

FUNDAMENTALS OF MODERN VLSI DEVICES

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PREFACE

It has been fifty years since the invention of the bipolar transistor, more than forty years since the invention of the integrated-circuit (IC) technology, and more than thirty-five years since the invention of the MOSFET. During this time, there has been a tremendous and steady progress in the development of the IC technology with a rapid expansion of the IC industry. One distinct characteristic in the evolution of the IC technology is that the physical feature sizes of the transistors are reduced continually over time as the lithography technologies used to define these features become available. For almost thirty years now, the minimum lithography feature size used in IC manufacturing has been reduced at a rate of $0.7\times$ every three years. In 1997, the leading-edge IC products have a minimum feature size of $0.25~\mu m$.

The basic operating principles of large and small transistors are the same. However, the relative importance of the various device parameters and performance factors for transistors of the 1-µm and smaller generations is quite different from those for transistors of larger-dimension generations. For example, in the case of CMOS, the power-supply voltage was lowered from the standard 5 V, starting with the 0.6- to 0.8-µm generation. Since then CMOS power supply voltage has been lowered in steps once every few years as the device physical dimensions are reduced. At the same time, many physical phenomena, such as short-channel effect and velocity saturation, which are negligible in large-dimension MOSFETs, are becoming more and more important in determining the behavior of MOSFETs of deep-submicron dimensions. In the case of bipolar devices, breakdown voltage and base-widening effects are limiting their performance, and power dissipation is limiting their level of integration on a chip. Also, the advent of SiGe-base bipolar technology has extended the frequency capability of small-dimension bipolar transistors into the range previously reserved for GaAs and other compound-semiconductor devices.

The purpose of this book is to bring together the device fundamentals that govern the behavior of CMOS and bipolar transistors into a single text, with emphasis on those parameters and performance factors that are particularly important for VLSI (very-large-scale-integration) devices of deep-submicron dimensions. The book starts with a comprehensive review of the properties of the silicon material, and the basic physics of p-n junctions and MOS capacitors, as they relate to the fundamental principles of MOS-FET and bipolar transistors. From there, the basic operation of MOSFET and bipolar

devices, and their design and optimization for VLSI applications are developed. A great deal of the volume is devoted to in-depth discussions of the intricate interdependence and subtle tradeoffs of the various device parameters pertaining to circuit performance and manufacturability. The effects which are particularly important in small-dimension devices, e.g., quantization of the two-dimensional surface inversion layer in a MOS-FET device and the heavy-doping effect in the intrinsic base of a bipolar transistor, are covered in detail. Also included in this book are extensive discussions on scaling and limitations to scaling of MOSFET and bipolar devices.

This book is suitable for use as a textbook by senior undergraduate or graduate students in electrical engineering and microelectronics. The necessary background assumed is an introductory understanding of solid-state physics and semiconductor physics. For practicing engineers and scientists actively involved in research and development in the IC industry, this book serves as a reference in providing a body of knowledge in modern VLSI devices for them to stay up to date in this field.

VLSI devices are too huge a subject area to cover thoroughly in one book. We have chosen to cover only the fundamentals necessary for discussing the design and optimization of the state-of-the-art CMOS and bipolar devices in the sub-0.5- μ m regime. Even then, the specific topics covered in this book are based on our own experience of what the most important device parameters and performance factors are in modern VLSI devices.

Many people have contributed directly and indirectly to the topics covered in this book. We have benefited enormously from the years of collaboration and interaction we had with our colleagues at IBM, particularly in the areas of advanced silicon-device research and development. These include Douglas Buchanan, Hu Chao, T. C. Chen, Wei Chen, Kent Chuang, Peter Cook, Emmanuel Crabbé, John Cressler, Bijan Davari, Robert Dennard, Max Fischetti, David Frank, Charles Hsu, Genda Hu, Randall Isaac, Khalid Ismail, G. P. Li, Shih-Hsien Lo, Yuh-Jier Mii, Edward Nowak, George Sai-Halasz, Stanley Schuster, Paul Solomon, Hans Stork, Jack Sun, Denny Tang, Lewis Terman, Clement Wann, James Warnock, Siegfried Wiedmann, Philip Wong, Matthew Wordeman, Ben Wu, and Hwa Yu.

We would like to acknowledge the secretarial support of Barbara Grady and the support of our management at IBM Thomas J. Watson Research Center where this book was written. Finally, we would like to give special thanks to our families – Teresa, Adrienne, and Brenda Ning and Betty, Ying, and Hsuan Taur – for their support and understanding during this seemingly endless task.

