POWDER TECHNOLOGY SERIES

FRANSFE FLUIDIZE

O. Molerus and K.-E. Wirth



Heat Transfer in Fluidized Beds

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Heat Transfer in Fluidized Beds

Powder Technology Series

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Japan

Many materials exist in the form of a disperse system, for example powders, pastes, slurries, emulsions and aerosols. The study of such systems necessarily arises in many technologies but may alternatively be regarded as a separate subject which is concerned with the manufacture, characterization and manipulation of such systems. Chapman & Hall were one of the first publishers to recognize the basic importance of the subject, going on to instigate this series of books. The series does not aspire to define and confine the subject without duplication, but rather to provide a good home for any book which has a contribution to make to the record of both the theory and the application of the subject. We hope that all engineers and scientists who concern themselves with disperse systems will use these books and that those who become expert will contribute further to the series.

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Preface

A prestigious form of research grant in Germany is the Sonderforschungsbereich, which provides continuous funding over a period of up to 15 years, but only as long as the work is yielding worthwhile results. We acknowledge financial support of our work at Erlangen by the Deutsche Forschungsgemeinschaft (DFG), Sonderforschungsbereich 222. Thanks to this support, the experimental results from six Dr.-Ing. dissertations have provided the basis for our book:

- Schweinzer, J. (1987) Heat transfer in bubbling fluidized beds at $Ar \ge 10^8$
- Seiter, M. (1990) Particle motion and solids concentration in circulating fluidized beds
- Mattmann, W. (1991) Heat transfer in pressurized circulating fluidized beds
- Burschka, A. (1993) Pulsed light method
- Dietz, S. (1994) Heat transfer in bubbling fluidized beds
- Gruber, U. (1995) Heat transfer in lean phase systems

This book is the result of the enthusiastic and trustful cooperation of its authors. Nevertheless, we are separate individuals. Chapters 1 to 12 and 19 are by O. Molerus; Chapters 13 to 18 are by K.-E. Wirth.

This book came into existence after many rewrites, patiently endured by Mrs Winter, who typed all versions of the manuscript, and by Mrs Scheffler-Kohler, who drew all the figures.

Bob Farmer and David Penfold helped us bridge the language gap to produce a readable book.

We are grateful to Professor Brian Scarlett of Delft University, who on behalf of Chapman & Hall allowed us to write this book. And we are grateful to Chapman & Hall for its excellent assistance in preparation and publication of our manuscript.

O. Molerus and K.-E. Wirth
Erlangen
July 1997

List of symbols

Latin letters

```
width of a surface element on the heat exchanger, m
A
                   amplitude, m
b
                   mass absorption coefficient, m<sup>2</sup> kg<sup>-1</sup>
R
                   heat capacity, W s kg<sup>-1</sup> K<sup>-1</sup>
                   heat capacity of the continuous phase, W s kg<sup>-1</sup> K<sup>-1</sup>
C_{\rm c}
                   gas specific heat, W s kg<sup>-1</sup> K<sup>-1</sup>
C_g
C_{p}
                   particle material specific heat, W s kg<sup>-1</sup> K<sup>-1</sup>
C
                   constant
d_{\rm p}
                   particle diameter, bubble diameter, m
d_{\rm pc}
                   characteristic particle size of a cold system, m
d_{\rm ph}
                   characteristic particle size of a hot system, m
D
                   diameter of optical fibre, diameter of the circulating fluidized bed
                   (Chapter 15), m
D_{p}
                   pipe diameter, m
D_{\mathsf{h}}
                   hydraulic diameter of the fluidized bed, m
F
                   cross-sectional area of the fluidized bed, m<sup>2</sup>
                   particle exchange frequency, s<sup>-1</sup>
f(t)
                   residence time distribution density, s<sup>-1</sup>
f_{\rm I}
                   particle exchange frequency at large heat exchanger surfaces, s<sup>-1</sup>
F(t)
                   cumulative residence time distribution
F_{\rm H}
                   adhesion force, N
F_{\text{particle}}
                   surface area of a particle, m<sup>2</sup>
                   surface area of the heat exchanger, m<sup>2</sup>
F_{\text{hex}}
                   gravitational acceleration, m s
g(u-u_{\rm mf})
                   normalized gas convective heat transfer function, defined by (7.1)
G_1, G_2
                   constant
h, h_{\text{max}}
                   heat transfer coefficient, maximum value, W m<sup>-2</sup> K<sup>-1</sup>
h_{i}
                   instantaneous heat transfer coefficient, W m<sup>-2</sup> K<sup>-1</sup>
h_{\rm gc}
                   gas convective component of heat transfer coefficient. W m<sup>-2</sup> K<sup>-1</sup>
```

