## permselective membranes

edited by C. E. ROGERS

### PERMSELECTIVE MEMBRANES

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### C. E. ROGERS

DIVISION OF MACROMOLECULAR SCIENCE CASE WESTERN RESERVE UNIVERSITY CLEVELAND, OHIO

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### **Preface**

Over the last decade it has become increasingly evident that the unique gas, vapor, or liquid permeability behavior of synthetic polymer membranes is of great fundamental and practical importance. The utilization of well-characterized permselective membranes for many novel separation or selective barrier processes is of interest for diverse fields of physical science, industrial technology, and

biological consideration.

The accelerating research and development efforts concerned with film and membrane materials, processes, and applications have many goals. An ultimate aim of research in this field is to establish mechanisms and laws relating solubility and transport in multicomponent systems with the molecular properties and characteristics of the components. Conversely, the nature of the movement of a penetrant in a solid can afford information about concurrent molecular processes related to such characteristics of the solid as the flexibility and conformation of the molecular chains, the nature of the interaction between adjoining molecular segments, and the overall morphology. In this sense, transport measurements can be considered as extremely sensitive molecular probe techniques suitable for detailed characterizations of polymer microstructure.

From the practical and technical viewpoint, knowledge of solution, diffusion, and permeation behavior is essential for the successful design and use of many products such as packaging films and other protective coatings. This knowledge is especially necessary for the efficient development of permselective membranes to satisfy the exacting specifications required for use as media for reverse osmosis desalination, artificial kidney and lung components, and for other precise separations of multicomponent penetrant mixtures. The emerging field of ion exchange membranes is a very important

area of study in this respect.

Many recent advances in membrane science and technology have been made possible by continuing progress in other fields of polymer science and engineering. The interdependence of polymer structure and transport behavior—a major factor affecting the ultimate properties of films and membranes—is of increasing importance as our ability to control polymer synthesis and to characterize polymer

iv PRE FACE

structure have become more precise and predictable. It is to be expected that even more dramatic progress in membrane technology will result from the ever quickening pace of research in related areas of science spurred on by the increased awareness of the present and potential importance of membrane phenomena.

Some of the most recent work pertaining to several areas of membrane science and technology was presented at the Symposium on Permselective Membranes of the 158th American Chemical Society meeting held in New York City, in September 1969. This symposium was sponsored jointly by the Division of Polymer Chemistry and the Division of Colloid and Surface Chemistry. The large attendance and active discussions which characterized both the formal symposium presentations and the informal discussion period that followed are indicative of the intense interest in these topics. This issue of the Journal of Macromolecular Science—Physics constitutes a permanent record of the formal proceedings for future reference, in anticipation that it may serve, in some part, to stimulate further studies of membrane phenomena.

C. E. Rogers

Division of Macromolecular Science Case Western Reserve University Cleveland, Ohio

### **Contributors to This Volume**

- W. H. BURGESS, Department of Chemical Engineering, North Carolina State University, Raleigh, North Carolina
- B. P. CROSS, Gulf General Atomic Company, San Diego, California
- S.-M. FANG, Department of Chemical Engineering and Metallurgy, Syracuse University, Syracuse, New York
- MORTON FELS, Department of Chemical Engineering, University of Waterloo, Waterloo, Ontario, Canada
- F. M. GRABER, Gulf General Atomic Company, San Diego, California
- H. B. HOPFENBERG, Department of Chemical Engineering, North Carolina State University, Raleigh, North Carolina
- ROBERT Y. M. HUANG, Department of Chemical Engineering, University of Waterloo, Waterloo, Ontario, Canada
- SUN-TAK HWANG, Department of Chemical Engineering, University of Iowa, Iowa City, Iowa
- R. M. JOBBINS, Department of Chemical Engineering and Metallurgy, Syracuse University, Syracuse, New York
- KARL KAMMERMEYER, Department of Chemical Engineering, University of Iowa, Iowa City, Iowa
- PETER J. F. KANITZ, Department of Chemical Engineering, University of Waterloo, Waterloo, Ontario, Canada
- N. LAKSHMINARAYANAIAH, Department of Pharmacology, University of Pennsylvania Medical School, Philadelphia, Pennsylvania
- C. E. LAMAZE, Camille Dreyfus Laboratory, Research Triangle Institute, Research Triangle Park, North Carolina
- H. K. LONSDALE, Gulf General Atomic Company, San Diego, California
- J. A. MARINSKY, Department of Chemistry, State University of New York at Buffalo, Buffalo, New York
- C. E. MILSTEAD, Gulf General Atomic Company, San Diego, California
- M. M. REDDY, Department of Chemistry, State University of New York at Buffalo, Buffalo, New York

