

# PETROLEUM PRODUCTION HANDBOOK

IN TWO VOLUMES

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The Atlantic Refining Company*

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VOLUME I

MATHEMATICS AND PRODUCTION EQUIPMENT

Society of Petroleum Engineers of AIME

Dallas, Texas

**PETROLEUM PRODUCTION HANDBOOK**

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## PREFACE

The *Petroleum Production Handbook* fills a long-time need for a comprehensive volume presenting practical information and data concerning the recovery of oil and gas from the underground reservoirs in which they occur. Petroleum production has progressed from the haphazard methods employed during the days of the "gusher" to a complex science requiring wide knowledge of available downhole and lease equipment and of the established engineering methods for controlling reservoir mechanics. Because the Handbook brings the important equipment and methods into perspective, it should prove to be the most important book in the library of the person engaged in this field of work.

The book is divided into two volumes and three sections. Volume I contains Section 1—Mathematics and Section 2—Production Equipment. In Volume II is Section 3—Reservoir Engineering. Within these sections are 47 chapters, each written by top experts in the particular field covered. Also included is the list of "Letter Symbols for Petroleum Engineering and Electric Logging" sponsored by the Society of Petroleum Engineers of AIME and accepted as a Standard by the American Standard Association.

The Mathematics Section presents the basic tables and calculation procedures required by the person engaged in petroleum production. The Production Equipment Section covers basic types of materials and tools available for use, including their capabilities and proper applications. Within the Reservoir Engineering Section are chapters treating formation rocks, fluids and gases, correlation methods, primary and secondary recovery data, and well treating.

Acknowledgement for exceptional cooperation is given to the Society of Petroleum Engineers of AIME, the American Petroleum Institute, the U.S. Bureau of Mines and the individual authors who are responsible for the excellent material presented within these pages. Also, appreciation is expressed to the following experts who reviewed material published in this Handbook:

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The rapid progress of petroleum technology has been due to the willingness of its leaders to freely publish important data for use by the entire industry. It is our hope that this *Petroleum Production Handbook* will contribute to this fund of knowledge and, in doing so, will lead to further progress in the economic recovery of oil and gas.

*Thomas C. Frick*

# CONTENTS

<i>Contributors</i> . . . . .	vii
<i>Preface</i> . . . . .	xi

## VOLUME I. MATHEMATICS AND PRODUCTION EQUIPMENT

### SECTION 1. MATHEMATICS

Chapter 1. Mathematical Tables and Weights and Measures . . . . .	1-3
---	-----

### SECTION 2. PRODUCTION EQUIPMENT

Chapter 2. Casing, Tubing, and Line Pipe . . . . .	2-1
Chapter 3. Wellhead Equipment and Flow-control Devices . . . . .	3-1
Chapter 4. Production Packers . . . . .	4-1
Chapter 5. Gass Lift . . . . .	5-1
Chapter 6. Hydraulic Pumps . . . . .	6-1
Chapter 7. Subsurface Sucker-rod Pumps . . . . .	7-1
Chapter 8. Sucker Rods . . . . .	8-1
Chapter 9. Pumping Units and Prime Movers for Pumping Units . . . . .	9-1
Chapter 10. Oil Storage . . . . .	10-1
Chapter 11. Oil and Gas Separators . . . . .	11-1
Chapter 12. Gas Measurement and Regulation . . . . .	12-1
Chapter 13. Lease-operated Hydrocarbon-recovery Systems and Gas-treating Systems . . . . .	13-1
Chapter 14. Surface Facilities for Waterflooding and Salt-water Disposal . . . . .	14-1
Chapter 15. Automation of Lease Equipment . . . . .	15-1
Chapter 16. Measuring, Sampling, and Testing Crude Oil . . . . .	16-1

## VOLUME II. RESERVOIR ENGINEERING

### SECTION 3. RESERVOIR ENGINEERING

Chapter 17. Gas Properties and Correlations . . . . .	17-3
Chapter 18. Properties of Crude Oils and Liquid Condensate . . . . .	18-1

