d(X, \beta(\alpha(X)))] \geq E[\min_i d(X, \beta(i))] \text{ where } 1 \leq i \leq N. \quad (1)$$

The mean squared error $d(X, \beta(\alpha(X))) = \|X - \beta(\alpha(X))\|^2$ is commonly used as the distortion measure.

The classification performance can be measured by the Bayes risk [7]:

$$B(\alpha, \delta) = \sum_{i=1}^M \sum_{j=1}^M P(\delta(\alpha(X)) = H_j | X \in H_i) P(H_i) C_{ij},$$

where C_{ij} is the relative cost of error incurred when $X \in H_i$ and $\delta(\alpha(X)) = H_j$. Often, $C_{ij} = 0$ when $i = j$ (correct decisions have zero cost). Note that the reproduction values supplied by β do not affect B . Define an indicator function $I_{H_i}(H_j)$ as 1 if