

# Social Statistics

A Text Using MicroCase®



William Fox

Fourth Edition

WADSWORTH MICROCASE  
STUDENT VERSION



# **Social Statistics**

Fourth Edition

**William Fox**  
Skidmore College

**THOMSON**  
—★—™  
**WADSWORTH**

Australia • Canada • Mexico • Singapore • Spain • United Kingdom • United States

Sociology Editor: *Bob Jucha*  
Assistant Editor: *Stephanie Monzon*  
Editorial Assistant: *Melissa Walter*

Marketing Manager: *Matthew Wright*  
Production Service: *Jodi Gleason*  
Copy Editor: *Margaret Moore*  
Printer: *Transcontinental Printing Inc.*

COPYRIGHT © 2003 Wadsworth Group.  
Wadsworth, is an imprint of the Wadsworth  
Group, a division of Thomson Learning, Inc.  
Thomson Learning™ is a trademark used herein under  
license.

ALL RIGHTS RESERVED. No part of this work  
covered by the copyright hereon may be reproduced or  
used in any form or by any means—graphic,  
electronic, or mechanical, including photocopying,  
recording, taping, Web distribution, or information  
storage and retrieval systems—without the prior  
written permission of the publisher.

Printed in Canada.

1 2 3 4 5 6 7 05 04 03 02 01

For permission to use material from this text,  
contact us by **Web**: <http://www.thomsonrights.com>  
**Fax**: 1-800-730-2215 **Phone**: 1-800-730-2214

For more information, contact  
**Wadsworth/Thomson Learning**  
**10 Davis Drive**  
**Belmont, CA 94002-3098**  
**USA**

For more information about our products, contact us:  
Thomson Learning Academic Resource Center  
1-800-423-0563  
<http://www.wadsworth.com>

**International Headquarters**  
Thomson Learning  
International Division  
290 Harbor Drive, 2<sup>nd</sup> Floor  
Stamford, CT 06902-7477  
**USA**

**UK/Europe/Middle East/South Africa**  
Thomson Learning  
Berkshire House  
168-173 High Holborn  
London WC1V 7AA  
United Kingdom

**Asia**  
Thomson Learning  
60 Albert Complex, #15-01  
Singapore 189969

**Canada**  
Nelson Thomson Learning  
1120 Birchmount Road  
Toronto, Ontario M1K 5G4

*To Collette, for all that matters.*

## **About the Author**

William Fox has a B.A. in Political Science from the University of Michigan and a Ph.D. in Sociology from Indiana University. He has taught at the University of Iowa, Florida Atlantic University, and Richmond College in London, and is now Professor of Sociology at Skidmore College in upstate New York. His current research interests are in urban folklore and social history. Bill lives with his wife, Collette, in an empty Victorian nest in Saratoga Springs, New York, where he enjoys biographies, Mozart, and roots music.

# Preface

This fourth edition of *Social Statistics* is prompted by the generous reception given previous editions and is guided by their users' comments and suggestions. Students and faculty alike have forwarded their ideas for conveying statistical ideas more effectively and efficiently. I have tried my best to incorporate the sense and substance of their suggestions in this edition. This edition uses updated and expanded data sets and incorporates a new version of the MicroCase software. I have again integrated data management techniques into statistical analysis and offered examples of statistical write-ups. Students welcomed the supportive, interactive style of earlier editions, and I have continued the same in this edition.

## MicroCase

This text uses a student version of MicroCase, a straightforward, no-nonsense piece of statistics software. MicroCase does data analysis and gets the job done efficiently, competently, and intelligently. You will learn statistics, and substantive social science too, with minimal distraction from the computer itself. No inundation with esoteric options. Just learning statistics (or whatever). Just doing data analysis. I have written this text in the same pragmatic spirit as MicroCase.

You will like MicroCase a lot. It can do just about any sort of statistical analysis that you are ever likely to want to carry out. Here are some of the things that MicroCase can do:

- Compute percentages.
- Produce statistical tables.
- Produce pie charts and bar graphs.
- Draw outline maps showing geographic distributions of variables.
- Compute means and medians.

- Compute standard deviations and variances.
- Compute cross-tabulations, chi squares, and measures of association.
- Do  $t$  tests and analyses of variance.
- Compute regression and correlation coefficients.
- Compute multiple regression and correlation coefficients.
- Create new variables from old ones and manage data in useful ways.

There's no need to worry if you don't know what some of these things are. You will know all of them after finishing this text and accompanying workbook.