Yuan Taur Tak H. Ning Yorktown Heights, New York, October, 1997

PHYSICAL CONSTANTS AND UNIT CONVERSIONS

Description	Symbol	Value and unit
Electronic charge	\overline{q}	$1.6 \times 10^{-19} \text{ C}$
Boltzmann's constant	\boldsymbol{k}	$1.38 \times 10^{-23} \text{ J/K}$
Vacuum permittivity	$arepsilon_0$	$8.85 \times 10^{-14} \text{ F/cm}$
Silicon permittivity	$arepsilon_{si}$	$1.04 \times 10^{-12} \text{ F/cm}$
Oxide permittivity	ε_{ox}	$3.45 \times 10^{-13} \text{ F/cm}$
Velocity of light in vacuum	c	$3 \times 10^{10} \text{ cm/s}$
Planck's constant	h	$6.63 \times 10^{-34} \text{ J-s}$
Free-electron mass	m_0	$9.1 \times 10^{-31} \text{ kg}$
Thermal voltage ($T = 300 \text{ K}$)	kT/q	0.0259 V
Angstrom	Å	$1 \text{ Å} = 10^{-8} \text{ cm}$
Nanometer	nm	$1 \text{ nm} = 10^{-7} \text{ cm}$
Micrometer (micron)	μm	$1 \ \mu m = 10^{-4} \ cm$
Millimeter	mm	1 mm = 0.1 cm
Meter	m	$1 \text{ m} = 10^2 \text{ cm}$
Electron-volt	eV	$1 \text{ eV} = 1.6 \times 10^{-19} \text{ J}$
$Energy = charge \times voltage$	E = qV	$\underline{J}oule = \underline{C}oulomb \times \underline{V}olt$
Charge = capacitance \times voltage	Q = CV	$\underline{\mathbf{C}}$ oulomb = $\underline{\mathbf{F}}$ arad $\times \underline{\mathbf{V}}$ olt
$Power = current \times voltage$	P = IV	$\underline{\mathbf{W}}$ att = $\underline{\mathbf{A}}$ mpere $\times \underline{\mathbf{V}}$ olt
$Time = resistance \times capacitance$	t = RC	$\underline{\text{second}} = \underline{\Omega} \text{ (ohm)} \times \underline{F} \text{arad}$
Current = charge/time	I = Q/t	$\underline{\mathbf{A}}mpere = \underline{\mathbf{C}}oulomb/\underline{\mathbf{s}}econd$
Resistance = voltage/current	R = V/I	$\underline{\Omega}$ (ohm) = \underline{V} olt/ \underline{A} mpere