	it a second of boot transfer coefficient
$h_{ m pc}$	particle convective component of heat transfer coefficient, $W \ m^{-2} \ K^{-1}$
$h_{ m L}$	heat transfer coefficient at large heat exchanger surface,
	$W m^{-2} K^{-1}$
h_1	surface-averaged heat transfer coefficient of a particle, W m ⁻² K ⁻¹
H	height, m
H_{CFB}	total height of the circulating fluidized bed (CFB), m
h _{cond particle}	heat transfer coefficient for one particle caused by heat conduction
•	in the gas, $W m^{-2} K^{-1}$
h_{cond}	heat transfer coefficient caused by heat conduction in the gas,
	$W m^{-2} K^{-1}$
$h_{ m conv}$	heat transfer coefficient caused by heat convection in the gas,
	$W m^{-2} K^{-1}$
$H_{ m mf}$	height of the solids at minimum fluidization, m
h_1	height of the lower steady-state section, m
$h_{ m ts}$	heat transfer coefficient in CFBs when two steady-state sections occur, W m ⁻² K ⁻¹
h_{os}	heat transfer coefficient in CFBs when one steady-state section
770S	occurs, W m ⁻² K ⁻¹
h_{rad}	heat transfer coefficient in CFBs caused by radiation, W m ⁻² K ⁻¹
$h_{\rm rad\ effective}$	heat transfer coefficient in CFBs effectively caused by radiation,
rad effective	$W m^{-2} K^{-1}$
I	dimensionless heat transfer coefficient, defined by (7.7)
I_0	intensity of unattenuated radiation, s ⁻¹
I	intensity of attenuated radiation (Chapter 13), s ⁻¹
J	dimensionless heat transfer coefficient, defined by (7.8)
k	thermal conductivity, W m ⁻¹ K ⁻¹
k_{c}	thermal conductivity of the continuous phase, W m ⁻¹ K ⁻¹
$k_{\rm e}$	effective thermal conductivity in a particle packet, W m ⁻¹ K ⁻¹
$k_{ m eff}$	effective thermal conductivity, defined by (7.9), W m ⁻¹ K ⁻¹
$k_{ m g}$	gas thermal conductivity, W m ⁻¹ K ⁻¹
$k_{ m p}$	particle material thermal conductivity, W m ⁻¹ K ⁻¹
K	lift force, N
l	1
•	[II] ^{2/3}
l_1	length, m $\equiv \left[\frac{\mu}{\sqrt{g}(\rho_{\rm p} - \rho_{\rm g})}\right]^{2/3}, \text{ laminar flow length scale, m}$
ΔL	length of a pipe element, m
$l_{\rm t}$	length of a pipe element, m $\equiv \left[\frac{\mu}{\sqrt{g(\rho_{p}-\rho_{g})\rho_{g}}}\right]^{2/3}, \text{ turbulent flow length scale, m}$
l_0	mean free path of gas molecules, m
	digital luminosity, initial value
L, L_0	length of the γ -ray beam in the circulating fluidized bed (Chapter
L	12)

