

$$4(y-2)+5 \geq 2(y+7)-1$$

# Algebra 1

$$f = \{(x, y) : y = ax^2 + bx + c\}$$

revised edition

# Algebra 1

REVISED EDITION

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# Symbols

		PAGE			PAGE
$5^2$	five to the second power	7	$\frac{1}{a}$	the reciprocal, or multi-	
$+$	addition (in BASIC)	9		plicative inverse, of $a$	84
$-$	subtraction (in BASIC)	9	$a - b$	the difference between $a$	
$*$	multiplication (in BASIC)	9		and $b$	99
$/$	division (in BASIC)	9	$a \div b$	the quotient of $a$ divided	
$\uparrow$	raising to a power (in			by $b$	109
	BASIC)	10	$\cap$	intersection	150
$-1$	negative number	12	$\cup$	union	150
$\overline{AB}$	line segment $AB$	13	$\angle A$	angle $A$	165
$\dots$	and so on	16	$p \wedge q$	$p$ and $q$	179
$\therefore$	therefore	16	$p \vee q$	$p$ or $q$	179
$1.54$	1.545454...	16	$p \rightarrow q$	if $p$ , then $q$	179
$\{ \}$	set	19	$p \leftrightarrow q$	$p$ if and only if $q$	179
$\in$	is an element of	20	$p'$	not $p$	179
$\notin$	is not an element of	20	$(a, b)$	the ordered pair with first	
$\subset$	is a subset of	20		coordinate $a$ , second	
$\emptyset$	empty set	20		coordinate $b$	188
$J$	set of integers	23	$f: x \rightarrow 2x$	the function $f$ that assigns	
$N$	set of natural numbers	24		$2x$ to $x$	195
$R$	set of rational numbers	24	$f(a)$	the value of the function $f$	
$\mathbb{R}$	set of real numbers	24		at $a$	196
$>$	is greater than	28	$\%$	percent	361
$<$	is less than	28	$\sqrt{a}$	principal square root of $a$	390
$\geq$	is greater than or equal to	28	$\sqrt{\phantom{x}}$	radical sign	390
$\leq$	is less than or equal to	28	$\approx$	is approximately equal to	392
$W$	set of whole numbers	45	$d(P, Q)$	the distance between the	
$\stackrel{?}{=}$	does equal ?, is this			points $P$ and $Q$	403
	statement true?	55	$\sqrt[n]{a}$	the real $n$ th root of $a$	
$\checkmark$	Yes, it is	55		(positive if $n$ is even)	412
$-a$	the additive inverse of $a$	58	$\pm$	plus or minus	421
$> =$	is greater than or equal to		$\text{SQR}(X)$	$\sqrt{X}$ , in BASIC	424
	(in BASIC)	61	$m^\circ \angle A$	degree measure of angle $A$	442
$< =$	is less than or equal to (in		$\sin A$	the sine of angle $A$	445
	BASIC)	61	$\cos A$	the cosine of angle $A$	445
$< >$	is not equal to (in BASIC)	61	$\tan A$	the tangent of angle $A$	445
$ a $	the absolute value of $a$	61	$\ \mathbf{v}\ $	norm of the vector $\mathbf{v}$	459
$\text{ABS}(X)$	the absolute value of $X$ (in		$s$	standard deviation	487
	BASIC)	67	$P(E)$	probability of the event $E$	490





*Two separate athletic events may be held simultaneously in this prototype design for a double stadium.*

# Contents

## *Chapter 1 Numbers and Variables*

**1**

### **Naming Numbers**

1-1 Numbers and Variables in Expressions 1, 1-2 Grouping Symbols 4, 1-3 Powers in Numerical and Variable Expressions 7, 1-4 Numbers and their Graphs 11, Self-Test 1 15.

### **Sets**

1-5 Real Numbers 15, 1-6 Sets and their Members 19, 1-7 Sets of Numbers 22, Self-Test 2 27.

### **Number Sentences**

1-8 Equations and Inequalities 28, 1-9 Applying Open Sentences 31, Self-Test 3 33.

Programming in BASIC 9, On the Calculator 19, Diversions 22, 26, Programming in BASIC 34, Biography: Maria Gaetana Agnesi 37.