LIST OF SYMBOLS

Symbol	Description	Unit
A	Area	cm ²
A_E	Emitter area	cm^2
χ	Common-base current gain	None
\mathbf{x}_0	Static common-base current gain	None
χ_F	Forward common-base current gain in the Ebers-Moll	
	model	None
ℓ_R	Reverse common-base current gain in the Ebers-Moll	
	model	None
t_T	Base transport factor	None
t_n	Electron-initiated rate of electron-hole pair generation	
	per unit distance	cm^{-1}
t_p	Hole-initiated rate of electron-hole pair generation per	
	unit distance	cm^{-1}
SV	Breakdown voltage	V
V_{CBO}	Collector-base junction breakdown voltage with emitter	
	open circuit	V
V_{CEO}	Collector-emitter breakdown voltage with base	
	open circuit	V
V_{EBO}	Emitter-base junction breakdown voltage with collector	
	open circuit	V
	Common-emitter current gain	None
0	Static common-emitter current gain	None
F	Forward common-emitter current gain in the Ebers-	- 10110
	Moll model	None
R	Reverse common-emitter current gain in the Ebers-	
	Moll model	None
	Velocity of light in vacuum (= 3×10^{10} cm/s)	cm/s
*	Capacitance	F
d	Depletion-layer capacitance (per unit area)	F (F/cm
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C_{aBE} Base-emitter diode depletion-layer capacitance (per unit area) F (F/cm²) C_{aBC} Base-collector diode depletion-layer capacitance (per unit area) F (F/cm²) C_D Diffusion capacitance F C_{Dn} Diffusion capacitance due to excess electrons F C_{Dp} Diffusion capacitance due to excess holes F C_{DE} Emitter diffusion capacitance F C_B Intrinsic gate capacitance F C_g Intrinsic gate capacitance F C_i Inversion-layer capacitance (per unit area) F (F/cm²) C_i Inversion-layer capacitance (per unit area F/cm² C_i Interface trap capacitance per unit area F/cm² C_j Junction capacitance per unit area F/cm² C_j Junction capacitance per unit area F C_{out} Gate-to-source (-drain) overlap capacitance (per edge) F C_{out} Gate-to-source (-drain) overlap capacitance (per edge) F C_{out} Gate-to-source (-drain) overlap capacitance (per edge) F C_{out} Vire capacitance per unit area F/cm²	Symbol	Description	Unit
$ \begin{array}{c} (\text{per unit area}) & \text{F (F/cm}^2) \\ \text{Base-collector diode depletion-layer capacitance} \\ (\text{per unit area}) & \text{F (F/cm}^2) \\ C_D & \text{Diffusion capacitance} & \text{F} \\ C_{Dn} & \text{Diffusion capacitance due to excess electrons} & \text{F} \\ C_{Dp} & \text{Diffusion capacitance due to excess holes} & \text{F} \\ C_{Dp} & \text{Emitter diffusion capacitance} & \text{F} \\ C_{DE} & \text{Emitter diffusion capacitance} & \text{F} \\ C_{g} & \text{Intrinsic gate capacitance} & \text{F} \\ C_{g} & \text{Intrinsic gate capacitance} & \text{F} \\ C_{i} & \text{Interface trap capacitance per unit area} & \text{F/cm}^2 \\ C_{i} & \text{Interface trap capacitance per unit area} & \text{F/cm}^2 \\ C_{j} & \text{Junction capacitance} & \text{F} \\ C_{J} & \text{Junction capacitance} & \text{F} \\ C_{J} & \text{Junction capacitance} & \text{F} \\ C_{L} & \text{Load capacitance} & \text{F} \\ C_{L} & \text{Load capacitance} & \text{F} \\ C_{m} & \text{Equivalent input capacitance of a logic gate} & \text{F} \\ C_{out} & \text{Equivalent output capacitance of a logic gate} & \text{F} \\ C_{out} & \text{Equivalent output capacitance of a logic gate} & \text{F} \\ C_{out} & \text{Silicon capacitance per unit area} & \text{F/cm}^2 \\ C_{si} & \text{Silicon capacitance per unit area} & \text{F/cm}^2 \\ C_{si} & \text{Silicon capacitance per unit length} & \text{F/cm}^2 \\ C_{w} & \text{Wire capacitance per unit length} & \text{F/cm}^2 \\ C_{w} & \text{Wire capacitance per unit length} & \text{F/cm}^2 \\ C_{\mu} & \text{Base-eollector capacitance in the small-signal hybrid-π} \\ & \text{equivalent-circuit model} & \text{F} \\ C_{\mu} & \text{Base-collector capacitance in the small-signal hybrid-π} \\ & \text{equivalent-circuit model} & \text{F} \\ D_{n} & \text{Electron diffusion coefficient} & \text{cm}^2/\text{s} \\ D_{n} & \text{Electron diffusion coefficient in the base of an n-p-n} \\ & \text{transistor} & \text{cm}^2/\text{s} \\ D_{p} & \text{Hole diffusion coefficient in the emitter of an n-p-n} \\ & \text{transistor} & \text{cm}^2/\text{s} \\ D_{p} & \text{Hole diffusion coefficient in the emitter of an n-p-n} \\ & \text{transistor} & \text{cm}^2/\text{s} \\ D_{p} & \text{Apparent bandgap narrowing} & \text{J} \\ \Delta E_{g} & \text{Bandgap-narrowing parameter in the base region} & \text{J} \\ \Delta E_{g} & Bandgap$	C_{dm}	Maximum depletion-layer capacitance (per unit area)	F (F/cm ²)
$ \begin{array}{c} C_{dBC} & \text{Base-collector diode depletion-layer capacitance} \\ & (\text{per unit area}) & \text{F (F/cm}^2) \\ C_D & \text{Diffusion capacitance} & \text{F} \\ C_{Dn} & \text{Diffusion capacitance due to excess electrons} & \text{F} \\ C_{Dp} & \text{Diffusion capacitance due to excess holes} & \text{F} \\ C_{DE} & \text{Emitter diffusion capacitance} & \text{F} \\ C_{DE} & \text{Emitter diffusion capacitance} & \text{F} \\ C_{B} & \text{Intrinsic gate capacitance} & \text{F} \\ C_{I} & \text{Inversion-layer capacitance (per unit area}) & \text{F (F/cm}^2) \\ C_{I} & \text{Interface trap capacitance per unit area} & \text{F/cm}^2 \\ C_{J} & \text{Junction capacitance} & \text{F} \\ C_{L} & \text{Load capacitance} & \text{F} \\ C_{out} & \text{Equivalent input capacitance of a logic gate} & \text{F} \\ C_{out} & \text{Equivalent output capacitance of a logic gate} & \text{F} \\ C_{Out} & \text{Equivalent output capacitance of a logic gate} & \text{F} \\ C_{Out} & \text{Cat-to-source (-drain) overlap capacitance (per edge)} & \text{F} \\ C_{Si} & \text{Silicon capacitance per unit area} & \text{F/cm}^2 \\ C_{Si} & \text{Silicon capacitance per unit length} & \text{F/cm}^2 \\ C_{w} & \text{Wire capacitance per unit length} & \text{F/cm}^2 \\ C_w & \text{Wire capacitance per unit length} & \text{F/cm}^2 \\ C_{\mu} & \text{Base-emitter capacitance in the small-signal hybrid-}\pi \\ & \text{equivalent-circuit model} & \text{F} \\ C_{\mu} & \text{Base-collector capacitance in the small-signal hybrid-}\pi \\ & \text{equivalent-circuit model} & \text{F} \\ C_{\mu} & \text{Base-collector capacitance in the base of an n-p-n} \\ & \text{transistor} & \text{cm}^2/\text{s} \\ D_{pB} & \text{Hole diffusion coefficient} & \text{cm}^2/\text{s} \\ D_{pE} & \text{Hole diffusion coefficient in the base of an n-p-n} \\ & \text{transistor} & \text{cm}^2/\text{s} \\ \Delta E_{g} & \text{Apparent bandgap narrowing} & \text{J} \\ \Delta E_{g} & \text{Apparent bandgap narrowing due to Se in the} \\ SiGe-base bipolar transistor & \text{J} \\ E & \text{Energy} & \text{J} \\ E & \text{Energy} & \text{J} \\ E & \text{Conduction-band edge} & \text{J} \\ E & \text{Conduction-band edge} & \text{J} \\ E & \text{Conduction-band edge} \\ E & Conduc$	C_{dBE}	Base-emitter diode depletion-layer capacitance	
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$		(per unit area)	F (F/cm ²)
C_{Dn} Diffusion capacitance F C_{Dn} Diffusion capacitance due to excess electrons F C_{Dp} Diffusion capacitance due to excess holes F C_{DE} Emitter diffusion capacitance F C_B Intrinsic gate capacitance F C_I Inversion-layer capacitance (per unit area) F (F/cm² C_I Interface trap capacitance per unit area F/cm² C_I Interface trap capacitance per unit area F/cm² C_J Junction capacitance F C_J Gate-to-source (-drain) overlap capacitance (per edge) F C_{ax} Oxide capacitance per unit area	C_{dBC}	Base-collector diode depletion-layer capacitance	
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C_{DE} Emitter diffusion capacitance F C_g Intrinsic gate capacitance F C_i Inversion-layer capacitance (per unit area) F (F/cm²) C_i Interface trap capacitance per unit area F/cm² C_i Junction capacitance per unit area F/cm² C_j Junction capacitance F C_L Load capacitance F C_m Equivalent input capacitance of a logic gate F C_{out} Equivalent input capacitance of a logic gate F C_{out} Equivalent output capacitance of a logic gate F C_{out} Equivalent output capacitance of a logic gate F C_{out} Gate-to-source (-drain) overlap capacitance (per edge) F C_{out} Gate-to-source (-drain) overlap capacitance (per edge) F C_{out} Gate-to-source (-drain) overlap capacitance (per edge) F C_{out} Oxide capacitance per unit area F/cm² C_{out} Wire capacitance per unit area F/cm² C_{out} Wire capacitance per unit area F/cm² C_{out} Base-emitter capacitance in the small-sign	C_{Dn}	Diffusion capacitance due to excess electrons	F
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C_L Load capacitance F C_{in} Equivalent input capacitance of a logic gate F C_{out} Equivalent output capacitance of a logic gate F C_{ov} Gate-to-source (-drain) overlap capacitance (per edge) F C_{ox} Oxide capacitance per unit area F/cm² C_{si} Silicon capacitance per unit length F/cm² C_w Wire capacitance per unit length F/cm C_{π} Base-emitter capacitance in the small-signal hybrid- π equivalent-circuit model F C_{μ} Base-collector capacitance in the small-signal hybrid- π equivalent-circuit model F d Width of diffusion region in a MOSFET cm D_n Electron diffusion coefficient cm²/s D_n Electron diffusion coefficient in the base of an n-p-n transistor cm²/s D_p Hole diffusion coefficient in the emitter of an n-p-n transistor cm²/s ΔV_t Threshold voltage roll-off due to short-channel effect V ΔE_g Apparent bandgap narrowing J ΔE_g Bandgap-narrowing parameter in the base region J ΔE_g Tota	C_j	Junction capacitance per unit area	F/cm ²
