EDGE DETECTION AND GEOMETRIC
METHODS IN COMPUTER VISION
TOPOLOGY,
PERCEPTION, ARTIFICIAL
INTELLIGENCE, LOW-LEVEL)

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EDGE DETECTION AND GEOMETRIC METHODS IN COMPUTER VISION

University of California, Berkeley

Ph.D. 1984

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DISSERTATION

Submitted in partial satisfaction of the requirements for the degree of $$\operatorname{\mathtt{DOCTOR}}$ OF PHILOSOPHY

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GRADUATE DIVISION

OF THE

UNIVERSITY OF CALIFORNIA, BERKELEY

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DOCTORAL DEGREE CONFERRED DECEMBER 18, 1984 Edge Detection and Geometric Methods in Computer Vision

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A. Peter Blicher

Edge Detection and Geometric Methods in Computer Vision

A. Peter Blicher

Abstract

Basic problems of vision are studied from the viewpoint of modern differential topology and geometry; primarily: edge detection, stereo matching, picture representation at multiple scales, and motion. Some mathematical background is provided for the non-expert.

A comprehensive review of edge detection is presented, including analyses from a mathematical perspective as well as evaluations of practical performance and promise.

Some new edge detection techniques are introduced, including a nonlinear operator based on a symmetry principle, a variational approach to global edge finding, and a least-squares localization method. A theorem is proved which shows that localizing edge position and orientation requires at least 2 orientation dependent families of convolution operators.

A unifying mathematical structure is presented for vision, notably stereo, motion stereo, optic flow (apparent flow of visual space under motion), and matching. The general matching problem is analyzed, and it is proved that generically, general matching is highly degenerate for monochrome pictures, but has a unique solution for 2 or more color dimensions. The result is extended to pictures with unknown bias and gain. Smale diagrams and level set topology are introduced as invariants useful for matching, reducing the problem to graph or tree matching. The level set topology tree is also proposed as a method of multi-scale description of the picture, and shown to be an invariant generalization of the "scale space" technique.

The motion problem is analyzed using Lie group methods, and a theorem is proved

establishing that generically 6 simultaneous values of time derivative of the monochrome picture function are necessary and sufficient to uniquely specify the 3-dimensional rigid motion of a generic given object. For 2 or more color dimensions, this is reduced to values at 3 points in the picture.

Thomas C. Binford

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Through the period of this work, my parents have been my greatest asset, not only by their love and sacrifice, but in many, many ways.

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For leading me to this research, I must also thank the professors of engineering who taught me that the key to engineering is understanding physics; the professors of physics who taught me that the key to physics is understanding mathematics; and the professors of mathematics who taught me that mathematics has nothing to do with the material world.

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Preface

I wrote this work for an audience of both vision workers and mathematicians. There are many people who could be counted in both groups, but the full intended audience has a wide spectrum of backgrounds. Among vision workers, I include students of biological vision, but it is artificial vision that I am directly addressing. It is widely appreciated that there are many common problems, but I haven't written about any specifically biological problems, such as explaining the function of some cell population. My hope is not only to communicate research results, but to convince readers in each of these fields that there is something of interest to them in the other. Many people have a bad taste from previous experience with touters of fancy mathematics in these concrete situations, with elixirs which turned out to be oversold or plain irrelevant. Mathematics is not magic; using it doesn't melt all impediments into triviality. It merely provides a structure for understanding, and an apparatus for resolving questions. If the questions are the right grist for the mill. Attracting these fields to each other isn't necessarily easy.

Also, it poses a problem in writing; since I have tried to keep the material accessible to the novice, some of it must necessarily be old hat to the expert, so I apologize to the expert whom I have subjected to the obvious. I have tried to make this work reasonably self-contained, including various standard definitions and results from differential topology and geometry. When these are not in the main line of thought, they have been relegated to fine print, so they can be easily skipped by those who already have the necessary background. Sometimes, standard terms are used before they are defined, and sometimes they are defined twice, partially from a lack of organization, but primarily to locate the mathematical digressions where they are most important, and avoid bogging things down where they are not. I haven't tried to be exhaustive in this, or I would have been obliged to include a complete introduction to differential topology and geometry,

something which has already been accomplished with great skill by others. The chapter Geometric Methods in Vision makes the heaviest use of abstract mathematics; therefore I have put most mathematical background material into the fine print of that chapter. Since I have assumed some of that background material in earlier chapters, the reader may find it useful to glance through it to clarify the unfamiliar, such as the implicit function theorem, or functional notation.

