

Elementary Surveying

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PREFACE

In this fourth edition of **ELEMENTARY SURVEYING**, changes have been made in every chapter except Chapter 21. Suggestions made by users of the book have been incorporated in the new edition, along with clarifying sentences (some in italics) in many places where experience indicated that they would be helpful. Some of the more important improvements are as follows:

Chapter 2, Theory of Measurements and Errors, has been almost completely rewritten and its coverage greatly expanded.

More complete discussions are given for the Tellurometer, Geodimeter, Electrotape, and other new equipment in Chapter 4, Linear Measurements. Material on the subtense bar has been moved to Chapter 4, and a brief introduction given to triangulation and trilateration. The approach to tape corrections has been revised to better show the signs involved.

Precision requirements and permissible closures are given greater emphasis in several chapters.

A two-page isogonic chart replaces the single-page drawing, and other material on the compass has been upgraded.

Noteforms have been improved by making a few changes.

The uses and advantages of the principle of reversion have been noted throughout the book, where appropriate, instead of just in the chapter on adjustments.

Astronomical data have been brought up to date in examples and tabulations, and source notes added in the illustrations.

The use of second differences in checking parabolic curves has been included.

A larger number of problems and questions at the end of each chapter (totaling about 650) cover a wider range. Where feasible, consecutive odd- and even-numbered problems are similar, except for data. Some problems are carried through several chapters so that progressive steps in their completion can be followed.

As in the third edition, emphasis is placed upon the theory of errors and optics; correlation of theory and practical field methods;

elimination of typical errors and mistakes; significant figures; use of basic values such as $\sin 1 \text{ min} = 0.0003$ and $\sin 1^\circ = 0.01\frac{3}{4}$ in solving ordinary problems without tables or slide rule; and the interdependence of field, computation, and mapping requirements.

Engineers, architects, geologists, and foresters must be able to make measurements and to analyze the precision and accuracy of the results obtained by other people. They should be qualified to properly locate and set machinery; to lay out houses, buildings, and other common structures; and to understand and prepare simple topographic maps. Each of these areas is discussed, and proper field procedures to obtain a desired precision are noted.

A few cost figures are introduced so that students will learn early in their college work to associate the three bases of engineering practice—theory, application, and costs. All surveying is a constant fight to eliminate or isolate errors and mistakes. In each chapter the student is reminded of this point, through lists of typical errors and mistakes.

Although the third and fourth editions retain the title **ELEMENTARY SURVEYING**, the material goes beyond the elementary stage in length and scope. The large number of chapters, however, permits inclusion or omission of subjects to correspond with the class time available for students in civil engineering, other engineering curricula, architecture, geology, and forestry. It might be noted that the easy-reading qualities of the third edition have been retained by keeping short lines for ready scanning and fewer lines per page.

Chapters are arranged in the order found most convenient at numerous colleges. Fundamental material is collected in the first sixteen chapters comprising Part I. Theory and use of the four fundamental surveying instruments—the tape, level, transit, and plane table—are described in detail, and new types of equipment are noted. Any chapter following Chapter 11 can be omitted without loss of continuity, although many of them are short enough to be suitable for a single assignment.

Limited coverage of such subjects as photogrammetry, field astronomy, boundary surveys, and industrial applications of surveying methods is given in Part II to fit the programs offered at some colleges. For example, the brief chapter on boundary surveys

is intended to make students aware of a few of the problems involved in the survey and transfer of property, and the legal requirements of professional registration. Some instructors give broad survey-type courses and want their students to get an over-all view of the many facets of the profession. It is believed that the arrangement and scope of material presented herein will meet that need.

Taping, leveling, and transit work are taken up in that order because students find it easier to acquire some facility with the equipment in that sequence, and because this arrangement permits the start and continuation of field work with a minimum of lecture time. The suggested order of field assignments given in Appendix A makes it possible to begin effective computation and drafting-room problems after just a few periods in the field if bad weather is encountered.

The difficulty in getting through all of the preliminary material (basic conceptions of the profession, history, theory of errors, and methods of notekeeping) before commencing field work during the first week is recognized. Nevertheless the authors feel that these topics must precede the theory and use of instruments.