13), m

```
L_{\rm p}
                   packing or pipe length, m
                   minimum length of heat exchanger, m
 M
 M_{\rm p}
                   mass of the solids in the CFB, kg
                   mass of the continuous phase, kg
 M_{\rm c}
 \dot{M}_{\rm p}
                   solids mass flow rate, kg s<sup>-1</sup>
 \dot{M}_{\rm g}
                   gas mass flow rate, kg s
                   number of particles, initial value (Chapter 2)
 n, n_{p0}
                   number of particle rows (Chapter 3)
 n
 P
                   power input, W
                  pressure, N m<sup>-2</sup>
p
                  normalized particle convective heat transfer, defined by (7.11)
p(u-u_{\rm mf})
                  pressure drop, N m<sup>-2</sup>
 \Delta p
 \Delta P_{\rm CFB}
                  total pressure drop in the riser of a CFB. N m<sup>-2</sup>
P_1, P_2
                  constants
P_1^*, P_2^*
                  constants
                  radiative heat flux from object 1 to object 2, W m<sup>-2</sup>
q_{12}
Ò
                  energy transfer per unit time, W
r
                  integration variable, m
                  characteristic particle dimension, m
r_0
R
                  aerodynamic resistance force, N
R
                  radius (Chapter 3), m
                  characteristic length of surface asperities, m
2
                  minimum effective surface asperities according to (3.25), m
S_{\min}
                  particle surface area, inner pipe surface area, m<sup>2</sup>
S_{\rm p}
t
                  time, s
\Delta t
                  time interval, s
T_{\rm m}
                  mean temperature, K
T_{\rm p}
                  particle temperature, K
T_{\rm susp}
                  suspension temperature, K
T_{\rm w}
                  wall temperature, K
\Delta T
                  temperature difference, K
\Delta T_{\log}
                  logarithmic temperature difference, K, defined by (3.6)
T_0
                  entrance temperature of the gas, K
                 exit temperature of the gas, K
T_1
11
                 superficial gas velocity, m s<sup>-1</sup>
                 superficial gas velocity at minimum fluidization condition, m s<sup>-1</sup>
u_{\rm mf}
                 shear field velocity, m s<sup>-1</sup>
u(y)
                 lateral particle velocity, m s<sup>-1</sup>
u_1
                 vertical particle velocity, m s<sup>-1</sup>
u_{\nu}
                 x-component of the velocity vector in Cartesian coordinates, m s<sup>-1</sup>
u_x
                 mean pipe flow velocity, superficial velocity of the continuous
U
                 phase, m s<sup>-1</sup>
                 maximum particle transport velocity, m s<sup>-1</sup>
v_{\text{max}}
                 velocity of the gas in the dilute phase, m s<sup>-1</sup>
UG
```

velocity of a particle, m s⁻¹ v_{p} velocity of the gas, m s⁻¹ v_{g} relative velocity, m s⁻¹ $v_{\rm rel}$

particle velocity in shear field, m s⁻¹

fluid volume, m³ V_{a}

volume of a fluidized bed, m³ $V_{\rm bed}$

volumetric flow rate of the continuous phase, m³ s⁻¹

velocity of the strands, m s⁻¹ w single-particle fall velocity, m s⁻¹ W_f

W probability

Cartesian coordinates, m x, y, z

X coordinate, m ΛX length, m coordinate, m yY coordinate, m

Greek letters

constant α β constant

accommodation coefficient Y

characteristic dimension for the space around the particles at δ

particulate fluidization, m

laminar boundary layer thickness, m δ_1

boundary layer length scale in the transitional regime, m δ_{tr} boundary layer length scale in the turbulent flow regime, m δ_{turb}

void fraction 3

minimum fluidization void fraction ϵ_{mf} emissivities of solid bodies 1, 2 81.2 emissivity of the particles ϵ_{n} emissivity of the wall $\varepsilon_{\rm w}$ emissivity of the system Erad

mass-related power input, W kg⁻¹ 8*

local void fraction ϵ_1

void fraction in the vicinity of the CFB wall ϵ_{wall}

A

μ

D. wall temperature, °C ϑ_{susp} suspension temperature, °C

particle temperature, °C ϑ_p J temperature (Chapter 16), °C viscosity, kg m⁻¹ s⁻¹

gas viscosity in a cold system, gas viscosity of the continuous phase μ_{c}

in Chapters 17 and 18, kg m⁻¹ s⁻¹

gas viscosity in a hot system, kg m⁻¹ s⁻¹ μ_h

kinematic viscosity, kinematic viscosity of the continuous phase, ν density, kg m⁻³ ρ bulk density, kg m⁻³ ρ_b density of the continuous phase, kg m⁻³ $\rho_{\rm c}$ gas density, kg m⁻³ ρ_g gas density in a cold system, kg m⁻³ Pgc gas density in a hot system, kg m⁻³ ρ_{gh} particle density, kg m⁻³ $\rho_{\rm p}$ Stefan-Boltzmann constant = 5.67×10^{-8} , W m⁻² K⁻⁴ σ τ mean residence time, s angle Φ Φ sphericity, dimensionless pressure drop in Chapters 15 and 16, defined by (15.2) Φ_{D} pressure drop shape factor cyclic frequency, s⁻¹ ω