The 3 major chapters (A Survey of Edge Detection, Contributions to Edge Detection, and Geometric Methods in Vision) are largely independent, and can be read in any order, or in isolation. The survey has many discussions which go beyond summarizing, and should be of interest to readers who are already familiar with the literature, as well as to newcomers. The contributions chapter is probably of most interest to specialists, while the geometry chapter is likely to appeal to the more mathematically inclined.

Stanford, California

October, 1984

	Ac	knowle	ede	gr	n	e	n	t	3 .	•			•						•		•	•		•	•													•													
	Pre	eface .	•			•											,			٠	•												•											٠							ii
1	Int	roduc	ti	io	D	1																																													
2	A	Surve	у	0	f		E	d	g	e	D	e	te	ec	:t	ic	or	2 .			•				•																		•								•
	2.1	Intro	od	lu	c	t	ic	on	ı				•	•												•																									
		2.1.1		٧	N	'n	ny	, ,	ec	g	c	de	eti	ec	:t	io	n	?		•	•					•							•																		(
		2.1.2		L	7 0)(a	ı	C	de	çe	d	ct	le	c	ti	or	n							•								•c 15								•									1	:
						S	p	a	ti	al	d	iſ	ſс	rc	en	ıti	ia	ti	o	n	:	31	10	ł	g	r	ac	li	er	nt		s	Li	m	a	tic	on													1	4
	•				4	۸	p	p	г	ЭX	in	12	li	io	n	a	ın	d	1	c	p	r	C:	sc	n	L	ai	ic	or	1	o	i	ır	ıa	g	0	ſu	n	ct	ic) n	1	•							1	8
		2.1.3		G																																														1	
		2.1.4	1	R	c	g	ii	or	1	gr	01	wi	nį	g																												•								2	0
	2.2	Gene																																																2	
																																																		2	
																																																		2	
																																																		2	3
																																																		2	
					I)																																												2	
																																																		25	
																																																		25	
	2.3	Local	N	Mo	ct																																													28	
		2.3.1																						•	•	•				•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	٠	•	•	•	26	

Roberts 1963	28
Local edge detector	29
Edge detection process	29:
Linking	30
Curve representation and segmentation	30.
Evaluation of line finding	31
Hueckel 1969, Hueckel 1971, Hueckel 1973	31
Evaluation	33
Nevatia 1977	34
Altes 1975	35
Evaluation	37
O'Gorman 1978	38
Turner 1974	40
Abdou 1978	41
Evaluation	44
Beaudet 1978	44
Evaluation	46
Ilsu, Mundy, Beaudet 1978	47
Experimental results	47
Evaluation	18
Dreschler and Nagel 1981a, Dreschler and Nagel 1981b	48
Experimental results	50
Evaluation	50
Haralick 1980	51
Evaluation	53
Haralick 1981, Haralick 1982, Haralick 1984	53
Evaluation	54
Ontimal Filters	55

		Shanmugam, Dickey, Green 1979	55
		The optimality of Gaussians	57
		Evaluation	58
		Marr and Hildreth 1979	59
		Evaluation	62
		Canny 1983	63
		The 1-dimensional problem	64
		Sensitivity criterion	64
		Localization criterion	65
		Optimizing sensitivity and localization	66
		Multiple response criterion and optimizing for all criteria	67
		The 2-dimensional problem	69
		Linking	74
•		Empirical results	75
		Evaluation	76
		A nonlinear approach	78
2.4	Globa	l Methods	81
	2.4.1	Accumulator arrays	81
		llough 1962	81
		Basic idea	81
		Evaluation	82
		Ballard and Sklansky 1976	83
		Summary of processing steps	83
		Evaluation	84
	2.4.2	Region growing	85
		Brice and Fennema 1970, Fennema and Brice 1970	85
		Phagocyte heuristic	85
		Weakness heuristic	85