C_{in} Equivalent input capacitance of a logic gate F C_{out} Equivalent output capacitance of a logic gate F C_{ov} Gate-to-source (-drain) overlap capacitance (per edge) F C_{ox} Oxide capacitance per unit area F/cm² C_{si} Silicon capacitance per unit area F/cm² C_w Wire capacitance per unit length F/cm C_{π} Base—emitter capacitance in the small-signal hybrid- π equivalent-circuit model F C_{μ} Base—collector capacitance in the small-signal hybrid- π F d Width of diffusion region in a MOSFET cm D_n Electron diffusion coefficient cm²/s D_{nB} Electron diffusion coefficient in the base of an n-p-n cm²/s D_p Hole diffusion coefficient cm²/s D_{pE} Hole diffusion coefficient in the emitter of an n-p-n cm²/s ΔV_t Threshold voltage roll-off due to short-channel effect V ΔE_g Apparent bandgap narrowing J ΔE_g Bandgap-narrowing parameter in the base region J ΔE_g Bandgap-narrowing parameter in the base bandgap	C_J	Junction capacitance	F
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C_{ov} Gate-to-source (-drain) overlap capacitance (per edge)F C_{ox} Oxide capacitance per unit areaF/cm² C_{si} Silicon capacitance per unit areaF/cm² C_w Wire capacitance per unit lengthF/cm C_{π} Base-emitter capacitance in the small-signal hybrid- π equivalent-circuit modelF C_{μ} Base-collector capacitance in the small-signal hybrid- π equivalent-circuit modelF d Width of diffusion region in a MOSFETcm D_n Electron diffusion coefficientcm²/s D_{nB} Electron diffusion coefficient in the base of an n-p-n transistorcm²/s D_p Hole diffusion coefficient in the emitter of an n-p-n transistorcm²/s ΔV_t Threshold voltage roll-off due to short-channel effectV ΔE_g Apparent bandgap narrowingJ ΔE_g Apparent bandgap narrowing due to Ge in the SiGe-base bipolar transistorJ E EnergyJ E EnergyJ E Conduction-band edgeJ	C_{in}	Equivalent input capacitance of a logic gate	F
C_{ox} Oxide capacitance per unit area F/cm^2 C_{si} Silicon capacitance per unit area F/cm^2 C_w Wire capacitance per unit length F/cm C_π Base-emitter capacitance in the small-signal hybrid- π equivalent-circuit model F C_μ Base-collector capacitance in the small-signal hybrid- π equivalent-circuit model F d Width of diffusion region in a MOSFETcm D_n Electron diffusion coefficientcm²/s D_{nB} Electron diffusion coefficient in the base of an n-p-n transistorcm²/s D_p Hole diffusion coefficient in the emitter of an n-p-ncm²/s D_{pE} Hole diffusion coefficient in the emitter of an n-p-ncm²/s ΔV_t Threshold voltage roll-off due to short-channel effectV ΔE_g Apparent bandgap narrowingJ ΔE_g Apparent bandgap narrowing due to Ge in the SiGe-base bipolar transistorJ E EnergyJ E EnergyJ E Conduction-band edgeJ	C_{out}	Equivalent output capacitance of a logic gate	F
C_{si} Silicon capacitance per unit area F/cm^2 C_w Wire capacitance per unit length F/cm C_π Base-emitter capacitance in the small-signal hybrid- π equivalent-circuit model F C_μ Base-collector capacitance in the small-signal hybrid- π equivalent-circuit model F d Width of diffusion region in a MOSFET cm D_n Electron diffusion coefficient cm^2/s D_{nB} Electron diffusion coefficient in the base of an $n-p-n$ transistor cm^2/s D_p Hole diffusion coefficient cm^2/s D_{pE} Hole diffusion coefficient in the emitter of an $n-p-n$ transistor cm^2/s ΔV_t Threshold voltage roll-off due to short-channel effect V ΔE_g Apparent bandgap narrowing J ΔE_{gB} Bandgap-narrowing parameter in the base region J $\Delta E_{g,SiGe}$ Total base bandgap narrowing due to Ge in the SiGe-base bipolar transistor J E Energy J E Energy J E Conduction-band edge J	C_{ov}	Gate-to-source (-drain) overlap capacitance (per edge)	F
C_w Wire capacitance per unit lengthF/cm C_π Base-emitter capacitance in the small-signal hybrid- π equivalent-circuit modelF C_μ Base-collector capacitance in the small-signal hybrid- π equivalent-circuit modelF d Width of diffusion region in a MOSFETcm D_n Electron diffusion coefficientcm²/s D_{nB} Electron diffusion coefficient in the base of an n-p-n transistorcm²/s D_p Hole diffusion coefficientcm²/s D_{pE} Hole diffusion coefficient in the emitter of an n-p-n transistorcm²/s ΔV_t Threshold voltage roll-off due to short-channel effectV ΔE_g Apparent bandgap narrowingJ ΔE_{gB} Bandgap-narrowing parameter in the base regionJ $\Delta E_{g,SiGe}$ Total base bandgap narrowing due to Ge in the SiGe-base bipolar transistorJEEnergyJ E_c Conduction-band edgeJ	C_{ox}	Oxide capacitance per unit area	F/cm ²
C_{π} Base-emitter capacitance in the small-signal hybrid- π equivalent-circuit model F C_{μ} Base-collector capacitance in the small-signal hybrid- π equivalent-circuit model F d Width of diffusion region in a MOSFET cm D_n Electron diffusion coefficient cm²/s D_{nB} Electron diffusion coefficient in the base of an n-p-n transistor cm²/s D_p Hole diffusion coefficient in the emitter of an n-p-n transistor cm²/s ΔV_t Threshold voltage roll-off due to short-channel effect V ΔE_g Apparent bandgap narrowing J $\Delta E_{g,SiGe}$ Total base bandgap narrowing due to Ge in the SiGe-base bipolar transistor J E Energy J E Conduction-band edge J	C_{si}	Silicon capacitance per unit area	F/cm ²
$C_{\mu} \qquad \text{Base-collector capacitance in the small-signal hybrid-}{\pi}$ $\text{equivalent-circuit model} \qquad F$ $d \qquad \text{Width of diffusion region in a MOSFET} \qquad \text{cm}$ $D_n \qquad \text{Electron diffusion coefficient} \qquad \text{cm}^2/\text{s}$ $D_{nB} \qquad \text{Electron diffusion coefficient in the base of an n-p-n}$ $\text{transistor} \qquad \text{cm}^2/\text{s}$ $D_p \qquad \text{Hole diffusion coefficient} \qquad \text{cm}^2/\text{s}$ $D_{pE} \qquad \text{Hole diffusion coefficient in the emitter of an n-p-n}$ $\text{transistor} \qquad \text{cm}^2/\text{s}$ $\Delta V_t \qquad \text{Threshold voltage roll-off due to short-channel effect} \qquad V$ $\Delta E_g \qquad \text{Apparent bandgap narrowing} \qquad \text{J}$ $\Delta E_{gB} \qquad \text{Bandgap-narrowing parameter in the base region} \qquad \text{J}$ $\Delta E_{g,SiGe} \qquad \text{Total base bandgap narrowing due to Ge in the}$ $\text{SiGe-base bipolar transistor} \qquad \text{J}$ $E \qquad \text{Energy} \qquad \text{J}$ $E \qquad \text{Energy} \qquad \text{J}$ $E \qquad \text{Conduction-band edge} \qquad \text{J}$	C_w	Wire capacitance per unit length	F/cm
C_{μ} Base—collector capacitance in the small-signal hybrid- π equivalent-circuit modelF d Width of diffusion region in a MOSFETcm D_n Electron diffusion coefficientcm²/s D_{nB} Electron diffusion coefficient in the base of an n-p-n transistorcm²/s D_p Hole diffusion coefficientcm²/s D_{pE} Hole diffusion coefficient in the emitter of an n-p-n transistorcm²/s ΔV_t Threshold voltage roll-off due to short-channel effectV ΔE_g Apparent bandgap narrowingJ ΔE_{gB} Bandgap-narrowing parameter in the base regionJ $\Delta E_{g.SiGe}$ Total base bandgap narrowing due to Ge in the SiGe-base bipolar transistorJ E EnergyJ E Conduction-band edgeJ	C_{π}	Base–emitter capacitance in the small-signal hybrid- π	
equivalent-circuit model F d Width of diffusion region in a MOSFET Cm D_n Electron diffusion coefficient Cm^2/s D_{nB} Electron diffusion coefficient in the base of an n-p-n Cm^2/s D_p Hole diffusion coefficient Cm^2/s D_pE Hole diffusion coefficient in the emitter of an n-p-n Cm^2/s ΔV_t Threshold voltage roll-off due to short-channel effect Cm^2/s ΔE_g Apparent bandgap narrowing Cm^2/s $\Delta E_{g,SiGe}$ Bandgap-narrowing parameter in the base region Cm^2/s C		equivalent-circuit model	F
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$\begin{array}{cccccccccccccccccccccccccccccccccccc$	D_n	Electron diffusion coefficient	cm ² /s
D_p Hole diffusion coefficient cm²/s D_{pE} Hole diffusion coefficient in the emitter of an n-p-n transistor cm²/s ΔV_t Threshold voltage roll-off due to short-channel effect V ΔE_g Apparent bandgap narrowing J ΔE_{gB} Bandgap-narrowing parameter in the base region J $\Delta E_{g,SiGe}$ Total base bandgap narrowing due to Ge in the SiGe-base bipolar transistor J E Energy J E Conduction-band edge J	D_{nB}	Electron diffusion coefficient in the base of an n-p-n	
D_{pE} Hole diffusion coefficient in the emitter of an n-p-n transistor cm ² /s ΔV_t Threshold voltage roll-off due to short-channel effect V ΔE_g Apparent bandgap narrowing J ΔE_{gB} Bandgap-narrowing parameter in the base region J $\Delta E_{g,SiGe}$ Total base bandgap narrowing due to Ge in the SiGe-base bipolar transistor J E Energy J E Conduction-band edge J		transistor	cm ² /s
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	D_p	Hole diffusion coefficient	cm ² /s
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	D_{pE}	Hole diffusion coefficient in the emitter of an n-p-n	
ΔE_g Apparent bandgap narrowing J ΔE_{gB} Bandgap-narrowing parameter in the base region J $\Delta E_{g,SiGe}$ Total base bandgap narrowing due to Ge in the SiGe-base bipolar transistor J E Energy J E_c Conduction-band edge J	·		cm ² /s
ΔE_g Apparent bandgap narrowing J ΔE_{gB} Bandgap-narrowing parameter in the base region J $\Delta E_{g,SiGe}$ Total base bandgap narrowing due to Ge in the SiGe-base bipolar transistor J E Energy J E_c Conduction-band edge J	ΔV_t	Threshold voltage roll-off due to short-channel effect	V
$\Delta E_{g,SiGe}$ Total base bandgap narrowing due to Ge in the SiGe-base bipolar transistor J E Energy J E_c Conduction-band edge J	ΔE_{g}		J
SiGe-base bipolar transistor J E Energy J E_c Conduction-band edge J	ΔE_{gB}	Bandgap-narrowing parameter in the base region	J
SiGe-base bipolar transistor J E Energy J E_c Conduction-band edge J	$\Delta E_{g,SiGe}$		
E _c Conduction-band edge J		- "	J
E _c Conduction-band edge J	E	Energy	J
	E_c		J
	E_v		J