Chapter 19.	Oil-system Correlations . . . . .	19-1
Chapter 20.	Phase Diagrams . . . . .	20-1
Chapter 21.	Properties of Produced Waters . . . . .	21-1
Chapter 22.	Hydrocarbon-water and Formation Water Correlations . . . . .	22-1
Chapter 23.	Properties of Reservoir Rocks . . . . .	23-1
Chapter 24.	Typical Core Analysis of Different Formations . . . . .	24-1
Chapter 25.	Relative Permeability . . . . .	25-1
Chapter 26.	Reservoir Traps . . . . .	26-1
Chapter 27.	Bottom-hole Pressures . . . . .	27-1
Chapter 28.	Temperatures in Wells . . . . .	28-1
Chapter 29.	Potential Tests for Oil Wells . . . . .	29-1
Chapter 30.	Open Flow of Gas Wells . . . . .	30-1
Chapter 31.	Wellbore Hydraulics . . . . .	31-1
Chapter 32.	Reservoir Performance Equations . . . . .	32-1
Chapter 33.	Development Plan for Oil Reservoirs . . . . .	33-1
Chapter 34.	Solution-gas-drive Oil Reservoirs . . . . .	34-1
Chapter 35.	Water-drive Oil Reservoirs . . . . .	35-1
Chapter 36.	Gas-condensate Reservoirs . . . . .	36-1
Chapter 37.	Estimation of Primary Oil and Gas Reserves . . . . .	37-1
Chapter 38.	Valuation of Oil and Gas Reserves . . . . .	38-1
Chapter 39.	Injection Operations . . . . .	39-1
Chapter 40.	Gas-injection Pressure Maintenance and Miscible-phase Displacement in Oil Reservoirs . . . . .	40-1
Chapter 41.	Water-injection Pressure Maintenance and Waterflood Processes . . . . .	41-1
Chapter 42.	Standard Letter Symbols for Petroleum Reservoir Engineering and Electric Logging . . . . .	42-1
Chapter 43.	Electrical Logging . . . . .	43-1
Chapter 44.	Radioactivity Well Logging . . . . .	44-1
Chapter 45.	Miscellaneous Well Logs . . . . .	45-1
Chapter 46.	Acidizing . . . . .	46-1
Chapter 47.	Formation Fracturing . . . . .	47-1
Chapter 48.	Remedial Clean-up and Other Stimulation Treatments . . . . .	48-1
Chapter 49.	Oil and Gas Leases . . . . .	49-1

*Index follows Chapter 49.*

*Section 1*

**MATHEMATICS**



# Chapter 1

## MATHEMATICAL TABLES AND WEIGHTS AND MEASURES\*

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### CONTENTS

#### MATHEMATICAL TABLES

By PHILIP FRANKLIN

	PAGE
Squares of Numbers.....	1-4
Cubes of Numbers.....	1-10
Square Roots of Numbers.....	1-14
Cube Roots of Numbers.....	1-18
Three-halves Powers of Numbers.....	1-24
Reciprocals of Numbers.....	1-26
Circles (Areas, Segments, etc.).....	1-30
Spheres (Volumes, Segments, etc.).....	1-36
Regular Polygons.....	1-41
Binomial Coefficients.....	1-41
Common Logarithms.....	1-42
Degrees and Radians.....	1-46
Trigonometric Functions.....	1-48
Exponentials.....	1-59
Natural (Napierian) Logarithms.....	1-60
Hyperbolic Functions.....	1-62
Multiples of 0.4343 and 2.3026.....	1-64
Residuals and Probable Errors.....	1-65
Compound Interest and Annuities.....	1-66
Decimal Equivalents.....	1-71

#### WEIGHTS AND MEASURES

By LEWIS V. JUDSON

	PAGE
U.S. Customary Weights and Measures....	1-72
Metric Weights and Measures.....	1-73
Systems of Units.....	1-74
Conversion Tables:	
Lengths.....	1-76
Areas.....	1-78
Volumes and Capacities.....	1-78
Masses (Weights).....	1-79
Velocities.....	1-80
Pressures.....	1-81
Energy, Work, Heat.....	1-82
Power.....	1-83
Density.....	1-84
Thermal Conductivity.....	1-84
Thermal Conductance.....	1-84
Time.....	1-85
Terrestrial Gravity.....	1-86
Specific Gravity and Density.....	1-86
Specific Gravity, API and Baumé.....	1-87
Mohs Scale of Hardness.....	1-88

REFERENCES FOR MATHEMATICAL TABLES: Allen, "Six-place Tables," McGraw-Hill. Comrie, "Chambers Shorter Six-figure Mathematical Tables," Chemical Publishing. Dwight, "Mathematical Tables of Elementary and Some Higher Mathematical Functions," McGraw-Hill. Dwight, "Tables of Integrals and Other Mathematical Data," Macmillan. Jahnke and Emde, "Tables of Functions," B. G. Teubner, Leipzig, or Dover. Peirce-Foster, "A Short Table of Integrals," Ginn. "Handbook of Chemistry and Physics," Chemical Rubber Co.