MicroCase is available for Windows-compatible computers like IBM, Dell, and Compaq computers. (Sorry, fellow Apple fans, but we have to use Windows computers for MicroCase.) You already own MicroCase. A version called Student MicroCase came on a CD-ROM disc with this text's workbook. Student MicroCase is a slimmed down but still powerful version of the full MicroCase.<sup>1</sup>

Don't worry if you don't know much about computers or even if you have never used one. You don't need to know much about computers themselves to make good, intelligent use of MicroCase to do statistics. You don't have to write computer programs or design computer systems—nothing like that. The accompanying workbook will give you all the information you need.

## What to Expect in this Text

Let me explain how I have organized this text. We will learn statistics by beginning with the simplest situations and then moving through increasingly complex analyses. We will start with methods for analyzing only one variable at a time. Then we will take up methods for analyzing a relationship between two variables. That's a little more complex. And finally we will consider techniques for studying relationships among three or more variables at a time. That's really complex. Sensibly enough (at least if you know some Latin), these three situations involve *univariate*, *bivariate*, and *multivariate analyses*, respectively. That is how we will proceed in this text. The workbook has exercises that encourage you to apply your knowledge of statistics and carry out computer analyses of real data.

---

<sup>1</sup> Your school may have the full MicroCase if it participates in the MicroCase Curriculum Plan and has a site license. You can find out from your instructor if the full MicroCase is available at your school.

---

This book covers basic statistical methods. Although you will not be a full-fledged statistician after finishing *Social Statistics*, you will know enough statistics to critically evaluate others' uses of basic statistical techniques and to analyze data yourself. In other words, you will be both an informed consumer and a responsible producer of statistics. You will also be well prepared to study more advanced statistics should you choose to do so. In short, you won't learn everything about statistics from this text, but you will learn a lot.

I have written this text for students in the social sciences and related disciplines such as social work, criminal justice, public administration, and education. I assume that you need to carry out real analyses using real data, so I do not avoid the problems you and I find in the "real world"—missing information, skewed data, outliers, variables that need to be collapsed, and so on. In this text we will face the messiness that makes the social world so challenging to study and so much fun to live in. This text relies heavily on real data from sources like the U.S. Census, *Uniform Crime Reports*, and the General Social Survey—data that full-fledged social scientists analyze in their own research. Thus, we can't avoid facing the real issues and problems that come with real data. Still, there are times when messiness of data can get in the way of learning statistics, so I have not hesitated to make up data to introduce certain statistical techniques when "clean" examples foster learning. We'll use whatever data—real or imaginary—best helps us learn statistics.

I also assume that you need to present your statistical analyses to others (your instructor now, employers or a larger "public" later in your life), so I include guidelines for writing up statistical analyses, formatting tables, and constructing graphs. You will also find examples of analysis write-ups following several chapters. You will probably find these write-ups useful as models for describing your own research results. You don't need to be a professional statistician to communicate statistical findings effectively to others. You will be able to do so after finishing this text.

So this text does not skimp on nitty-gritty details about doing real statistics in the real world. But I am also concerned that you understand statistical principles and reasoning. You need this understanding to know what statistical procedures are right for given situations and to interpret statistical analyses sensibly. Therefore, I will go beyond formulas and procedures to explain why we are doing what we do. You will find almost no computational formulas in this book to facilitate calculations. Computers render such formulas unnecessary. There is, of course, a place for computational formulas. They mostly belong in a Museum of Statistical Antiquities, maybe in a glass case next to slide rules, to remind us how unpleasant and tedious statistics used to be.



But this text does not shy away entirely from formulas and calculations. To the contrary, we will learn to do calculations “by hand” before using the friendly computer to do this mostly routine work for us. Initially while learning data analysis, calculating statistics with our human brains is essential for understanding why statistics work the way they do and what the computer’s faster brain does for us. However, we will use definitional rather than computational formulas. Although less convenient and more tedious, definitional formulas describe what statistics are really about and thus are the best way to understand how statistics works. The *Doing Statistics Using MicroCase* workbook accompanying this text invites you to do paper-and-pencil calculations before carrying out computer analyses.

But in the last analysis (literally), the computer exercises in the workbook are even more important than the “by hand” exercises. I have written the workbook for you to use actively with a computer. You should, in fact, read and do most of the workbook while using a computer.

You will find this textbook and workbook conversational in style. That’s deliberate. It’s the way I teach. My students and I interact in the classroom and, within the limits imposed by print, there is no reason why you and I should not interact via this text. So, I hope you will not take my use of the second-person “you” as an unwarranted familiarity, nor my frequent use of “we” as either an affectation or a ploy. You and I—*we*—are learning statistics together even though you are learning stat for the first time and I am learning it for the umpteenth time.