Symbol	Description	Unit
E_a	Ionized-acceptor energy level	J
E_d	Ionized-donor energy level	J
E_f	Fermi energy level	J
E_g	Energy gap of silicon	J
E_i	Intrinsic Fermi level	J
E	Electric field	V/cm
\mathscr{E}_c	Critical field for velocity saturation	V/cm
$\mathscr{E}_{e\!f\!f}$	Effective vertical field in MOSFET	V/cm
\mathscr{E}_{ox}	Oxide electric field	V/cm
\widetilde{e}_s	Electric field at silicon surface	V/cm
\mathcal{E}_{x}	Vertical field in silicon	V/cm
\mathscr{E}_y	Lateral field in silicon	V/cm
€0	Vacuum permittivity (= 8.85×10^{-14} F/cm)	F/cm
si	Silicon permittivity (= 1.04×10^{-12} F/cm)	F/cm
ox	Oxide permittivity (= 3.45×10^{-13} F/cm)	F/cm
f	Probability that an electronic state is filled	None
f	Frequency, clock frequency	Hz
max	Maximum frequency of oscillation	Hz
f_T	Cutoff frequency	Hz
I	Fan-in	None
FO O	Fan-out	None
>	Barrier height	V
b_{ox}	Silicon-silicon dioxide interface potential	
	barrier for electrons	V
p_{ms}	Work-function difference between metal and silicon	V
O_n	Electron quasi-Fermi potential	v
p_p	Hole quasi-Fermi potential	V
	Number of degeneracy	None
ds	Small-signal output conductance	A/V
m	Small-signal transconductance	A/V
\vec{r}_E	Emitter Gummel number	s/cm ⁴
G_B	Base Gummel number	s/cm ⁴
	Emitter injection efficiency	None
	Planck's constant (= 6.63×10^{-34} J-s)	J-s
	Time-dependent current	Α
3	Time-dependent base current in a bipolar transistor	Α
,	Time-dependent small-signal base current	Α
7	Time-dependent collector current in a bipolar transistor	Α