\* From Marks' *Mechanical Engineers' Handbook*, Theodore Baumeister (ed.), 6th ed., McGraw-Hill, 1958.

## Squares of Numbers

<i>N</i>	0	1	2	3	4	5	6	7	8	9	Avg diff
<b>1.00</b>	1.000	1.002	1.004	1.006	1.008	1.010	1.012	1.014	1.016	1.018	2
1	1.020	1.022	1.024	1.026	1.028	1.030	1.032	1.034	1.036	1.038	
2	1.040	1.042	1.044	1.047	1.049	1.051	1.053	1.055	1.057	1.059	
3	1.061	1.063	1.065	1.067	1.069	1.071	1.073	1.075	1.077	1.080	
4	1.082	1.084	1.086	1.088	1.090	1.092	1.094	1.096	1.098	1.100	
<b>1.05</b>	1.102	1.105	1.107	1.109	1.111	1.113	1.115	1.117	1.119	1.121	
6	1.124	1.126	1.128	1.130	1.132	1.134	1.136	1.138	1.141	1.143	
7	1.145	1.147	1.149	1.151	1.153	1.156	1.158	1.160	1.162	1.164	
8	1.166	1.169	1.171	1.173	1.175	1.177	1.179	1.182	1.184	1.186	
9	1.188	1.190	1.192	1.195	1.197	1.199	1.201	1.203	1.206	1.208	
<b>1.10</b>	1.210	1.212	1.214	1.217	1.219	1.221	1.223	1.225	1.228	1.230	
1	1.232	1.234	1.237	1.239	1.241	1.243	1.245	1.248	1.250	1.252	
2	1.254	1.257	1.259	1.261	1.263	1.266	1.268	1.270	1.272	1.275	
3	1.277	1.279	1.281	1.284	1.286	1.288	1.290	1.293	1.295	1.297	
4	1.300	1.302	1.304	1.306	1.309	1.311	1.313	1.316	1.318	1.320	
<b>1.15</b>	1.322	1.325	1.327	1.329	1.332	1.334	1.336	1.339	1.341	1.343	
6	1.346	1.348	1.350	1.353	1.355	1.357	1.360	1.362	1.364	1.367	
7	1.369	1.371	1.374	1.376	1.378	1.381	1.383	1.385	1.388	1.390	
8	1.392	1.395	1.397	1.399	1.402	1.404	1.407	1.409	1.411	1.414	
9	1.416	1.418	1.421	1.423	1.426	1.428	1.430	1.433	1.435	1.438	
<b>1.20</b>	1.440	1.442	1.445	1.447	1.450	1.452	1.454	1.457	1.459	1.462	
1	1.464	1.467	1.469	1.471	1.474	1.476	1.479	1.481	1.484	1.486	
2	1.488	1.491	1.493	1.496	1.498	1.501	1.503	1.506	1.508	1.510	
3	1.513	1.515	1.518	1.520	1.523	1.525	1.528	1.530	1.533	1.535	
4	1.538	1.540	1.543	1.545	1.548	1.550	1.553	1.555	1.558	1.560	
<b>1.25</b>	1.562	1.565	1.568	1.570	1.573	1.575	1.578	1.580	1.583	1.585	3
6	1.588	1.590	1.593	1.595	1.598	1.600	1.603	1.605	1.608	1.610	
7	1.613	1.615	1.618	1.621	1.623	1.626	1.628	1.631	1.633	1.636	
8	1.638	1.641	1.644	1.646	1.649	1.651	1.654	1.656	1.659	1.662	
9	1.664	1.667	1.669	1.672	1.674	1.677	1.680	1.682	1.685	1.687	
<b>1.30</b>	1.690	1.693	1.695	1.698	1.700	1.703	1.706	1.708	1.711	1.713	
1	1.716	1.719	1.721	1.724	1.727	1.729	1.732	1.734	1.737	1.740	
2	1.742	1.745	1.748	1.750	1.753	1.756	1.758	1.761	1.764	1.766	
3	1.769	1.772	1.774	1.777	1.780	1.782	1.785	1.788	1.790	1.793	
4	1.796	1.798	1.801	1.804	1.806	1.809	1.812	1.814	1.817	1.820	
<b>1.35</b>	1.822	1.825	1.828	1.831	1.833	1.836	1.839	1.841	1.844	1.847	
6	1.850	1.852	1.855	1.858	1.860	1.863	1.866	1.869	1.871	1.874	
7	1.877	1.880	1.882	1.885	1.888	1.891	1.893	1.896	1.899	1.902	
8	1.904	1.907	1.910	1.913	1.915	1.918	1.921	1.924	1.927	1.929	
9	1.932	1.935	1.938	1.940	1.943	1.946	1.949	1.952	1.954	1.957	
<b>1.40</b>	1.960	1.963	1.966	1.968	1.971	1.974	1.977	1.980	1.982	1.985	
1	1.988	1.991	1.994	1.997	1.999	2.002	2.005	2.008	2.011	2.014	
2	2.016	2.019	2.022	2.025	2.028	2.031	2.033	2.036	2.039	2.042	
3	2.045	2.048	2.051	2.053	2.056	2.059	2.062	2.065	2.068	2.071	
4	2.074	2.076	2.079	2.082	2.085	2.088	2.091	2.094	2.097	2.100	
<b>1.45</b>	2.102	2.105	2.108	2.111	2.114	2.117	2.120	2.123	2.126	2.129	
6	2.132	2.135	2.137	2.140	2.143	2.146	2.149	2.152	2.155	2.158	
7	2.161	2.164	2.167	2.170	2.173	2.176	2.179	2.182	2.184	2.187	
8	2.190	2.193	2.196	2.199	2.202	2.205	2.208	2.211	2.214	2.217	
9	2.220	2.223	2.226	2.229	2.232	2.235	2.238	2.241	2.244	2.247	

