BASIC BUSINESS MATH



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Library of Congress Cataloging-in-Publication Data Dansby, Robert L.

Basic business math / Robert L. Dansby.
p. cm.
ISBN 0-13-060971-4 1. Business mathematics—Problems, exercises, etc. HF5691.D36 1992 650'.01'513—dc20

I. Title. 91-37186 CIP

DEDICATION

This book is dedicated to my wife, Barbara; and to my son, Champ-for without them, no project would be meaningful.

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Printed in the United States of America $10 \ \ 9 \ \ 8 \ \ 7 \ \ 6 \ \ 5 \ \ 4 \ \ 3 \ \ 2 \ \ 1$

ISBN 0-13-060971-4

Prentice-Hall International (UK) Limited, London Prentice-Hall of Australia Pty. Limited, Sydney

Prentice-Hall Canada Inc., Toronto

Prentice-Hall Hispanoamericana, S.A., Mexico

Prentice-Hall of India Private Limited, New Delhi

Prentice-Hall of Japan, Inc., Tokyo

Simon & Schuster Asia Pte. Ltd., Singapore

Editora Prentice-Hall do Brasil, Ltda., Rio de Janeiro



We live in a fast-moving, rapidly changing world. Skills in basic business mathematics are needed to enable you to begin your career and move up in that career. According to the latest research, the average professional person (bookkeeper, accountant, office worker, manager, etc.) will change positions at least six times during a working career. Many of these changes will take place because individuals will have the educational and occupational skills needed to keep moving up the success ladder.

Basic Business Math is designed to give you the basic math skills needed to enter the work force. It is a very user-friendly text that is aimed at the following objectives:

- 1. Thoroughly reviewing the fundamental operations of arithmetic: whole numbers (addition, subtraction, multiplication, and division), fractions, decimals, and percents
- 2. Developing the student's ability to apply the basic math skills to common business situations
- 3. Developing the student's ability to solve common business problems involving discounts, payroll, interest, markup, and banking
- 4. Developing the student's ability to use shortcuts and work mentally with speed and accuracy

Basic Business Math has been designed to allow you to work on an individual basis or receive instruction in the traditional classroom setting. It teaches by introducing concepts, supported by examples, and immediate feedback. Text matter and problems move from easy to more challenging.

Study your business math concepts well. You will be gaining skills that will benefit you throughout your entire working career as well as in your personal life.

ACKNOWLEDGMENTS

I would like to express my sincere thanks to my many academic colleagues who offered many excellent suggestions and recommen-

dations during the review process of this book and its supplements. This project would not have been possible without their expert assistance. Their time, experience, and expertise are greatly appreciated.

John Bloomquist
Angelo M. Bonoan, Jr.

Lamson Junior College, Phoenix, AZ
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Union City, NJ

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Blake Business School, New York, NY

Special thanks are also in order to my good friends at Prentice Hall, who are responsible for this book. My sincere appreciation goes to Jim Boyd, Editor-in-Chief; Bob Kern, Marketing Manager; and Lisamarie Brassini and Cindy Harford, Supplements Editors.

Accolades are also in order for my Production Editor, Jackie Martin, for her enthusiasm, promptness, and unflagging devotion to the project.

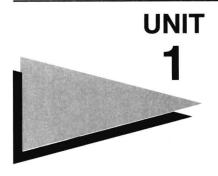
Finally, I would like to recognize the significant contribution of my good friend and professional colleague, Dennis McCollum. Dennis read every page of the manuscript and checked every answer in the book. His professional help and moral support are immensely appreciated.



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Reading and Writing Whole Numbers

A whole number is a number that we use for counting and numbering. We use these ten symbols, called **digits**, to represent whole numbers:

Using these ten digits, we can express any number, large or small. Numbers above the ten basic digits are formed by using combinations of the ten basic digits. The number "10," for example, is formed by using a combination of the first two digits.

THE PLACE VALUE SYSTEM

We can determine the value of each digit in a number by looking at its **place**, or its location, in the number. Thus, each digit in a number has a **place value**. To illustrate place value, let's look at the figure, which shows the number "5" in three different *places*.