Symbol	Description	Unit
$\overline{i_c}$	Time-dependent small-signal collector current	A
i_E	Time-dependent emitter current in a bipolar transistor	Α
I	Current	Α
I_B	Static base current in a bipolar transistor	Α
I_C	Static collector current in a bipolar transistor	Α
I_E	Static emitter current in a bipolar transistor	Α
I_S	Switch current in an ECL circuit	Α
I_g	Gate current in a MOSFET	Α
I_0	MOSFET current per unit width at threshold	A/cm
I_{dsat}	MOSFET saturation current	A
I_{on}	MOSFET on current (per unit width)	A (A/cm)
$I_{o\!f\!f}$	MOSFET off current (per unit width)	A (A/cm)
I_n	nMOSFET current per unit width	A/cm
I_p	pMOSFET current per unit width	A/cm
I_N	nMOSFET current	Α
I_P	pMOSFET current	Α
I_{ds}	Drain-to-source current in a MOSFET	Α
I_{sx}	Substrate current in a MOSFET	Α
J	Current density	A/cm ²
J_B	Base current density	A/cm ²
J_C	Collector current density	A/cm ²
J_n	Electron current density	A/cm ²
J_p	Hole current density	A/cm ²
k	Boltzmann's constant (= 1.38×10^{-23} J/K)	J/K
κ	Scaling factor (>1)	None
l	Mean free path	cm
L	Length, MOSFET channel length	cm
L_D	Debye length	cm
L_n	Electron diffusion length	cm
L_p	Hole diffusion length	cm
\dot{L}_{met}	Metallurgical channel length of MOSFET	cm
$L_{\it eff}$	Effective channel length of MOSFET	cm
L_w^-	Wire length	cm
m	MOSFET body-effect coefficient	None
m_0	Free-electron mass (= 9.1×10^{-31} kg)	kg
m^*	Electron effective mass	kg
M	Avalanche multiplication factor	None
μ	Carrier mobility	cm ² /V-s
	•	, , ,