Moving the decimal point ONE place in *N* requires moving it TWO places in body of table (see p. 1-8).

Squares (continued)

N	0	1	2	3	4	5	6	7	8	9	Avg diff
1.50	2.250	2.253	2.256	2.259	2.262	2.265	2.268	2.271	2.274	2.277	3
1	2.280	2.283	2.286	2.289	2.292	2.295	2.298	2.301	2.304	2.307	
2	2.310	2.313	2.316	2.320	2.323	2.326	2.329	2.332	2.335	2.338	
3	2.341	2.344	2.347	2.350	2.353	2.356	2.359	2.362	2.365	2.369	
4	2.372	2.375	2.378	2.381	2.384	2.387	2.390	2.393	2.396	2.399	
1.55	2.402	2.406	2.409	2.412	2.415	2.418	2.421	2.424	2.427	2.430	
6	2.434	2.437	2.440	2.443	2.446	2.449	2.452	2.455	2.459	2.462	
7	2.465	2.468	2.471	2.474	2.477	2.481	2.484	2.487	2.490	2.493	
8	2.496	2.500	2.503	2.506	2.509	2.512	2.515	2.519	2.522	2.525	
9	2.528	2.531	2.534	2.538	2.541	2.544	2.547	2.550	2.554	2.557	
1.60	2.560	2.563	2.566	2.570	2.573	2.576	2.579	2.582	2.586	2.589	
1	2.592	2.595	2.599	2.602	2.605	2.608	2.611	2.615	2.618	2.621	
2	2.624	2.628	2.631	2.634	2.637	2.641	2.644	2.647	2.650	2.654	
3	2.657	2.660	2.663	2.667	2.670	2.673	2.676	2.680	2.683	2.686	
4	2.690	2.693	2.696	2.699	2.703	2.706	2.709	2.713	2.716	2.719	
1.65	2.722	2.726	2.729	2.732	2.736	2.739	2.742	2.746	2.749	2.752	
6	2.756	2.759	2.762	2.766	2.769	2.772	2.776	2.779	2.782	2.786	
7	2.789	2.792	2.796	2.799	2.802	2.806	2.809	2.812	2.816	2.819	
8	2.822	2.826	2.829	2.832	2.836	2.839	2.843	2.846	2.849	2.853	
9	2.856	2.859	2.863	2.866	2.870	2.873	2.876	2.880	2.883	2.887	
1.70	2.890	2.893	2.897	2.900	2.904	2.907	2.910	2.914	2.917	2.921	
1	2.924	2.928	2.931	2.934	2.938	2.941	2.945	2.948	2.952	2.955	
2	2.958	2.962	2.965	2.969	2.972	2.976	2.979	2.983	2.986	2.989	
3	2.993	2.996	3.000	3.003	3.007	3.010	3.014	3.017	3.021	3.024	
4	3.028	3.031	3.035	3.038	3.042	3.045	3.049	3.052	3.056	3.059	
1.75	3.062	3.066	3.070	3.073	3.077	3.080	3.084	3.087	3.091	3.094	4
6	3.098	3.101	3.105	3.108	3.112	3.115	3.119	3.122	3.126	3.129	
7	3.133	3.136	3.140	3.144	3.147	3.151	3.154	3.158	3.161	3.165	
8	3.168	3.172	3.176	3.179	3.183	3.186	3.190	3.193	3.197	3.201	
9	3.204	3.208	3.211	3.215	3.218	3.222	3.226	3.229	3.233	3.236	
1.80	3.240	3.244	3.247	3.251	3.254	3.258	3.262	3.265	3.269	3.272	
1	3.276	3.280	3.283	3.287	3.291	3.294	3.298	3.301	3.305	3.309	
2	3.312	3.316	3.320	3.323	3.327	3.331	3.334	3.338	3.342	3.345	
3	3.349	3.353	3.356	3.360	3.364	3.367	3.371	3.375	3.378	3.382	
4	3.386	3.389	3.393	3.397	3.400	3.404	3.408	3.411	3.415	3.419	
1.85	3.422	3.426	3.430	3.434	3.437	3.441	3.445	3.448	3.452	3.456	
6	3.460	3.463	3.467	3.471	3.474	3.478	3.482	3.486	3.489	3.493	
7	3.497	3.501	3.504	3.508	3.512	3.516	3.519	3.523	3.527	3.531	
8	3.534	3.538	3.542	3.546	3.549	3.553	3.557	3.561	3.565	3.568	
9	3.572	3.576	3.580	3.583	3.587	3.591	3.595	3.599	3.602	3.606	
1.90	3.610	3.614	3.618	3.621	3.625	3.629	3.633	3.637	3.640	3.644	
1	3.648	3.652	3.656	3.660	3.663	3.667	3.671	3.675	3.679	3.683	
2	3.686	3.690	3.694	3.698	3.702	3.706	3.709	3.713	3.717	3.721	
3	3.725	3.729	3.733	3.736	3.740	3.744	3.748	3.752	3.756	3.760	
4	3.764	3.767	3.771	3.775	3.779	3.783	3.787	3.791	3.795	3.799	
1.95	3.802	3.806	3.810	3.814	3.818	3.822	3.826	3.830	3.834	3.838	
6	3.842	3.846	3.849	3.853	3.857	3.861	3.865	3.869	3.873	3.877	
7	3.881	3.885	3.889	3.893	3.897	3.901	3.905	3.909	3.912	3.916	
8	3.920	3.924	3.928	3.932	3.936	3.940	3.944	3.948	3.952	3.956	
9	3.960	3.964	3.968	3.972	3.976	3.980	3.984	3.988	3.992	3.996	