When you are finished with this book, I hope you will begin a lifetime using statistics effectively. I trust that you will be an intelligent critic of others’ applications of statistics and will use statistics intelligently yourself. But beyond these practical goals, I hope you will appreciate the beauty, elegance, and grace of statistics. Like other magnificent achievements of human reason, statistics at its core is an aesthetic endeavor.

## **What You Need to Bring to This Text**

You are probably interested in what you need to know *before* you begin to learn statistics. I assume you know basic arithmetic—adding, subtracting, multiplying, and dividing. You should also be reasonably comfortable with fractions and decimals, squares and square roots, and simple equations.

Whatever else you need to know you will learn along the way. All the better if you have had a course in research methods, but that is not essential. Likewise, I hope you have had several substantive

courses in the social sciences, but those too are not really necessary. Frankly, I assume more motivation and good will on your part than I do prior knowledge.

I trust that you have a good statistics teacher. I think good textbooks matter (that's why I have worked hard on this one), but reading even the best text is less important than learning from a knowledgeable and enthusiastic teacher.

Oh yes, you also need a calculator. An inexpensive one is fine as long as it finds square roots. Some graph paper will also be useful.

## Acknowledgments

This fourth edition, like its predecessors, was written at Skidmore College. I am fortunate indeed to teach at a college so committed to the liberal arts, high-quality teaching, and support of its faculty . . . and so cognizant that these three commitments are one.

This text began with my former colleague Richard Rosenfeld, now at the University of Missouri at St. Louis. Rick extolled the virtues of MicroCase, gently nagged me to try it, suggested the need for an accompanying stat text, and then actively supported my project at critical points. Without Rick, I would not have published this book.

Many users of previous editions offered suggestions that were most helpful for revisions. Especially valuable for this fourth edition have been comments and ideas from these colleagues across the country:

Michelle Benson, University at Buffalo, SUNY  
 Judith G. Calvo, California State University, Fresno  
 Walter F. Carroll, Bridgewater State College  
 Douglas Forbes, University of Wisconsin, Marshfield  
 David J. Gotcher, Abilene Christian University  
 Daniel A. Powers, University of Texas at Austin  
 Zhenchao Qian, Arizona State University  
 David Shafer, University of South Florida  
 James V. Spickard, University of Redlands  
 John Tinker, California State University, Fresno  
 Yvonne Vissing, Salem State College  
 Susan Waller, University of Central Oklahoma

The Wadsworth folks—Julie Aguilar, Jodi Gleason, Margaret Moore, and Meredith Reitman—did everything they could to aid this book's progress. They variously caught errors, edited, and provided MicroCase displays, all with much care and patience. Most important of all, however, they offered patience. I thank them all for seeing this project through with an optimal blend of professionalism and empathy.

Any errors that remain are mine alone.

Thanks, too, to my students over the years, especially at Skidmore College. True, they couldn't stop me from trying different teaching strategies on them. But they need not have been so good-natured nor have taught me so much, and for that I am grateful. I received assistance from Skidmore College's computer specialists, especially Leo Geoffrion and Beth Dupont. These are the user-friendliest bunch of alpha geeks anywhere. Lauren Sweeney, my terrific assistant, worked on this textbook project with extraordinary diligence and moxie.

I want to thank Elton Jackson, Professor Emeritus of Sociology at Indiana University, for teaching me statistics. On the first day of class, Elton promised a new way of seeing the world. He delivered on that promise. I learned statistics and much more from Elton Jackson.

My appreciation goes to several individuals and institutions who provided the data files upon which most of the workbook exercises are based. First, I obtained all my data sets from the MicroCase Data Archive, which saved me weeks of work. Special thanks goes to Tom W. Smith at the National Opinion Research Center for his continued direction and administration of the General Social Survey. Thanks also goes to the Inter-University Consortium for Political and Social Research (ICPSR) and to The Roper Center for their many years of distribution of the General Social Survey. The data archives maintained by the ICPSR and The Roper Center are an invaluable service to social science researchers.

I am grateful to the Literary Executor of the late Sir Ronald A. Fisher, F.R.S., Dr. Frank Yates, F.R.S., and the Longman Group Ltd, London, for permission to reprint parts of Tables III and IV from their book *Statistical Tables for Biological, Agricultural and Medical Research*.

But most of all, I want to thank Emmylou Harris and Collette Fox. Emmylou and all her acoustic pals make great music that goes so well with statistics and just about everything else in life. And Collette makes that life worthwhile.