Symbol	Description	Unit
$\mu_{\it eff}$	Effective mobility	cm ² /V-s
μ_n	Electron mobility	cm ² /V-s
μ_p	Hole mobility	cm ² /V-s
n	Density of free electrons	cm^{-3}
n_0	Density of free electrons at thermal equilibrium	cm^{-3}
n_i	Intrinsic carrier density	cm^{-3}
n_{ie}	Effective intrinsic carrier density	${ m cm^{-3}}$
n_{ieB}	Effective intrinsic carrier density in base of bipolar	
	transistor	cm^{-3}
n_{ieE}	Effective intrinsic carrier density in emitter of bipolar	
	transistor	cm^{-3}
n_n	Density of electrons in n-region	cm^{-3}
n_p	Density of electrons in p-region	cm^{-3}
N_a	Acceptor impurity density	cm^{-3}
N_d	Donor impurity density	cm^{-3}
N_b	Impurity concentration in bulk silicon	cm^{-3}
N_c	Effective density of states of conduction band	cm^{-3}
N_v	Effective density of states of valence band	cm^{-3}
N_B	Base doping concentration	cm^{-3}
N_C	Collector doping concentration	cm^{-3}
N_E	Emitter doping concentration	cm^{-3}
p	Density of free holes	cm^{-3}
p_0	Density of free holes at thermal equilibrium	cm^{-3}
p_n	Density of holes in n-region	cm^{-3}
p_p	Density of holes in p-region	cm^{-3}
P	Power dissipation	\mathbf{W}
P_{ac}	Active power dissipation	\mathbf{W}
$P_{o\!f\!f}$	Standby power dissipation	W
q	Electronic charge (= 1.6×10^{-19} C)	C
Q	Charge	C
Q_B	Excess minority charge in the base	C
Q_E	Excess minority charge in the emitter	C
Q_{BE}	Excess minority charge in the base-emitter space-	
	charge region	C
Q_{BC}	Excess minority charge in the base-collector space-	
	charge region	C
Q_{DE}	Total stored minority-carrier charge in a bipolar transis-	
	tor biased in the forward-active mode	C
Q_{pB}	Hole charge per unit area in base of n-p-n transistor	C/cm ²