$\pi^2 = 9.86960$        $1/\pi^2 = 0.101321$        $e^2 = 7.38906$

## Squares (continued)

<i>N</i>	0	1	2	3	4	5	6	7	8	9	Avg diff
<b>2.00</b>	4.000	4.004	4.008	4.012	4.016	4.020	4.024	4.028	4.032	4.036	4
1	4.040	4.044	4.048	4.052	4.056	4.060	4.064	4.068	4.072	4.076	
2	4.080	4.084	4.088	4.093	4.097	4.101	4.105	4.109	4.113	4.117	
3	4.121	4.125	4.129	4.133	4.137	4.141	4.145	4.149	4.153	4.158	
4	4.162	4.166	4.170	4.174	4.178	4.182	4.186	4.190	4.194	4.198	
<b>2.05</b>	4.202	4.207	4.211	4.215	4.219	4.223	4.227	4.231	4.235	4.239	
6	4.244	4.248	4.252	4.256	4.260	4.264	4.268	4.272	4.277	4.281	
7	4.285	4.289	4.293	4.297	4.301	4.306	4.310	4.314	4.318	4.322	
8	4.326	4.331	4.335	4.339	4.343	4.347	4.351	4.356	4.360	4.364	
9	4.368	4.372	4.376	4.381	4.385	4.389	4.393	4.397	4.402	4.406	
<b>2.10</b>	4.410	4.414	4.418	4.423	4.427	4.431	4.435	4.439	4.444	4.448	
1	4.452	4.456	4.461	4.465	4.469	4.473	4.477	4.482	4.486	4.490	
2	4.494	4.499	4.503	4.507	4.511	4.516	4.520	4.524	4.528	4.533	
3	4.537	4.541	4.545	4.550	4.554	4.558	4.562	4.567	4.571	4.575	
4	4.580	4.584	4.588	4.592	4.597	4.601	4.605	4.610	4.614	4.618	
<b>2.15</b>	4.622	4.627	4.631	4.635	4.640	4.644	4.648	4.653	4.657	4.661	
6	4.666	4.670	4.674	4.679	4.683	4.687	4.692	4.696	4.700	4.705	
7	4.709	4.713	4.718	4.722	4.726	4.731	4.735	4.739	4.744	4.748	
8	4.752	4.757	4.761	4.765	4.770	4.774	4.779	4.783	4.787	4.792	
9	4.796	4.800	4.805	4.809	4.814	4.818	4.822	4.827	4.831	4.836	
<b>2.20</b>	4.840	4.844	4.849	4.853	4.858	4.862	4.866	4.871	4.875	4.880	
1	4.884	4.889	4.893	4.897	4.902	4.906	4.911	4.915	4.920	4.924	
2	4.928	4.933	4.937	4.942	4.946	4.951	4.955	4.960	4.964	4.968	
3	4.973	4.977	4.982	4.986	4.991	4.995	5.000	5.004	5.009	5.013	
4	5.018	5.022	5.027	5.031	5.036	5.040	5.045	5.049	5.054	5.058	