Dimensionless groups

$$Ar \equiv \frac{d_p^3 g(\rho_p - \rho_g) \rho_g}{\mu^2}$$

$$Archimedes number$$

$$C_D \equiv \frac{R}{[(\pi d_p^2)/4](\rho_g/2)u^2}$$

$$Co \equiv \frac{k_g Cst}{\rho_p c_p d_p^3}$$

$$Bi \equiv \frac{h d_p}{k_p}$$

$$Dr \equiv \frac{\Delta P}{\Delta L} \frac{d_p^3}{\rho_g v^2} \frac{1}{1 - \varepsilon}$$

$$Eu \equiv \frac{4}{3} \frac{(\rho_p - \rho_g) d_p g}{\rho_g u^2} \varepsilon^2$$

$$Fr \equiv \frac{\upsilon}{d_p g}$$

$$Fr_p \equiv \frac{\upsilon}{\sqrt{\frac{\rho_p - \rho_g}{\rho_g} d_p g}}$$

$$Fr_{pwf} \equiv \frac{\upsilon}{\sqrt{\frac{\rho_p - \rho_g}{\rho_g} d_p g}}$$

$$particle Froude number built with the terminal free-fall velocity of a single particle$$

$Fr_{p \text{ umf}} \equiv \frac{u_{\text{mf}}}{\sqrt{\frac{\rho_{p} - \rho_{g}}{\rho_{g}} d_{p} g}}$	particle Froude number built with the minimum fluidization velocity
$Nu, Nu_{max} \equiv \frac{hd_{p}}{k_{g}}$	Nusselt number, maximum value
$\mathrm{Nu_{cond\ particle}} \equiv rac{h_{\mathrm{cond\ particle}}d_{\mathrm{p}}}{k_{\mathrm{g}}}$	Nusselt number for a particle in the Stokes regime
$Nu_{cond} \equiv \frac{h_{cond} d_{p}}{k_{g}}$	Nusselt number caused by heat conduction in the gas
$\mathrm{Nu_{conv}} \equiv rac{h_{\mathrm{conv}} d_{\mathrm{p}}}{k_{\mathrm{g}}}$	Nusselt number caused by heat convection in the gas
$\mathrm{Nu_{ts}} \equiv rac{h_{\mathrm{ts}}d_{\mathrm{p}}}{k_{\mathrm{g}}}$	Nusselt number in CFBs when two steady-state sections occur
$\mathrm{Nu_{os}} \equiv \frac{h_{\mathrm{os}} d_{\mathrm{p}}}{k_{\mathrm{g}}}$	Nusselt number in CFBs when one steady-state section occurs
$\mathrm{Nu_{rad}} \equiv rac{h_{ m rad}d_{ m p}}{k_{ m g}}$	Nusselt number caused by radiation
$\mathrm{Nu_{rad\ effective}} \equiv rac{h_{\mathrm{rad\ effective}}d_{\mathrm{p}}}{k_{\mathrm{g}}}$	Nusselt number effectively caused by radiation
$\mathrm{Nu_c} \equiv \frac{hd_\mathrm{p}}{k_\mathrm{c}}$	Nusselt number built with the thermal conductivity of the continuous phase
$\mathrm{Nu_p} \equiv rac{hD_\mathrm{p}}{k_\mathrm{g}}$	pipe flow Nusselt number
$Pe \equiv \frac{\rho_{\rm g} c_{\rm g} d_{\rm p} u}{k_{\rm g}}$	Peclet number
$\mathrm{Pe}_{\mathrm{fl}} \equiv \frac{\rho_{\mathrm{g}} c_{\mathrm{g}} d_{\mathrm{p}} \sqrt{[(\rho_{\mathrm{p}} - \rho_{\mathrm{g}})/\rho_{\mathrm{g}}] d_{\mathrm{p}} g}}{k_{\mathrm{g}}}$	fluidization Peclet number
$\mathrm{Pe}_{\mathrm{p}} \equiv \frac{p_{\mathrm{g}} c_{\mathrm{g}} D_{\mathrm{p}} v}{k_{\mathrm{g}}}$	pipe flow Peclet number
$\Pr \equiv \frac{c_{\rm g} \mu}{k_{\rm g}}$	Prandtl number
$\mathrm{Pr_c} \equiv \frac{c_\mathrm{c}\mu_\mathrm{c}}{k_\mathrm{c}}$	Prandtl number of the continuous phase