Chapter Summary 35, Chapter Review 36, Chapter Test 36.

## *Chapter 2 Basic Properties of Real Numbers*

**39**

### **Axioms and Theorems**

2-1 Quantifiers 39, 2-2 Some Axioms of Addition and Multiplication 42, 2-3 The Distributive Axiom 47, Self-Test 1 52.

### **Addition of Real Numbers**

2-4 Addition on the Number Line 53, 2-5 The Additive Inverse of a Number 57, 2-6 Absolute Value 61, Self-Test 2 64.

Diversion 45, Programming in BASIC 46, Diversion 52, Programming in BASIC 61, 65, 67.

Chapter Summary 65, Chapter Review 66, Chapter Test 67.

## ***Chapter 3 Using Number Properties***

**69**

### **Addition Properties**

3-1 Proving Theorems about Addition 69, 3-2 Adding Real Numbers 73, Self-Test 1 78.

### **Multiplication Properties**

3-3 Multiplying Real Numbers 79, 3-4 The Multiplicative Inverse of a Number 84, Self-Test 2 91.

On the Calculator 84, Programming in BASIC 89, Extra for Experts/Indirect Proof 91, Biography: Elijah McCoy 95, Careers in Forestry 95.

Chapter Summary 93, Chapter Review 93, Chapter Test 94

## ***Chapter 4 Solving Equations and Problems***

**97**

### **Addition and Subtraction Transformations**

4-1 Transforming Equations by Addition 97, 4-2 Subtracting Real Numbers 99, Self-Test 1 106.

### **Multiplication and Division Transformations**

4-3 Transforming Equations by Multiplication 107, 4-4 Dividing Real Numbers 109, 4-5 Using Inverse Operations 115, Self-Test 2 118.

### **Problem Solving**

4-6 From Words to Symbols 119, 4-7 Using Equations to Solve Problems 123, 4-8 Equations Having the Variable in Both Members 127, 4-9 Working with Formulas 132, Self-Test 3 135.

Diversion 106, On the Calculator 135, Programming in BASIC 136.

Chapter Summary 137, Chapter Review 137, Chapter Test 139, Cumulative Review (Chapters 1–4) 140.

## ***Chapter 5 Solving Inequalities and Problems***

**143**

### **Solving Inequalities**

5-1 Axioms of Inequality 143, 5-2 Equivalent Inequalities 148, 5-3 Intersection and Union of Sets 150, 5-4 Combining Inequalities 153, 5-5 Absolute Values in Open Sentences (Optional) 156, Self-Test 1 158.

### **Solving Problems**

5-6 Problems about Integers 159, 5-7 Problems about Angles 164, 5-8 Problems of Uniform Motion 168, 5-9 Mixture Problems; Problems without Solutions 174, Self-Test 2 178.

Diversion 178, Extra for Experts/Symbolic Logic: Boolean Algebra 179, Biography: Amelia Earhart 185, Careers in Architecture 185.

Chapter Summary 182, Chapter Review 183, Chapter Test 184.

## *Chapter 6 Functions, Relations, and Graphs*

187

### **Ordered Pairs and Their Graphs**

6-1 Coordinates in a Plane 187, 6-2 Functions and Relations 191, 6-3 Graphing Relations and Functions 195, Self-Test 1 199.

### **Open Sentences in Two Variables**

6-4 Solving Open Sentences in Two Variables 201, 6-5 The Graph of a Linear Equation in Two Variables 206, 6-6 Direct Variation and Proportion 210, Self-Test 2 217.

### **Lines in a Coordinate Plane**

6-7 Slope and y-Intercept of a Line 218, 6-8 Determining an Equation of a Line: Slope and One Point 221, 6-9 Determining an Equation of a Line: Two Points 223, 6-10 The Graph of a Linear Inequality in Two Variables 227, Self-Test 3 229.

Diversion 197, Programming in BASIC 199, 204, 226, Extra for Experts/Transformations of the Plane: Translations 230.

Chapter Summary 232, Chapter Review 233, Chapter Test 235.

## *Chapter 7 Systems of Open Sentences*

237

### **Solving Systems of Linear Equations in Two Variables**

7-1 Using Graphs 237, 7-2 Using Addition or Subtraction 242, 7-3 Using Linear Combinations 244, 7-4 Using Substitution 247, Self-Test 1 250.