<b>2.25</b>	5.062	5.067	5.072	5.076	5.081	5.085	5.090	5.094	5.099	5.103	5
6	5.108	5.112	5.117	5.121	5.126	5.130	5.135	5.139	5.144	5.148	
7	5.153	5.157	5.162	5.167	5.171	5.176	5.180	5.185	5.189	5.194	
8	5.198	5.203	5.208	5.212	5.217	5.221	5.226	5.230	5.235	5.240	
9	5.244	5.249	5.253	5.258	5.262	5.267	5.272	5.276	5.281	5.285	
<b>2.30</b>	5.290	5.295	5.299	5.304	5.308	5.313	5.318	5.322	5.327	5.331	
1	5.336	5.341	5.345	5.350	5.355	5.359	5.364	5.368	5.373	5.378	
2	5.382	5.387	5.392	5.396	5.401	5.406	5.410	5.415	5.420	5.424	
3	5.429	5.434	5.438	5.443	5.448	5.452	5.457	5.462	5.466	5.471	
4	5.476	5.480	5.485	5.490	5.494	5.499	5.504	5.508	5.513	5.518	
<b>2.35</b>	5.522	5.527	5.532	5.537	5.541	5.546	5.551	5.555	5.560	5.565	
6	5.570	5.574	5.579	5.584	5.588	5.593	5.598	5.603	5.607	5.612	
7	5.617	5.622	5.626	5.631	5.636	5.641	5.645	5.650	5.655	5.660	
8	5.664	5.669	5.674	5.679	5.683	5.688	5.693	5.698	5.703	5.707	
9	5.712	5.717	5.722	5.726	5.731	5.736	5.741	5.746	5.750	5.755	
<b>2.40</b>	5.760	5.765	5.770	5.774	5.779	5.784	5.789	5.794	5.798	5.803	
1	5.808	5.813	5.818	5.823	5.827	5.832	5.837	5.842	5.847	5.852	
2	5.856	5.861	5.866	5.871	5.876	5.881	5.885	5.890	5.895	5.900	
3	5.905	5.910	5.915	5.919	5.924	5.929	5.934	5.939	5.944	5.949	
4	5.954	5.958	5.963	5.968	5.973	5.978	5.983	5.988	5.993	5.998	
<b>2.45</b>	6.002	6.007	6.012	6.017	6.022	6.027	6.032	6.037	6.042	6.047	
6	6.052	6.057	6.061	6.066	6.071	6.076	6.081	6.086	6.091	6.096	
7	6.101	6.106	6.111	6.116	6.121	6.126	6.131	6.136	6.140	6.145	
8	6.150	6.155	6.160	6.165	6.170	6.175	6.180	6.185	6.190	6.195	
9	6.200	6.205	6.210	6.215	6.220	6.225	6.230	6.235	6.240	6.245	

Moving the decimal point ONE place in *N* requires moving it TWO places in body of table (see p. 1-8).