The subject of notes and noteforms—an important part of surveying and engineering—is discussed in a separate chapter. Most of the sample noteforms are collected in Appendix A instead of being scattered throughout the text.

Suggestions and criticism will be greatly appreciated.

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INTRODUCTION

1-1. Definition of surveying. Surveying is the science or art of making the measurements necessary to determine the relative positions of points above, on, or beneath the surface of the earth, or to establish such points. The work of the surveyor, which largely consists of making such measurements, can be divided into three parts:

FIELD WORK—Making and recording measurements in the field.

COMPUTING—Making the necessary calculations to determine locations, areas, and volumes.

MAPPING—Plotting the measurements and drawing a map.

1-2. Importance of surveying. Surveying is one of the oldest arts practiced by man, because from the earliest times it has been found necessary to mark boundaries and divide land. It is now indispensable in all branches of engineering. For example, surveys are required prior to and during the planning and construction of highways, railroads, buildings, bridges, missile ranges and launching sites, tunnels, canals, irrigation ditches, dams, drainage works, and water-supply and sewerage systems. They are also essential in laying out pipelines and mine shafts. The use of surveying or surveying methods has become common in the layout of assembly lines and jigs, the fabrication of airplanes, and the placement of equipment, and in many related tasks in aeronautical, agricultural, chemical, electrical, mechanical, and mining engineering, and in geology and forestry. Optical tooling represents an application of surveying in shop practice.

1-3. Training for all engineers. All engineers must know the limits of accuracy possible in construction, plant design and layout, and manufacturing processes, even though someone else does the actual surveying. This knowledge is best obtained by making measurements with the surveying equipment employed in practice, as such measurements will provide a true concept of the theory of errors.

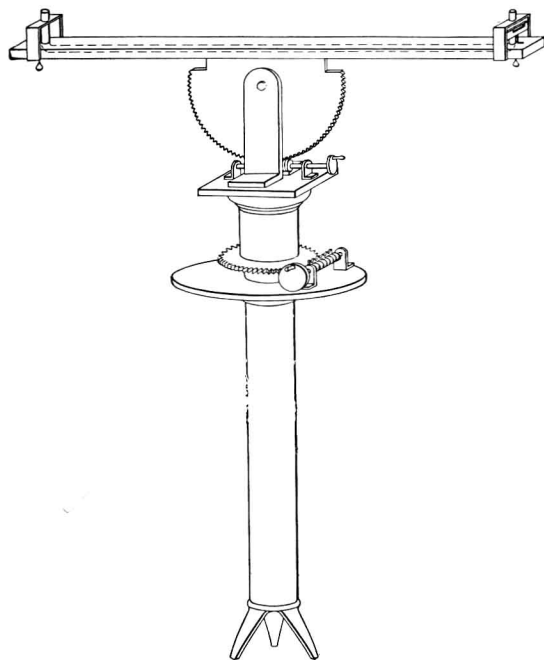
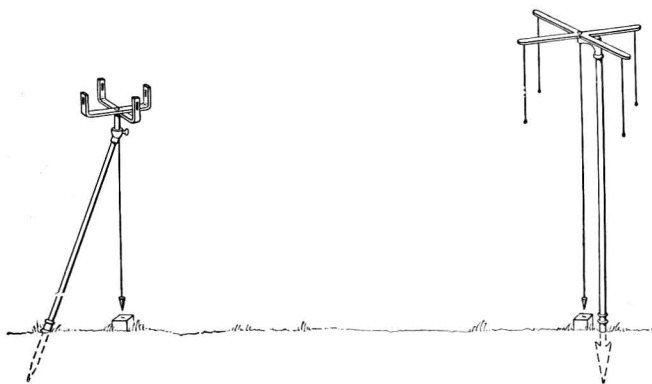
FIG. 1-1. The dioptra.¹

FIG. 1-2. The groma.

¹ Figures 1-1, 2, 3, and 4 are shown through the courtesy of Professor Edward Noble Stone.