Symbol	Description	Unit
Q_s	Total charge per unit area in silicon	C/cm ²
Q_d	Depletion charge per unit area	C/cm ²
Q_i	Inversion charge per unit area	C/cm ²
Q_f	Fixed oxide charge per unit area	C/cm ²
Q_m	Mobile charge per unit area	C/cm ²
Q_{it}	Interface trapped charge per unit area	C/cm ²
Q_{ot}	Oxide trapped charge per unit area	C/cm ²
Q_{ox}	Equivalent oxide charge density per unit area	C/cm ²
r, R	Resistance	Ω
r_b	Base resistance	Ω
r_{bi}	Intrinsic base resistance	Ω
r_{bx}	Extrinsic base resistance	Ω
r_c	Collector series resistance	Ω
r_e	Emitter series resistance	Ω
r_0	Output resistance in small-signal hybrid- π equivalent-	
	circuit model	Ω
r_{π}	Input resistance in small-signal hybrid- π equivalent-	
	circuit model	Ω
R_L	Load resistance in a circuit	Ω
R_s	Source series resistance	Ω
R_d	Drain series resistance	Ω
R_{sd}	Source-drain series resistance	Ω
R_{ch}	MOSFET channel resistance	Ω
R_w	Wire resistance per unit length	Ω/cm
R_{Sbi}	Sheet resistance of intrinsic-base layer	Ω/\square
R_{sw}	Equivalent switching resistance of a CMOS gate	Ω
R_{swn}	Equivalent switching resistance of nMOSFET pulldown	Ω
R_{swp}	Equivalent switching resistance of pMOSFET pullup	Ω
ho	Resistivity	Ω-cm
ho	Charge density	C/cm ³
$ ho_{sh}$	Sheet resistivity	Ω/\square
$ ho_{ch}$	Sheet resistivity of MOSFET channel	Ω/\square
$ ho_{sd}$	Sheet resistivity of source or drain region	Ω/\square
$ ho_c$	Specific contact resistivity	Ω -cm ²
S	MOSFET subthreshold slope	V/decade
S_p	Surface recombination velocity for holes	cm/s
σ_V	Vertical straggle of Gaussian doping profile	cm
σ_L	Lateral straggle of Gaussian doping profile	cm
t	Time	S

Symbol	Description	Unit
t_B	Base transit time	S
t_E	Emitter delay time	S
t_{BE}	Base-emitter depletion-layer transit time	S
t_{BC}	Base-collector depletion-layer transit time	S
t_{ox}	Oxide thickness	cm
t_w	Thickness of wire	cm
T	Absolute temperature	K
τ	Lifetime	s
τ	Circuit delay	s
$ au_b$	Buffered delay	s
$ au_{int}$	Intrinsic, unloaded delay	s
$ au_F$	Forward transit time of bipolar transistor	S
τ_n	Electron lifetime	S
τ_n	nMOSFET pulldown delay	s
$ au_{nB}$	Electron lifetime in base of n-p-n transistor	S
τ_p	Hole lifetime	S
$ au_p$	pMOSFET pullup delay	S
$ au_{pE}$	Hole lifetime in emitter of n-p-n transistor	S
$ au_R$	Reverse transit time of bipolar transistor	S
$ au_w$	Wire RC delay	S
υ	Velocity	cm/s
$v_{\it th}$	Thermal velocity	cm/s
v_d	Carrier drift velocity	cm/s
v_{sat}	Saturation velocity of carriers	cm/s
V	Voltage	V
V	Quasi-Fermi level along MOSFET channel	V
V_A	Early voltage	V
V_{app}	Applied voltage across p-n diode	V
V_{app}'	Applied voltage appearing immediately across p-n	
	junction (smaller than V_{app} by IR drops in series	
	resistances)	V
V_{BE}	Base-emitter bias voltage	V
V_{BC}	Base-collector bias voltage	V
V_{CE}	Collector-to-emitter voltage	V
V_{dd}	Power-supply voltage	V
V_{ds}	Source-to-drain voltage	V
V_{dsat}	MOSFET drain saturation voltage	V
V_{fb}	Flat-band voltage	V
V_{ox}	Potential drop across oxide	V
V_g	Gate voltage	V

Symbol	Description	Unit
$\overline{V_{bs}}$	Substrate reverse-bias voltage	V
V_t	Threshold voltage ($2\psi_B$ definition)	V
V_{on}	Linearly extrapolated threshold voltage	V
V_{in}	Input node voltage of a logic gate	V
V_{out}	Output node voltage of a logic gate	V
V_x	Node voltage between stacked nMOSFETs of a NAND	
	gate	V
W	Width, MOSFET width	cm
W_n	nMOSFET width	cm
W_p	pMOSFET width	cm
W_B	Intrinsic-base width	cm
W_d	Depletion-layer width	cm
W_{dBE}	Base-emitter junction depletion-layer width	cm
W_{dBC}	Base-collector junction depletion-layer width	cm
W_{dm}	Maximum depletion-layer width	cm
W_{dm}^0	Maximum depletion-layer width in long-channel device	cm
W_E	Emitter-layer width (thickness)	cm
W_S	Source junction depletion-layer width	cm
W_D	Drain junction depletion-layer width	cm
υ	Angular frequency	rad/s
\mathfrak{c}_j	Junction depth	cm
x_c, x_i	Depth of inversion channel	cm
ly .	Potential	V
ψ_B	Difference between Fermi level and intrinsic level	V
ν_{bi}	Built-in potential	V
ν_f	Fermi potential	V
ν_i	Intrinsic potential	V
ν_s	Surface potential	V

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