	Billions	s	Mi	llion	s	Tho	usar	nds	Hui	ndre	ds
Hundrede	Tens Ones	Hund	Tens	Ones	Hima	Tens	Ones	Hund	Tens	Ones	
										5	Example A
									5	0	Example B
								5	0	0	Example C

The first 5 (Example A) is in the *ones* place; therefore, it has a value of 5 ones. The second 5

(Example B) is in the *tens* place. So, it has a value of 5 tens and no ones, and is written as 50. The third 5 (Example C) is in the *hundreds* place; so, it has a value of 5 hundreds, no tens, and no ones, and is written as 500. Notice that each place has a value that is worth ten times the value of the place to its right.

The place value system lets us write numbers in a very compact way. For example, the number 256 is actually:

			_						_			_
	Bi	llion	s	М	illion	s	Tho	usar	nds	Hu	ndre	ds
H	Tens	Ones	Hing	Tens	Ones	Him	Tens	Ones	Hims	Tens	Ones	
									2	5	6	
20 + 5 +	6 (2 hu 5 ter 6 on	ns)∻	eds) «	-							

The number "256" is read as "two hundred fifty-six" and is the sum of its place values.

READING LARGER NUMBERS

Using the place value system makes it much easier to express and read large numbers. For example, let's look at the figure, which shows the number 1,216,566 with its place values labeled.

	Bi	llion	s	Mi	llion	s	Tho	usar	nds	Hui	ndre	ds
/	ફ /	/		ફ/	/		so /	/		ફ/	/	
1	ens ens) Jes	/3	ָאַ / קַּפּֿ) Jes	1 4	ğ / g	nec /	1 4	0 0	Jes / Jes	./
	Tens	18		7ens	18	\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\	Tens	15	\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\	/e	/5	
\vdash	\leftarrow			\leftarrow	1	2	1	6	5	6	6	(
					1	2	1	6	5	6	6	

We read this number as one million, two hundred sixteen thousand, five hundred sixty-six.

To make the number easier to read, commas are used to separate the digits into groups of three. Each group of three digits (except the ones group) is read by saying the three-digit number followed by the name of the group it belongs to. Let's look at some other examples.

EXAMPLE 1: Read the number 12,318,412 out loud. Solution:

Billion	s	Mi	illion	s	Tho	usar	nds	Hui	ndre	ds
$\left \wp \right $		8			8/			\$		
fundred; ens) / œ	. / .	/ .	ĕ /	./.	, / t	ğ/,	./ ,	, /
Hund Jens	1	Tens	Ones	Hung	Tens	Ones	1	Tens	Ones	
	_			_			_	_		/
		1	2	3	1	8	4	1	2	

twelve million, three hundred eighteen thousand, four hundred twelve

EXAMPLE 2: Read the number 10,615,258,016 out loud. Solution:

[Bi	llion	s	М	illion	s	Tho	usar	nds	Hu	ndre	ds
	sp.			so _s			sp/	7	7	sp/	$\overline{}$	7
	Sus			7/) les		ens ens	2 / 8	13	ens ens	es / sa	· /
[=	7e/	0] £	7.	6	\z	7 _e /	δ	/₹	/e/	5	
	1	0	6	1	5	2	5	8	0	1	6	

ten billion, six hundred fifteen million, two hundred fifty-eight thousand, sixteen EXAMPLE 3: Read the number 210,344,865,008 out loud. Solution:

[Bi	llion	s	М	illion	s	Tho	usar	nds	Hui	ndre	ds
Hund	Tens	Ones		Tens	Ones	1 3	Tens	Ones	Hund	Tens	Ones	3/
2	1	0	3	4	4	8	6	5	0	0	8	

two hundred ten billion, three hundred fortyfour million, eight hundred sixty-five thousand, eight

In reading the number in the last example, notice that zeros are not read. This is because a zero means "no value." Thus, the number 500 means: no ones, no tens, and five hundreds. In the same way, the number 3,008 means: eight ones, no tens, no hundreds, and three thousands.