### **Solving Problems**

7-5 Using Two Variables to Solve Problems 251, 7-6 Motion Problems 255, 7-7 Digit Problems 257, Self-Test 2 260.

### **Additional Topics (Optional)**

7-8 Graphs of Systems of Linear Inequalities 260, 7-9 Linear Programming 262, 7-10 Systems of Linear Equations in Three Variables 267, Self-Test 3 271.

Programming in BASIC 250, 266, Extra for Experts/Matrices 272, Biography: R. A. Fisher 277.

Chapter Summary 274, Chapter Review 275, Chapter Test 276.

## *Chapter 8 Polynomials and Their Factors*

279

### **Products**

8-1 Polynomials 279, 8-2 Multiplication and Powers 283, 8-3 Multiplying Polynomials 286, 8-4 Finding Products at Sight 290, Self-Test 1 292.

### **Factors**

8-5 Factoring Monomials 293, 8-6 Factoring Monomials from Polynomials 297, 8-7 Factoring Special Polynomials 299, 8-8 Factoring Quadratic Trinomials (1) 301, 8-9 Factoring Quadratic Trinomials (2) 303, Self-Test 2 305.



### **Applications of Factoring**

8-10 Using Factoring to Solve Equations 306, 8-11 Using Factoring to Solve Problems 310, Self-Test 3 313.

Diversion 283, Programming in BASIC 296, Extra for Experts/Transformations of the Plane: Reflections 314, On the Calculator 318, Biography: Werner von Braun 321.

Chapter Summary 315, Chapter Review 316, Chapter Test 318, Cumulative Review (Chapters 5–8) 319.

## ***Chapter 9 Polynomials and Rational Expressions*** **323**

### **Division of Polynomials**

9-1 Laws of Exponents for Division 323, Dividing a Polynomial by a Monomial 328, 9-3 Quotients of Polynomials: Rational Expressions 331, Self-Test 1 334.

### **Simplifying Rational Expressions**

9-4 Simplifying Rational Expressions 335, 9-5 Zero and Negative Exponents 338, Self-Test 2 341.

### **Operations with Rational Expressions**

9-6 Products and Quotients of Rational Expressions 342, 9-7 Sums and Differences of Rational Expressions (1) 346, 9-8 Sums and Differences of Rational Expressions (2) 348, Self-Test 3 352.

Diversion 338, Programming in BASIC 353, Biography: Margaret Mead 355, Careers in Commercial Art 355.

Chapter Summary 353, Chapter Review 353, Chapter Test 354.

## ***Chapter 10 Rational Expressions in Open Sentences*** **357**

### **Open Sentences Involving Rational Coefficients**

10-1 Open Sentences with Coefficients Named by Fractions 357, 10-2 Percent Problems 361, Self-Test 1 365.

### **Rational Expressions in Equations and Problems**

10-3 Fractional Equations 365, 10-4 Number Problems 369, 10-5 Work Problems 371, 10-6 Motion Problems 373, Self-Test 2 376.

### **Rational Expressions in Types of Variations**

10-7 Inverse Variation 376, 10-8 Joint and Combined Variation 379, Self-Test 3 384.

Biography: Lise Meitner 387, Careers in Teaching 387.

Chapter Summary 384, Chapter Review 385, Chapter Test 386.

## ***Chapter 11 Irrational Numbers and Radicals***

**389**

### **Irrational Numbers**

11-1 Square Roots 389, 11-2 Decimals and Fractions 392, 11-3 Finding Rational Approximations to Square Roots 395, Self-Test 1 398.

### **Using the Pythagorean Theorem**

11-4 The Pythagorean Theorem 399, 11-5 The Distance Formula 403, Self-Test 2 405.

### **Working with Radicals**

11-6 Simplifying Radicals (1) 405, 11-7 Simplifying Radicals (2) 407, 11-8 Sums and Products of Radical Expressions 409, Self-Test 3 411.

Diversion, 394, Programming in BASIC 394, Diversion 398, Programming in BASIC 398, Extra for Experts/ $n$ th Roots 412, On the Calculator 415.

Chapter Summary 413, Chapter Review 414, Chapter Test 415.