- C. E. ROGERS, Division of Macromolecular Science, Case Western Reserve University, Cleveland, Ohio
- V. T. STANNETT, Department of Chemical Engineering, North Carolina State University, Raleigh, North Carolina
- S. A. STERN, Department of Chemical Engineering and Metallurgy, Syracuse University, Syracuse, New York
- S. STERNBERG, Division of Macromolecular Science, Case Western Reserve University, Cleveland, Ohio
- THOMAS E. TANG, Department of Chemical Engineering, University of Iowa, Iowa City, Iowa
- H. YASUDA, Camille Dreyfus Laboratory, Research Triangle Institute, Research Triangle Park, North Carolina
- K. D. ZIEGEL, Elastomer Chemicals Department, E. I. du Pont de Nemours and Company, Wilmington, Delaware

### **Contents**

Preface	iii
Contributors to This Volume	v
TRANSPORT OF DISSOLVED OXYGEN THROUGH SILICONE	
RUBBER MEMBRANE	1
Sun-Tak Hwang, Thomas E. S. Tang,	
and Karl Kammermeyer	
Summary	1
Introduction	2
Theory	2
Experiments	4
Results and Discussion	6
Conclusion	9
Glossary of Symbols	9
References	9
GAS TRANSPORT IN SEGMENTED BLOCK COPOLYMERS $K.\ D.\ Ziegel$	11
Summary	11
Introduction	11
Experimental Procedure	13
Polymer Films	13
Gases	13
Technique of Measurement	13
Results	15
Discussion	17
References	21
TRANSPORT OF NOBLE GASES IN POLY(METHYL	
ACRYLATE)	23
W. H. Burgess, H. B. Hopfenberg, and V. T. Stannett	
Summary	23
Introduction	24

Experimental	0.1
Results and Discussion	2'
Experimental Values for Tg in PMA	29
Solubility of Noble Gases in PMA	32
Molecular Stiffness and Transport	3'
Comparison of PMA and PVA	38
References	38
PERMEATION OF GASES AT HIGH PRESSURES	
S. A. Stern, SM. Fang, and R. M. Jobbins	41
Summary	
Introduction	41
Experimental Procedure	42
Permeability Apparatus	43
Membranes	43
Gases	44
Results	44
Pure Gases	46
Carbon Dioxide-Polyethylene System	46
Nitrous Oxide-, Ethane-, and Ethylene-Polyethylene	46
Systems	
Methane-Polyethylene System	49
Nitrogen- and Helium-Polyethylene Systems	54
Gas Mixtures	54
Comparison with Other Measurements	57
Discussion and Conclusions	62
References	65
	68
PERMEATION OF GASES THROUGH MODIFIED POLYMER FILMS III. GAS PERMEABILITY AND SEPARATION CHAR-	
ACTERISTICS OF GAMMA-IRRADIATED TEFLON FEP	
COPOLYMER FILMS	71
Robert Y. M. Huang and Peter J. F. Kanitz	71
Summary Introduction	71
	72
Experimental Details	72
Materials	72
Apparatus Procedure	73
Discussion of Results	74
	74
Effect of Irradiation Atmosphere and Postirradiation Heat Treatment	
Transport of Nitrogen and Methane Gases	74
Permeability of Irradiated Copolymer Films	78
Diffusion in Irradiated Teflon FEP Copolymer	78
	80