Also notice that we did not use the word "and" when reading any of the whole numbers in our examples. To take another example, the number "375" is read as "three hundred seventy-five," *not* as "three hundred and seventy-five." You only use "and" to show that a whole number also has a partial unit; we will talk about this in a later unit.

EXPRESSING WHOLE NUMBERS AS DOLLARS

To express a number in dollars, you write the dollar sign to the left of the number. Thus, "fifty dollars" is written as \$50. To give another example, "four thousand, five hundred forty dollars" is written as \$4,540.

■ UNIT 1 Exercises

Write the place value of the underlined digit.

1. 566

6. 23,498

2. 287

7. 44,593

3. 892

8. 125,986

4. 1,975

9. 345,687

5. 4,587

10. 15,677,890

Write these numbers.

	- 1	Bi	llion	s	М	illion	s	Tho	usar	nds	Hui	ndre	ds
	Hund	Tens	Ones	Hund	Tens	Ones	Hund	Tens	Ones	Hund	Tens	Ones	
11.								2	2	8	1	5	
12.					3	8	0	1	6	7	7	2	
13.			5	6	7	9	4	3	8	2	9	9	
14.	5	4	5	8	9	6	3	7	5	0	0	0	
15.				1	0	0	3	1	8	0	1	7	
16.							9	9	0	0	0	0	

Write these numbers in words.

- 17. 76
- 18. 235
- 19. 2,398
- 20. 12,398

ANSWERS

- 2.
- 3. _____
- 4.
- 5. _____
- 6. _____
- 7. _____
- 8. _____
- 9. _____
- 10. _____

- *25. 33,325,385,398

Write these numbers in digits.

- 26. seventy-five
- 27. forty-eight
- 28. Two hundred ninety-nine
- 29. Eight hundred four
- 30. Fifteen thousand, three hundred three
- 31. One hundred two thousand, thirty-nine
- 32. Six million, four hundred two thousand



ANS	W	FR	S
HIVO	44		J

- 26. _____
- 27. _____
- 28. _____
- 29. _____
- 30. _____
- 31. _____
- 32. _____

UNIT 2

Rounding Off Whole Numbers

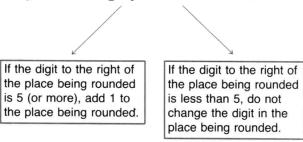
Astronomers tell us that the sun is 93,000,000 miles from earth. Does this mean that the distance has been exactly measured and the sun is precisely 93,000,000 miles away? Or does it mean that, by using mathematical formulas, astronomers have calculated that the sun is around 93,000,000 miles away and this figure is rounded to even millions to make it easier to work with and to remember?

Actually, the sun is *around* 93,000,000 miles from earth, not *exactly* 93,000,000 miles. There are many times when numbers are rounded to make them easier to use. For example, the population of New York City is often said to be 8,000,000 people. At a given time, however, the actual population could be a little over 8,000,000 or a little under 8,000,000. What if it were, say, 8,124,512? This number would be hard to remember. So, it is simply rounded to an even 8,000,000.

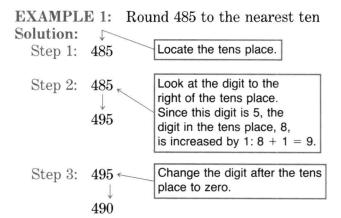
To "round off" a number means to use an approximate value instead of the exact value. To round off a number, follow these steps:

Step 1: Locate the place that you want to round the number to.

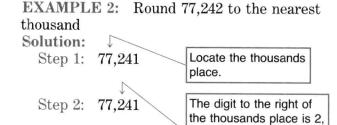
Step 2: Look at the digit to the immediate *right* of the digit you want to round:



Step 3: Drop all digits after the place being rounded and replace them with zeros.



Rounded answer = 490



Step 3: $77,241 \leftarrow$ Change all digits after the rounding place to zero. 77,000

which is less than 5; do not change the digit in the thousands place.