		Evaluation	٠		٠.	٠		•	٠	٠.	85	,
		Kirsch 1971	•			•	•,•		•	٠.	86	3
		Evaluation	•			•		•	٠		87	7
		Somerville and Mundy 1976	•								. 88	3
		Experimental results									90)
	2.4.3	Histogramming									. 90)
		Ohlander 1975	٠						•		90)
		Evaluation									. 9	1
		Shafer 1980							٠		. 9	1
	2.4.4	Optimal linking			• 10		•				. 9:	3
		Montanari 1970, Montanari 1971					•				. 9:	3
		Evaluation									. 9	4
		Martelli 1972, Martelli 1973	•				•		•		. 9	5
		Evaluation							•	•	. 9	6
		Rosenfeld, Hummel, Zucker 1975, Zucker, Hum	ım	el,	R	osc	nſ	cl	d .	197	77 9	6
		Evaluation									. 9	8
Cor	tribut	ions to Edge Detection					•			٠	. 10	0
3.1	Introd	luction									. 10	0
3.2	Edge	localization in both θ and x								•	. 10	2
1	3.2.1	Introduction								•	. 10	2
	3.2.2	Some Mathematics of Parametric Convolutions .			•		•			•	. 10	2
	3.2.3	The Limitations of Zero-crossings	•		•		•			•	. 10	7
		Definition of zero crossings	•				•			•	. 10	7
	÷	Remarks on the definition of zero crossings	•				•			٠	. 10	7
		Case 1: s of class C^r , $r \geq 1 \ldots \ldots$	•							•	. 10	8
		Case 2: s of class C^0					•			٠	. 10	ç
3.3	Nonli	near Local Edge Detection	•				•			٠	. 11	2
	3.3.1	The even-odd operator of [Binford 1981]						•			. 11	4
	3.1	2.4.4 Contribut 3.1 Introd 3.2 Edge 3.2.1 3.2.2 3.2.3	Evaluation	Evaluation	Evaluation Somerville and Mundy 1978 Experimental results 2.4.3 Histogramming Ohlander 1975 Evaluation Shafer 1980 2.4.4 Optimal linking Montanari 1970, Montanari 1971 Evaluation Martelli 1972, Martelli 1973 Evaluation Rosenfeld, Hummel, Zucker 1975, Zucker, Hummel, Evaluation Contributions to Edge Detection 3.1 Introduction 3.2 Edge localization in both θ and x 3.2.1 Introduction 3.2.2 Some Mathematics of Parametric Convolutions 3.2.3 The Limitations of Zero-crossings Definition of zero crossings Remarks on the definition of zero crossings Case 1: s of class C ^r , τ ≥ 1 Case 2: s of class C ⁰ 3.3 Nonlinear Local Edge Detection	Evaluation	Evaluation Somerville and Mundy 1976 Experimental results 2.4.3 Histogramming Ohlander 1975 Evaluation Shafer 1980 2.4.4 Optimal linking Montanari 1970, Montanari 1971 Evaluation Martelli 1972, Martelli 1973 Evaluation Rosenfeld, Hummel, Zucker 1975, Zucker, Hummel, Rose Evaluation Contributions to Edge Detection 3.1 Introduction 3.2 Edge localization in both ℓ and x 3.2.1 Introduction 3.2.2 Some Mathematics of Parametric Convolutions 3.2.3 The Limitations of Zero-crossings Definition of zero crossings Remarks on the definition of zero crossings Case 1: s of class C ⁷ , τ ≥ 1 Case 2: s of class C ⁰ 3.3 Nonlinear Local Edge Detection	Evaluation Somerville and Mundy 1976 Experimental results 2.4.3 Histogramming Ohlander 1975 Evaluation Shafer 1980 2.4.4 Optimal linking Montanari 1970, Montanari 1971 Evaluation Martelli 1972, Martelli 1973 Evaluation Rosenfeld, Hummel, Zucker 1975, Zucker, Hummel, Rosenfeld, Hummel, Zucker 