Solubility in Irradiated Teflon FEP Copolymer Films	83
Permeation of Nitrogen-Methane Gas Mixtures	84
Separation of Nitrogen-Methane Gas Mixtures	86
References	87
	01
THEORETICAL INTERPRETATION OF THE EFFECT OF MIXTURE COMPOSITION ON SEPARATION OF LIQUIDS	
IN POLYMERS	89
Morton Fels and Robert Y. M. Huang	
Summary	89
Introduction	89
Theory	90
Steady-State Permeabilities of Individual Components in a	
Binary Mixture	90
Experimental	93
Steady-State Permeation and Separation	93
Procedure	96
Unsteady-State Discussion	96
Discussion of Results	96
Steady-State Permeation and Separation	96
Unsteady-State Desorption Results	101
Comparison of Pure Liquid Permeabilities	102
Binary Permeabilities	103
Conclusions	108
References	108
PERMSELECTIVITY OF SOLUTES IN HOMOGENEOUS	
WATER-SWOLLEN POLYMER MEMBRANES	
H. Yasuda and C. E. Lamaze	111
Summary	111
Introduction	112
Criteria of Homogeneous Membrane and Modes of Transport	113
Permeability of Gases in Porous and Homogeneous Polymer Films Diffusive Permeability of Solutes through Water-Swollen Polymer	115
Membranes	122
a. Dependence on Hydration	124
b. Dependence on the Solute Size	124
c. Role of Sieve Mechanism	124
d. Effect of Membrane Charge	127
Piezometric Permeability of Water through Water-Swollen Polymer	
Membranes	128
Permselectivity of Solutes in Various Membrane Processes	130
References	133

ION-EXCHANGE SELECTIVITY COEFFICIENTS IN EX- CHANGE OF CALCIUM, STRONTIUM, COBALT, NICKEL, ZINC, AND CADMIUM IONS WITH HYDROGEN ION IN VARIOUSLY CROSS-LINKED POLYSTYRENE SULFONATE	
CATION EXCHANGERS AT 25°C  M. M. Reddy and J. A. Marinsky	135
Summary	135
Introduction	136
Experimental Details	137
Materials	137
Procedure	139
Results	140
Discussion	149
Conclusion	154
References	156
ION AND WATER TRANSPORT THROUGH PERMSELECTIVE	
MEMBRANES	159
N. Lakshminarayanaiah	100
Summary	159
References	165
AVOICE CHOOS	100
PERMEABILITY OF CELLULOSE ACETATE MEMBRANES	
TO SELECTED SOLUTES	167
H. K. Lonsdale, B. P. Cross, F. M. Graber, and	
C. E. Milstead	
Summary	167
Introduction	167
Experimental	168
Reverse Osmosis	168
Desorption Rate	169
Direct Osmosis	171
Results and Discussion	171
Reverse Osmosis with Modified Membranes	171
Reverse Osmosis with Thin-Film Composite Membranes	174
Desorption Rate	174
Factorial Experiment	178
Comparison of Reverse Osmosis and Desorption Rate Results	182
References	186

CONTENTS xi

T	RANSPORT THROUGH PERMSELECTIVE MEMBRANES	189
	C. E. Rogers and S. Sternberg	
	Summary	189
	Introduction	190
	Nature of Membrane Transport Processes	190
	Some Factors Affecting Membrane Permeability	192
	Transport in Heterogeneous Polymer Membranes	197
	A Mathematical Model for Transport in Asymmetric Membranes	198
	Predictions of Permeability Magnitude and Preference Factors	201
	References	205