## ***Chapter 12 Quadratic Equations and Functions***

**417**

### **Quadratic Equations**

12-1 Completing the Square 417, 12-2 The Quadratic Formula 420, Self-Test 1 424.

### **Quadratic and Other Polynomial Functions**

12-3 Quadratic Functions 425, 12-4 Polynomial Functions 429, 12-5 Quadratic Inequalities 431, Self-Test 2 432.

Diversion 419, Programming in BASIC 424, 433, Extra for Experts/Rational Exponents 433.

Chapter Summary 436, Chapter Review 436, Chapter Test 437, Cumulative Review (Chapters 9–12) 437.

## ***Chapter 13 Trigonometry and Vectors***

**441**

### **Trigonometry**

13-1 Angles 441, 13-2 Trigonometric Functions 445, 13-3 Trigonometric Tables 449, 13-4 Solving Triangles 450, Self-Test 1 458.

### **Vectors**

13-5 Vectors in the Plane 459, 13-6 The Sum of Two Vectors 462, 13-7 Applications of Vectors 466, Self-Test 2 468.

On the Calculator 466, Diversion 466, Biography: Richard Dedekind 471, Careers in Broadcasting, 471.

Chapter Summary 469, Chapter Review 469, Chapter Test 470.

## Graphical Representation of Data

14-1 Dot Frequency Diagrams and Relative Frequency 473, 14-2 Histograms and Frequency Polygons 476, 14-3 Cumulative Frequency 480, Self-Test 1 483.

## Arithmetical Description of Data

14-4 Statistical Averages 484, 14-5 Measures of Variation 486, Self-Test 2 488.

## Probability

14-6 The Probability of an Event 489, 14-7 Experimental Probability 492, Self-Test 3 495.

Diversions 476, 483, Careers in Farming, 497

Chapter Summary 495, Chapter Review 496, Chapter Test 497.

## Comprehensive Review (Chapters 1-14)

498

## Tables

501

## Extra Practice

505

## Answers to Self-Tests

521

## Glossary

527

## Index

535

## Answers to Selected Exercises

543

# 1

# Numbers and Variables

## Naming Numbers

**OBJECTIVES** for Sections 1-1 through 1-4:

1. *Simplify numerical expressions which involve arithmetic operations, powers, or grouping symbols.*
2. *Evaluate variable expressions.*
3. *Graph numbers, and state the coordinates of points, on the number line.*
4. *Express measurements by means of directed numbers.*

### 1-1 Numbers and Variables in Expressions

One kind of symbol used in algebra is a *numeral*, or *numerical expression*. A **numerical expression** is simply a name for a number. The number is called the **value** of the expression. For example,

$4 \times 9$  is a numerical expression for the number 36.  
36 is the value of  $4 \times 9$ .

You can use the equality symbol,  $=$ , and write

$$4 \times 9 = 36.$$

Whenever you replace a numerical expression with the simplest, or most common, name of its value, you say that you have **simplified the expression**.

In simplifying a numerical expression, you use the following fact:

### Substitution Principle

Changing the numeral by which a number is named in an expression does not change the value of the expression.

Below are several expressions and their values:

Numerical Expression	Value	You write:
$15 + 12$	27	$15 + 12 = 27$
$5 - 1$	4	$5 - 1 = 4$
$7 \times 8$ (or $7 \cdot 8$ )	56	$7 \times 8 = 56$
$42 \div 6$	7	$42 \div 6 = 7$

Another kind of symbol used in algebra is a *variable*, or a *variable expression*. A **variable** is a letter such as  $n$ ,  $a$ , or  $x$ , or a symbol such as  $\frac{?}{?}$ , used to stand for a number or numbers. A **variable expression** is an expression containing at least one variable, but it may also contain other symbols, including numerals. The set of numbers that a variable can stand for is called the **replacement set**, or **domain**, of the variable. The members of the domain are the **values** of the variable. For example, if  $n$  can stand for 2 or 5, then you write  $n = 2$  or  $n = 5$ .  $3 \times n$  is a variable expression.

If  $n = 2$ , then  $3 \times n = 3 \times 2 = 6$ .

If  $n = 5$ , then  $3 \times n = 3 \times 5 = 15$ .