$$\frac{r_0}{\delta} \equiv \left[\frac{\zeta}{\sqrt[3]{1-\epsilon}} \ - \ 1 \right]^{-1}$$

Re

$$Re_{\varepsilon} \equiv \frac{vd}{\varepsilon v}$$

$$\mathrm{Re}_{\mathrm{rel}} \equiv \frac{v_{\mathrm{rel}} d_{\mathrm{p}}}{\mathrm{v}}$$

$$Re_{umf} \equiv \frac{u_{mf}d_{p}}{v}$$

$$Re_w \equiv \frac{wd_p}{v}$$

$$Re_{\rm wf} \equiv \frac{w_{\rm f} d_{\rm p}}{v}$$

$$Sta = \frac{hd_{p}}{\rho_{g}c_{g}d_{p}u}$$

Sta₁

 Sta_n

$$Sta_{w} \equiv \frac{h_{conv}}{\rho_{g} c_{g} w}$$

$$\pi_{1} \equiv \frac{d_{p}^{3} g (\rho_{p} - \rho_{g})^{2}}{u^{2}}$$

$$\pi_2 \equiv rac{
ho_{
m p}}{
ho_{
m g}}$$
 . $\pi_3 \equiv rac{c_{
m g} \mu}{k_{
m g}} \equiv {
m Pr}$

$$\pi_4 \equiv \frac{c_{\rm p} \mu}{k_{\rm g}}$$

$$\pi_5 \equiv \frac{k_p}{k_c}$$

length ratio, $\zeta = 0.9$ for a fluidized bed, $\zeta = 0.95$ for a fixed bed Reynolds number, different

definitions

Reynolds number built with the interstitial fluid velocity

Reynolds number built with the relative velocity

Reynolds number built with the minimum fluidization velocity

Reynolds number built with the velocity of the downward-falling wall strands

Reynolds number built with the terminal free-fall velocity of a single particle

Stanton number

Stanton number for the first particle row mean Stanton number for *n* rows of particles

Stanton number for the wall strands

Prandtl number

$$\pi_6 \equiv \frac{hd_p}{k_g} \equiv \text{Nu}$$

$$\Omega^{1/3} \equiv \left[\frac{\rho_g^2}{\mu g(\rho_p - \rho_g)}\right]^{1/3} u$$

Nusselt number

dimensionless gas velocity

Contents

Prefa	reface	
List	of symbols	ix x
1	Introduction	1
1.1	Modelling heat transfer in bubbling fluidized beds	1
1.2	Heat transfer in circulating fluidized beds	1
1.3	Related systems	2
1.4	Short outline of the contents	2
1.5	Limits of the book	4
2	Particle migration at solid surfaces and heat transfer in bubbling	
	fluidized beds	5
2.1	Introduction	5
2.2	The pulsed light method	5
2.3	Experimental rig	6
2.4	Analysis of the visualization data	7
2.5	Particle exchange frequency and the heat transfer coefficient	10
2.6	Mean residence times at solid surfaces	12
2.7	Influence of probe size on measured heat transfer coefficients	15
3	Heat transfer in particle beds	18
3.1	Introduction	18
3.2	Particle-to-gas heat transfer in particle beds at Pe ≤ 10	18
3.3	Heat transfer where inertial effects are insignificant	19
3.4	Equivalent pipe diameter	20
3.5	Heat transfer from a single particle inside a particle array	21
3.6	Fluid heating by percolation through a particle array	21
3.7	A single particle in the emulsion phase: experimental comparison	22
3.8	Heat transfer to a percolating gas from a hot array of particles:	
	experimental comparison	23
3.9	Heat transfer in particle beds with a stagnant interstitial gas	25
3.10	Contact resistance	26