# Transport of Dissolved Oxygen through Silicone Rubber Membrane\*

SUN-TAK HWANG, THOMAS E. S. TANG, AND KARL KAMMERMEYER

Department of Chemical Engineering University of Iowa Iowa City, Iowa

#### Summary

The transport of dissolved oxygen in water through a silicone rubber membrane was studied theoretically and experimentally. The apparent oxygen permeability coefficients of silicone rubber were measured at various membrane thicknesses, temperatures, and concentration levels. The permeation flux was measured under both steady— and unsteady—state conditions. For the first time, the thickness effect of dissolved gas permeation has been studied. It was found that the apparent permeability increases with increasing membrane thickness and approaches asymptotically to the gas phase permeability. A general equation was developed to explain this phenomenon based on the concept of immobile boundary layers. It was also observed that the apparent oxygen permeability increased exponentially with increasing concentration levels in water. The temperature dependency of permeability was of the Arrhenius type.

\*This work was supported by the National Institutes of Health.

### INTRODUCTION

Even though there are numerous publications dealing with studies of gas permeation through membranes, very few are concerned with dissolved gases. A recent study by Yasuda [1,2] on permeation of oxygen dissolved in water presents an interesting comparison of gas-to-gas permeabilities of oxygen with those of oxygen in water-to-oxygen in water. Among many polymer membranes employed, silicone rubber showed a marked difference in its magnitude of permeability from other membranes. Another related study by Robb [3] demonstrates that the oxygen diffusion from water into a submerged cage covered by a thin silicone membrane is adequate to sustain life of test animals for several days. The transport of dissolved gases through membranes is an indispensable phenomenon in the physiology of respiration and in the development of the artificial lung and artificial gills.

The purpose of the present study was to investigate fundamental factors involved in the transport of dissolved gases through membranes. Variables studied are temperature, thickness of membrane, and concentration of dissolved oxygen in water.

### THEORY

A model adopted in the following analysis is a rather general one. A schematic view of cross section of the membrane is shown in Fig. 1. It is assumed that both sides of the membrane are covered by thin layers of immobile fluid, which would give an extra resistance to permeation. The transport of dissolved gas through such a system consists of the following stepwise processes:

- 1. Diffusion through the boundary layer
- 2. Sorption into the membrane
- 3. Diffusion through the membrane
- 4. Desorption out of the membrane
- 5. Diffusion through the boundary layer

Each step presents a resistance of different magnitude to the gas transport. For practical purposes, however, the resistances of some steps are negligible in comparison with those of others. In the case of gas-phase permeation, processes 1 and 5 are not involved, and the resistances due to the steps 2 and 4 may even be negligible. However, for dissolved-gas permeation, a large boundary resistance may result due to steps 1, 2, 4, and 5. The presence of these boundary resistances will reduce the available driving force for diffusion inside the membrane.

The conventional definition of permeability Q is given by a steady-state flow equation:

$$F = Q (\Gamma_1 - \Gamma_2) / L \tag{1}$$

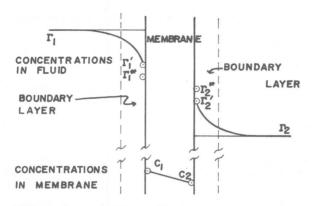


FIG. 1. Concentration profile across the membrane.

If diffusivity is independent of concentration, the same steady-state flux can also be written for the inside of the membrane as

$$F = D(C_1 - C_2)/L \tag{2}$$

Should diffusivity be concentration dependent, an average diffusivity can be used. Since the inside concentrations  $C_1$  and  $C_2$  are very difficult to measure, the permeability is frequently used to report the flow data. However, permeability is generally not a constant nor is it a property of a membrane. Rather, it is a phenomenological coefficient, which does not indicate the actual mechanism of the transport process.