This is called **evaluating the expression**. In a variable expression like  $3 \times n$ , the multiplication sign is often omitted.

$3 \times n$  may be written  $3n$ .

**EXAMPLE** Evaluate each expression for the given value of each variable.

a.  $x - 3$ ;  $x = 7$

b.  $5y$ ;  $y = 8$

c.  $9 - \frac{12}{n}$ ;  $n = 3$

d.  $a + b - 2$ ;  $a = 4$  and  $b = 11$

**SOLUTION**

a.  $x - 3 = 7 - 3 = 4$

b.  $5y = 5 \times y = 5 \times 8 = 40$

c.  $9 - \frac{12}{n} = 9 - \frac{12}{3} = 9 - 4 = 5$

d.  $a + b - 2 = 4 + 11 - 2 = 13$

## Oral Exercises

Give the simplest name of the value of each expression.

1.  $12 + 31$

2.  $57 - 31$

3.  $120 \div 4$

4.  $8 \times 24$

Evaluate each expression when  $x = 4$ .

5.  $x - 2$

6.  $7x$

7.  $8 - \frac{12}{x}$

8.  $10 + x$

Evaluate each expression when  $a = 3$  and  $b = 5$ .

9.  $a + b$

10.  $b - a$

11.  $\frac{a + b}{2}$

12.  $ab$

13. If  $y = 5$ , write four variable expressions using  $y$  that have a value of 10.

14. If  $m = 1$ , how many variable expressions can be written using  $m$  that have a value of 1?

## Written Exercises

Give the simplest name of the value of each expression.

- A**
- |                   |                   |                             |                    |
|-------------------|-------------------|-----------------------------|--------------------|
| 1. $352 + 226$    | 2. $537 + 138$    | 3. $1642 - 853$             | 4. $1980 - 1974$   |
| 5. $1185 \div 5$  | 6. $9690 \div 19$ | 7. $215 \times 13$          | 8. $57 \times 348$ |
| 9. $3 + 12 + 413$ | 10. $8753 - 985$  | 11. $9 \times 12 \times 21$ | 12. $5656 \div 56$ |

Evaluate the expression.

- |   |  |
|---|--|
| 13. $x + 5$ when $x = 7$  | 14. $7 - x$ when $x = 0$                                     |
| 15. $10 + x$ when $x = 3$   | 16. $3x$ when $x = 9$  |
| 17. $5x$ when $x = 1$   | 18. $\frac{15}{x}$ when $x = 3$                              |
| 19. $\frac{x}{8}$ when $x = 0$                                    | 20. $x - 9$ when $x = 11$                                    |
| 21. $c + d$ when $c = 5$ and $d = 8$                              | 22. $d - c$ when $c = 4$ and $d = 7$                         |
| 23. $c - d$ when $c = 1$ and $d = 0$                              | 24. $cd$ when $c = 9$ and $d = 8$                            |
| 25. $\frac{c}{d}$ when $c = 14$ and $d = 2$                       | 26. $\frac{d}{c}$ when $c = 75$ and $d = 25$                 |
| 27. $c + d - 4$ when $c = 9$ and $d = 3$                          | 28. $c - d + 5$ when $c = 18$ and $d = 9$                    |
| <b>B</b> 29. $c + d$ when $c = \frac{1}{3}$ and $d = \frac{3}{4}$ | 30. $c + d - 1$ when $c = \frac{3}{4}$ and $d = \frac{5}{8}$ |
| 31. $c - d + 1$ when $c = 1.25$ and $d = 0.33$                    | 32. $c - d + 1$ when $c = 0.65$ and $d = 0.27$               |
| 33. $cd + 1$ when $c = \frac{7}{8}$ and $d = \frac{4}{3}$         | 34. $cd - 1$ when $c = 2\frac{1}{4}$ and $d = 4$             |



Evaluate the expression.