In addition to stressing the need for reasonable limits of accuracy, surveying emphasizes the value of significant figures. An engineer must know when to work to hundredths of a foot instead of to tenths or thousandths, or perhaps the nearest foot, and what precision in field data is necessary to justify carrying out computations to the desired number of decimal places. With experience, he learns how the equipment and personnel available govern procedures and results.

Neat sketches and computations are the mark of an orderly mind, which in turn is an index of sound engineering background and competence. Taking field notes under all sorts of conditions is excellent preparation for the kind of recording and sketching expected of engineers. Additional training having a carry-over value is obtained in arranging computations properly.

1-4. History of surveying. The oldest historical records in existence today which bear directly on the subject of surveying state that this science had its beginning in Egypt. Herodotus says Sesostris (about 1400 B.C.) divided the land of Egypt into plots for the purpose of taxation. The annual floods of the Nile River swept away portions of these plots, and surveyors were appointed to replace the bounds. These early surveyors were called *rope-stretchers*. Their measurements were made by means of ropes with markers at unit distances.

As a consequence of this work the early Greek thinkers developed the science of geometry. Their advance, however, was chiefly along the lines of pure science. Heron stands out prominently for applying science to surveying, about 120 B.C. He was the author of several important treatises of interest to engineers, including one called *The Dioptra*, which related the methods of surveying a field, drawing a plan, and making calculations. This treatise also described one of the first pieces of surveying equipment recorded, the *dioptra* (Fig. 1-1). For many years Heron's work was the most authoritative among Greek and Egyptian surveyors.

Real development in the art of surveying came through the practical-minded Romans, whose best-known treatise on surveying was by Frontinus. Although the original manuscript disappeared, copied portions have been preserved. This noted Roman engineer and surveyor, who lived in the first century, was a pioneer in the field and his treatise remained the standard for many years.

The engineering ability of the Romans was demonstrated by their extensive construction work throughout the Empire. The surveying

necessary for this construction resulted in the organization of a surveyors' guild. Ingenious instruments were developed and used. Among these were the *groma* (Fig. 1-2), used for sighting; the *libella* (Fig. 1-3), an A frame with a plumb bob, used for leveling; and the *chorobates* (Fig. 1-4), a horizontal straightedge about 20 ft long, with supporting legs and with a groove on top for water to serve as a level.

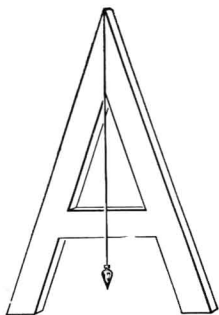


FIG. 1-3. The libella.

One of the oldest Latin manuscripts in existence is the *Codex Acerianus*, written about the sixth century. It contains an account of surveying as practiced by the Romans and includes several pages from Frontinus' treatise. The manuscript was found in the tenth century by Gerbert and served as the basis for his text on geometry, which was largely devoted to surveying.

During the Middle Ages, Greek and Roman science was kept alive by the Arabs. Little progress was made in the art of surveying, and the only writings pertaining to it were called "practical geometry."

In the thirteenth century Von Piso wrote *Practica Geometria*, which contained instructions on surveying. He also wrote *Liber Quadratorum*, dealing chiefly with the *quadrans*, a square brass frame having a 90° angle and other scales marked off on it. A movable pointer was used for sighting. Other instruments of the period were the *astrolabe*, a metal circle with a pointer hinged at its center and held by a ring at the top, and the *cross staff*, a wooden rod about 4 ft long with an adjustable crossarm at right angles to it. The known lengths of the arms of the cross staff permitted distances to be measured by proportion and angles.

In the eighteenth and nineteenth centuries the art of surveying advanced more rapidly. The need for maps and the location of national boundaries caused England and France to make extensive surveys requiring accurate triangulation. Thus geodetic surveying began. The United States Coast and Geodetic Survey was established by an act of Congress in 1807.

Increased land values and the importance of exact boundaries, along with the demand for public improvements in the turnpike, canal, and railroad eras, brought surveying into a prominent position.