Because it is very difficult to separate steps 2 and 4 from steps 1 and 5 experimentally, it is convenient to lump the resistances of steps 1 and 2 in a group, and steps 4 and 5 in another. Then the flow equation for one side of the membrane can be written

$$F = (\Gamma_1 - \Gamma_1)/r_1 \tag{3}$$

and for the other side,

$$F = (\Gamma_2^* - \Gamma_2)/r_2 \tag{4}$$

where  $r_1$  and  $r_2$  are film resistances including resistances of sorption and desorption if there are any. The fictitious quantities,  $\Gamma_1^*$  and  $\Gamma_2^*$ , are the concentrations which would have produced the inside concentrations  $C_1$  and  $C_2$ , respectively under equilibrium conditions. If a linear isotherm (Henry's law) is applicable,

$$C_1 = S\Gamma_1^* \tag{5}$$

$$C_2 = S\Gamma_2^* \tag{6}$$

If Eqs. (3) to (6) are combined with Eq. (2), then one can solve for F:

$$F = \frac{DS(\Gamma_1 - \Gamma_2)}{DS(\Gamma_1 + \Gamma_2) + L}$$
(7)

Comparing Eq. (7) with Eq. (1), the following is obvious:

$$Q = \frac{DSL}{DS(r_1 + r_2) + L}$$
 (8)

This equation tells exactly how the observed permeability changes as the thickness of a membrane varies. Also, it shows that the film resistance could be significant when the diffusivity of the membrane is large, or when the thickness of a membrane is small. If there is no such film present, then the film resistance simply becomes zero, and the observed permeability reduces to the familiar form:

$$Q = DS (9)$$

### **EXPERIMENTS**

Both steady- and unsteady-state permeabilities were measured for oxygen dissolved in water through silicone rubber membranes (Dow Corning Medical Grade Silastic) with nominal thicknesses of 5, 10, 20, 40, and 62 mils. In addition, two more membranes were made of Dow Corning's Silastic RTV-501 having thicknesses of 180 and 277 mils. The oxygen concentration in water was measured with a Beckman Model 777 laboratory oxygen analyzer. Distilled water was degassed before preparing a dissolved oxygen solution by boiling the water and purging it by nitrogen gas. The oxygen-containing water was prepared by bubbling air into the degassed water until a desired oxygen concentration was obtained.

The steady-state measurements of oxygen flux were easily achieved by having two flowing streams of different oxygen concentrations on each side of the membrane. Two magnetic stirrers gave good agitation on both sides. At steady-state, the oxygen partial pressures of inlet and outlet streams were measured. From the material balance for dissolved oxygen,

$$\frac{QA(\Gamma_1 - \Gamma_2)}{L} + qS_W(\Gamma_0 - \Gamma_2) = 0$$
 (10)

the permeability was calculated by the following equation:

$$Q = qS_{W}\left(\frac{L}{A}\right)\left(\frac{\Gamma_{2} - \Gamma_{0}}{\Gamma_{1} - \Gamma_{2}}\right)$$
(11)

The first term in Eq. (10) represents the oxygen transport through the film; the second term represents the oxygen depletion from the water flowing over the upstream face of the membrane.

The unsteady-state measurements were also necessary because of experimental difficulties encountered in the steady-state measurements for thicker membranes. One side of the membrane was sealed and the other side was in contact with a large reservoir of dissolved oxygen solution. Of course, good agitation was maintained during the experiments by the same magnetic stirrers. The buildup of oxygen partial pressure was recorded as a function of time. From the material balance,

$$VS_{W} \frac{d\Gamma_{2}}{dt} = \frac{QA(\Gamma_{1} - \Gamma_{2})}{L}$$
 (12)

Since  $\Gamma_1$  remains virtually constant, Eq. (12) can be rewritten

$$Q = -\frac{VLS_W}{A} \frac{d \ln (\Gamma_1 - \Gamma_2)}{dt}$$
 (13)

Thus, the unsteady-state permeability can be easily calculated from the slope of the oxygen pressure buildup plot (Fig. 2). Various oxy-

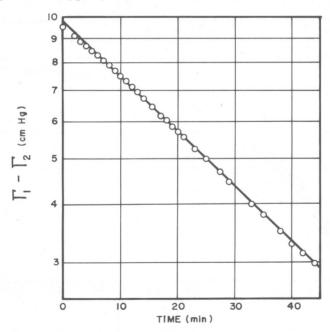


FIG. 2. Typical unsteady-state data.