35.  $\frac{c}{d}$  when  $c = \frac{1}{2}$  and  $d = \frac{3}{4}$
36.  $\frac{c}{d} - 1$  when  $c = 1.25$  and  $d = 0.5$
37.  $\frac{d}{c} + 1$  when  $c = 1.25$  and  $d = 0.5$
38.  $e + f + g$  when  $e = \frac{1}{2}$ ,  $f = \frac{1}{3}$ , and  $g = \frac{1}{4}$
39.  $efg$  when  $e = \frac{2}{3}$ ,  $f = \frac{3}{4}$ , and  $g = 16$
40.  $gfe$  when  $e = \frac{2}{3}$ ,  $f = \frac{3}{4}$  and  $g = 16$
41. Show that the expressions  $x + y$  and  $y + x$  have the same value when  $x = \frac{1}{3}$  and  $y = \frac{1}{5}$ .
42. Show that the expressions  $\frac{x+y}{2}$  and  $\frac{x}{2} + \frac{y}{2}$  have the same value when  $x = \frac{1}{2}$  and  $y = \frac{1}{4}$ .
43. Find values for  $x$  and  $y$  that make the expressions  $x - y$  and  $y - x$  have the same value.
44. Find values for  $x$  and  $y$  that make the expressions  $x + y$  and  $xy$  have the same value.

## 1-2 Grouping Symbols

When more than one operation must be done to find the value of an expression, **parentheses** ( ) are often used to make clear the order in which the operations are to be carried out.

$2 \cdot 5 + 8$  could mean

Either	Or
$(2 \cdot 5) + 8 =$	$2 \cdot (5 + 8) =$
$10 + 8 =$	$2 \cdot 13 =$
18	26
← different values →	

A pair of parentheses is a **grouping symbol**. Brackets and braces may also be used as grouping symbols:

Parentheses	Brackets	Braces
$2 \cdot (5 + 8)$	$2 \cdot [5 + 8]$	$2 \cdot \{5 + 8\}$

The product  $2 \cdot (5 + 8)$  is usually written without the multiplication dot simply as  $2(5 + 8)$ . A product like  $2 \cdot 13$  may be written

$2(13)$  or  $(2)13$  or  $(2)(13)$

Variables are grouped in the same way as numbers. But:

$2n + 8$  always means  $(2n) + 8$   
 $3n - 5$  always means  $(3n) - 5$   
 $19 \div 4n$  always means  $19 \div (4n)$

Notice that in a fraction like  $\frac{3+7}{11}$  or  $\frac{n+2}{9}$ , the bar is both a division sign and a grouping symbol. Thus,  $\frac{3+7}{11} = \frac{10}{11}$ .

When  $n = 5$ ,  $\frac{n+2}{9} = \frac{5+2}{9} = \frac{7}{9}$ .

In the numerical expression in Example 1, below, you see a pair of parentheses inside a pair of brackets. Notice that to simplify such an expression, you first simplify the numeral in the innermost grouping symbol, then work toward the outermost grouping symbol.

**EXAMPLE 1** Find the value of  $5[24 - 3(7)]$ .

**SOLUTION** 
$$\begin{aligned} 5[24 - 3(7)] &= 5[24 - 21] \\ &= 5(3) \\ &= 15 \end{aligned}$$

**EXAMPLE 2** Find the value of  $3(x + 4) - 2x$  when  $x = 5$ .

**SOLUTION** 
$$\begin{aligned} 3(x + 4) - 2x &= 3(5 + 4) - 2(5) \\ &= 3(9) - 2(5) \\ &= 27 - 10 \\ &= 17 \end{aligned}$$

**EXAMPLE 3** If  $n$  has the replacement set  $\{2, 3, 4\}$ , find the corresponding values of  $5n - 7$ .

<b>SOLUTION</b>	When $n = 2$ ,	When $n = 3$ ,	When $n = 4$ ,
	$5n - 7 = 5(2) - 7$	$5n - 7 = 5(3) - 7$	$5n - 7 = 5(4) - 7$
	$= 10 - 7$	$= 15 - 7$	$= 20 - 7$
	$= 3$	$= 8$	$= 13$

## Oral Exercises

Find the value of each expression.