vi Contents

3.11	Effective thermal conductivity of particle beds	28
3.12	Long time asymptotic solution for heating up a moving bed	29
3.13	Conclusions on heat transfer in bubbling fluidized beds	33
4	Heat transfer mechanisms in bubbling fluidized beds	35
4.1	General features of heat transfer in bubbling fluidized beds	35
4.2	Non-dimensional groups from particle properties and fluid properties	37
4.3	Maximum heat transfer coefficient in the laminar flow regime $(Ar \le 10^2)$	38
4.4	Maximum heat transfer coefficient in bubbling fluidized beds for	
	Archimedes numbers $10^5 \le Ar \le 10^8$	44
4.5	Conclusions	45
5	Prediction of minimum fluidization velocity	48
6	Physical properties of the media	51
6.1	Relevant physical properties	51
6.2	Gas properties	51
6.3	Particle properties	53
7	Prediction of heat transfer in bubbling fluidized beds at $Ar \leq 10^8$	55
7.1	Introduction	55
7.2	Strategy to derive the new correlation	55
7.3	Dependence of gas convective heat transfer on excess gas velocity	56
7.4	Significance of the assumed particle convective heat transfer mechanism	57
7.5	Dependence of particle convective heat transfer on excess gas velocity	59
7.6	Dependence of heat transfer on excess gas velocity in the intermediate range	62
7.7	Comparison with experiments	63
1.1	Comparison with experiments	65
8	Significant features of equation (7.17)	69
8.1	Introduction	69
8.2 8.3	Completeness of the solution	69
8.4	Inaccurate prediction of the minimum fluidization velocity	70
8.5	Influence of particle size Influence of particle shape	71
8.6	Influence of gas pressure	71
0.0	influence of gas pressure	72
9	Heat transfer at $Ar > 10^8$	75
9.1	General features and proposed correlation	75
9.2	Comparison with heat transfer measurements in a pressurized fluidized bed with a built-in bundle of horizontal tubes	76
9.3	Introducing the turbulent flow length scale	77
	<u> </u>	

10	Physical background to convective heat transfer	78
10.1	Introduction	78
10.2	Maximum heat transfer coefficient as a system property	78
10.3	Physical background to particle convective heat transfer	79
10.4	Physical background to the turbulent flow length scale $l_{\rm t}$	82
11	Heat transfer at elevated temperatures	84
11.1	Convective heat transfer	84
11.2	Simulated direct measurements of the radiative component of heat transfer	87
11.3	Radiative heat transfer	88
12	Historical remarks	90
13	Fluid dynamics of circulating fluidized beds	96
13.1	Operating region of circulating fluidized beds	96
13.2	Overall flow condition in CFBs	97
13.3	State and pressure drop diagram of the gas/solid flow in CFBs	97
13.4	Flow conditions immediately next to the wall of a heat exchanger	105
14	Experimentally determined wall-to-suspension heat transfer	
	coefficients in circulating fluidized beds	111
14.1	Experimental test rig	111
14.2	Influence of heat exchanger length on the heat transfer coefficient	113
14.3	Experimentally determined heat transfer coefficients when two	
	steady-state sections occur in the CFB	114
14.4	Experimentally determined heat transfer coefficients when one	
	steady-state section occurs in the CFB	119
15	Prediction of the heat transfer in circulating fluidized beds	
	without considering the influence of radiation	123
15.1	Heat transfer mechanisms	123
15.2	Heat transfer with two steady-state sections	124
	15.2.1 Flow condition of the downward-moving strands in the wall region	124
	15.2.2 Heat transfer for low Archimedes number in the gas/solid system	127
	15.2.3 Heat transfer for high Archimedes numbers in the gas/solid system	130
	15.2.4 Correlation for heat transfer over the whole range of	
150	Archimedes numbers	131
15.3	Heat transfer with one steady-state section	135

Contents vii