Rounded answer = 77,000

It is important to remember that when rounding, you only look at two digits: the place being rounded and the place to its right; do not look at any other digit.

Now, before we start the exercises, let's look at a few more examples.

EXAMPLES:

788 rounded to the nearest ten = 7907,455 rounded to the nearest hundred = 7,500



12,898 rounded to the nearest thousand	= 13,000
255,790 rounded to the nearest ten-thousand	= 260,000
397,800 rounded to the nearest hundred-thousand	= 400,000
1,897,476 rounded to the nearest million	= 2,000,000

UNIT 2 Exercises

Round these numbers to the nearest ten.

1. 75

6. 9.593

2.874

7. 12,356

3. 999

8. 15,837

4. 899

9. 25,925

5. 3,456

10. 33,121

Round these numbers to the nearest hundred.

11. 678

16. 4,610

12. 234

17. 12,875

13. 1,565

18. 17,008

14. 1,843

19. 21,081

15. 2,877

20. 34.571

Round these numbers to the nearest thousand.

21. 1,898

26. 21,967

22. 2,458

27. 45,854

23. 7,916

28. 67,858

24. 5,718

29. 91,546

25. 9,469

30. 77,999

ANSWERS

- 1. _____ 2. _____
- 3. _____
- 4. _____
- 5. _____
- 6. _____
- 8. _____
- 9. _____
- 10.
- 11. ____
- 12. _____
- 13. _____
- 14. _____
- 15. _____
- 16. _____
- 17. _____
- 18. _____
- 19. _____
- 20. _____
- 21. _____
- 22. _____
- 23. _____
- 24. _____
- 25. _____
- 26. _____
- 27. _____
- 28. _____
- 29. _____ 30. _____

Round these numbers to the nearest ten-thousand. **ANSWERS** 31. _____ 31. 34,598 36. 18,387 32. _____ 33. _____ 32. 56,987 37. 48,698 34. _____ 35. _____ 33. 47,698 38. 187,487 36. _____ 37. _____ 34. 59,308 39. 287,376 38. _____ 39. _____ 35. 59,287 40. 155,985 40. _____ Round these numbers to the nearest hundred-thousand. 41. _____ 41. 128,765 46. 705,982 42. _____ 43. _____ 42. 768,876 47. 3,409,876 44. _____ 45. _____ 43. 345,986 48. 4,986,487 46. _____ 47. _____ 44. 234,765 49. 7,856,387 48. _____ 49. _____ 45. 998,475 50. 8,265,973 50. _____ Round these numbers to the nearest million. 51. _____ 51. 3,598,587 56. 12,398,459 52. _____ 53. _____ 52. 4,598,219 57. 24,998,765 54. _____ 55. _____ 53. 8,498,986 58. 56,985,876 56. _____ 57. _____ 54. 3,999,876 59. 55,267,985 58. _____ 59. _____ 55. 7,987,376 60. 79,999,000 60. _____

ANSWERS

UNIT 2 Applications

1. Algood Company had these sales figures for the year:

Territory	Sales
North	\$2,988,964
South	3,499,437
East	3,288,388
West	4,988,876
East Central	2,388,984

Round each figure to the nearest thousand dollars.

2. Below are this month's sales for Lakeside Grocery. Round each amount to the nearest ten-thousand dollars.

Grocery:

\$78,988

Meat:

\$54,987

Produce:

\$32,876

Dairy:

\$18,769

Hardware: \$12,344

3. Round the cost of these clothing items to the nearest ten dollars.

Leather coats: \$99

Suede coats:

\$88

Belts:

\$12

Dress shoes:

\$65

Top coats:

\$95

4.	Zen Corporation had these profit figures for the last five years.
	Round each figure to the nearest million dollars.

19X1							\$2,488,987
LUZLI	•	•	•	•	•	•	Ψω, 100,00

- 5. Round 12,467,886 to the nearest:
 - a. ten
 - b. hundred
 - c. thousand
 - d. ten-thousand
 - e. hundred-thousand
 - f. million



4.	 _

5.	a.	
	_	