- $6(3) + 5$
- $56 - 3(8)$
- $4(3 + 7)$
- $9(8 - 4)$
- $(4 \cdot 4) + (5 \cdot 5)$
- $(7 \cdot 6) - (5 \cdot 4)$
- $\frac{23 + 4}{3 + 6}$
- $\frac{5(6)}{4(15)}$
- $\frac{5 \times 9}{2 + 7}$
- $2(5) + \frac{18}{6}$
- $\frac{18 - 4}{1 \times 2}$
- $(7 - 4)(3 + 5)$
- $2x + (x + 1)$  when  $x = 4$
- $3(x - 1) - x$  when  $x = 6$
- $5x - 3$  when  $x = 3$
- $x + 2(x + 3)$  when  $x = 5$
- If  $y$  has the replacement set  $\{1, 2, 3\}$ , find the corresponding values of  $3y - 2$ .
- Can you find the replacement set for  $2x + 3$  if the corresponding values are 3, 13, and 19?

## Written Exercises

Find the value of each expression.

- A**
- $20(5)(3)$
  - $17 + (5 + 15)$
  - $(23 + 4) + 7$
  - $8(3) + 30(3)$
  - $5(25 + 15)$
  - $(17 + 8)9$
  - $\frac{80 - 10}{15 + 20}$
  - $\frac{(5 \cdot 7) + 5}{(9 \cdot 3) - 7}$
  - $\frac{(6)(6) + (8)(8)}{(4)(4) + (3)(3)}$
  - $[18 - (9)(2)]3$
  - $4[3(3) + 4(5)]$
  - $[35 - 3(4)] + 25$
  - $[(8)(7) - (2)(3)] \div 2$
  - $[5(5) + 4(6)] \div 7$
  - $[9(7) - 8(0)] \div 9$
  - $2(x + 2) - 2$  when  $x = 2$
  - $16 - 3(y - 5)$  when  $y = 7$
  - $5(a + 5) + 5$  when  $a = 10$
  - $15 + 6(w + 1)$  when  $w = 6$
  - $2u + (u + 3)$  when  $u = 8$
  - $9v - 10$  when  $v = 25$
  - $(7x - 5) + 3$  when  $x = 12$
  - $15 + (5y - 5)$  when  $y = 1$
  - If  $x$  has the replacement set  $\{2, 4, 6\}$ , find the corresponding values of  $4x - 1$ .
  - If  $y$  has the replacement set  $\{1, 3, 5\}$ , find the corresponding values of  $5y + 3$ .
  - If  $t$  has the replacement set  $\{2, 3, 5\}$ , find the corresponding values of  $100t - 10$ .
- B**
- $[7(2) - 4] + [9 + 8(4)]$
  - $2[3(5) - 7] + [10 + 4(6)]$
  - $[5(9) + 8][8 + 9(5)]0$
  - $5[(8)(4) + 8] - (8)5$
  - $\{6 + 2[3(2) + 1] + 1\}3$
  - $2\{[3(2) + 5] + 3\}$
  - $\{(6 \cdot 250) \div [8(8) \div (4 \cdot 4)]\} + [25(12 \div 6)]$
  - $\{[(23 - 7)(6 + 4)] + 340\} - \{(48 \div 4)[24(7) \div (18 - 4)]\}$
  - $2(x - 1) + 3(x + 2) + 1$  when  $x = 10$
  - $3(2y + 3)(y - 2)$  when  $y = 3$
  - $5[(3w - 4) + (2w + 4)]$  when  $w = 2$
  - $(3w - 1)(3w + 1) + (2w + 1)(2w - 1)$  when  $w = 2$
  - $\frac{4u + 3}{2u + 3} + 2u + 1$  when  $u = 6$
  - If  $x$  has the replacement set  $\{10, 20, 30\}$ , find the corresponding values of  $10x + 2(x + 10)$ .
  - If  $y$  has the replacement set  $\{0, 2, 4, 6, 8\}$ , find the corresponding values of  $\frac{4y + 4}{2}$ .
  - If  $t$  has the replacement set  $\{10, 100, 1000, 10,000\}$ , find the corresponding values of  $4(t - 1) + 2(t - 1)$ .
  - If  $u$  has the replacement set  $\{1, 2, 3, 4, 5, 6, 7, 8, 9\}$ , find the greatest corresponding value of  $\frac{2u - 1}{2u}$ .
  - If  $v$  has the replacement set  $\{\frac{1}{2}, \frac{1}{3}, \frac{1}{4}, \frac{1}{5}\}$ , find the corresponding values of  $\frac{1}{2v}$ . Which is the least corresponding value?