1975, Zucker, Ilummel, Rosenfeld Detection 3.1 Introduction 3.2 Edge localization in both ∅ and z 3.2.1 Introduction 3.2.2 Some Mathematics of Parametric Convolutions 3.2.3 The Limitations of Zero-crossings Definition of zero crossings Remarks on the definition of zero crossings Case 1: s of class C ^r , r ≥ 1 Case 2: s of class C ⁰ 3.3 Nonlinear Local Edge Detection	Evaluation Somerville and Mundy 1976 Experimental results 2.4.3 Histogramming Ohlander 1975 Evaluation Shafer 1980 2.4.4 Optimal linking Montanari 1970, Montanari 1971 Evaluation Martelli 1972, Martelli 1973 Evaluation Rosenfeld, Hummel, Zucker 1975, Zucker, Hummel, Rosenfeld Evaluation Contributions to Edge Detection 3.1 Introduction 3.2 Edge localization in both θ and z 3.2.1 Introduction 3.2.2 Some Mathematics of Parametric Convolutions 3.2.3 The Limitations of Zero-crossings Definition of zero crossings Remarks on the definition of zero crossings Case 1: s of class C ⁷ , τ ≥ 1 Case 2: s of class C ⁰ 3.3 Nonlinear Local Edge Detection	Evaluation Somerville and Mundy 1976 Experimental results 2.4.3 Histogramming Ohlander 1975 Evaluation Shafer 1980 2.4.4 Optimal linking Montanari 1970, Montanari 1971 Evaluation Martelli 1972, Martelli 1973 Evaluation Rosenfeld, Hummel, Zucker 1975, Zucker, Hummel, Rosenfeld Evaluation Contributions to Edge Detection 3.1 Introduction 3.2 Edge localization in both ∅ and z 3.2.1 Introduction 3.2.2 Some Mathematics of Parametric Convolutions 3.2.3 The Limitations of Zero-crossings Definition of zero crossings Remarks on the definition of zero crossings Case 1: s of class C ^r , r ≥ 1 Case 2: s of class C ⁰ 3.3 Nonlinear Local Edge Detection	Kirsch 1971 Evaluation Somerville and Mundy 1978 Experimental results 2.4.3 Histogramming Ohlander 1975 Evaluation Shafer 1980 2.4.4 Optimal linking Montanari 1970, Montanari 1971 Evaluation Martelli 1972, Martelli 1973 Evaluation Rosenfeld, Hummel, Zucker 1975, Zucker, Hummel, Rosenfeld 197 Evaluation Contributions to Edge Detection 3.1 Introduction 3.2 Edge localization in both θ and z 3.2.1 Introduction 3.2.2 Some Mathematics of Parametric Convolutions 3.2.3 The Limitations of Zero-crossings Definition of zero crossings Remarks on the definition of zero crossings Case 1: s of class C ⁰ 3.3 Nonlinear Local Edge Detection	Ohlander 1975 90 Evaluation 91 Shafer 1980 99 2.4.4 Optimal linking 91 Montanari 1970, Montanari 1971 91 Evaluation 99 Martelli 1972, Martelli 1973 91 Evaluation 99 Rosenfeld, Hummel, Zucker 1975, Zucker, Hummel, Rosenfeld 1977 91 Evaluation 99 Contributions to Edge Detection 100 3.1 Introduction 100 3.2 Edge localization in both θ and x 100 3.2.1 Introduction 100 3.2.2 Some Mathematics of Parametric Convolutions 100 3.2.3 The Limitations of Zero-crossings 100 Definition of zero crossings 100 Remarks on the definition of zero crossings 100 Case 1: s of class C^r , $r \ge 1$ 100 Case 2: s of class C^0 10