## **Any Comments or Suggestions?**

I want very much to hear from you if you have any helpful feedback concerning this text. Let me know what you like and don't like about it, what works well and what can be improved, what might be left out and what needs to be added. E-mail me at [statprof@skidmore.edu](mailto:statprof@skidmore.edu). Or you can write me by snail mail at the following address:

William Fox  
Department of Sociology, Anthropology,  
and Social Work  
Skidmore College  
Saratoga Springs, NY 12866

One final word before we start learning statistics: I had a great time writing this book. I hope you enjoy it just as much.

Bill Fox  
Skidmore College

# Contents

About the Author.....	xi
Preface .....	xiii

## Part I: Introduction and Univariate Analyses

<b>Chapter 1: Statistics and Variables .....</b>	<b>3</b>
1.1 Statistics and Data .....	4
1.2 Overview of Statistics .....	5
1.3 Samples and Populations .....	6
1.4 Variables.....	8
1.5 Levels of Measurement.....	9
1.6 Mutually Exclusive and Collectively Exhaustive .....	14
1.7 Continuous and Discrete Variables.....	15
1.8 What Cases, Variables, and Data Files Look Like.....	16
1.9 Aggregate Data .....	18
1.10 Ideas and Thinking.....	20
1.11 Playing with Data .....	22
1.12 Summing Up Chapter 1.....	22
<b>Chapter 2: Frequency and Percentage Distributions .....</b>	<b>27</b>
2.1 Frequency Distributions .....	28
2.2 Percentage Distributions .....	31
2.3 Cumulative Distributions.....	34
2.4 Creating Sensible and Well-Formatted Tables.....	36
2.5 Collapsing Variables .....	38
2.6 Excluding Missing Data .....	42
2.7 Selecting Subsets of Cases .....	45
2.8 Pie Charts and Bar Graphs.....	45
2.9 Outliers.....	48

2.10	Mapping Ecological Variables .....	49
2.11	Summing Up Chapter 2.....	51
<b>Writing Statistics 1: Percentages Distributions, Graphs, and Maps .....</b>		<b>55</b>
<b>Chapter 3: Averages .....</b>		<b>61</b>
3.1	Mode.....	62
3.2	Median .....	63
3.3	Mean.....	66
3.4	Properties of the Mean.....	68
3.5	The Mean for Dichotomous Variables .....	70
3.6	Which to Use—Mode, Median, or Mean?.....	72
3.7	Summing Up Chapter 3.....	75
<b>Chapter 4: Measures of Variation .....</b>		<b>79</b>
4.1	Variances and Standard Deviations.....	80
4.2	Shapes of Distributions.....	87
4.3	Standard Scores (Z-Scores).....	89
4.4	Normal Distributions.....	91
4.5	Sampling Distributions.....	94
4.6	Confidence Intervals .....	98
4.7	Some Cautions Using Univariate Statistics .....	100
4.8	Summing Up Chapter 4.....	102
<b>Writing Statistics 2: Averages and Standard Deviations .....</b>		<b>105</b>

## **Part II: Bivariate Analyses**

<b>Chapter 5: Cross-tabulation .....</b>		<b>109</b>
5.1	Bivariate Frequency Tables.....	110
5.2	Bivariate Percentage Tables .....	113
5.3	How to Read Percentage Tables .....	116
5.4	Positive, Negative, and Curvilinear Relationships.....	118
5.5	Format Conventions for Bivariate Tables.....	122
5.6	Stacked Bar Graphs for Bivariate Relationships .....	125
5.7	A Caution About Bivariate Tables Based on Small Ns.....	126
5.8	Association Does <i>Not</i> Imply Causation.....	127
5.9	Summing Up Chapter 5.....	129
<b>Chapter 6: The Chi-Square Test of Statistical Significance .....</b>		<b>133</b>
6.1	The Logic of Tests of Statistical Significance .....	134
6.2	The Chi-Square Test .....	137
6.3	Problems with Expected Frequencies Less Than 5 .....	144
6.4	Statistical Significance Does Not Mean Substantive Significance.....	145

6.5	Significance Tests on Population Data .....	147
6.6	Summing Up Chapter 6.....	147
<b>Chapter 7: Measures of Association for Cross-tabulations .....</b>		<b>151</b>
7.1	Overview of Measures of Association .....	152
7.2	Chi-Square-Based Measures for Nominal Variables: V and $\phi$ .....	152
7.3	Lambda .....	155
7.4	Choosing a Nominal Measure of Association .....	158
7.5	Measures of Association for Ordinal Variables: Gamma .....	159
7.6	Somers' $D_{YX}$ .....	164
7.7	Measures of Association: An Overview .....	168
7.8	Summing Up Chapter 7.....	169
<b>Writing Statistics 3: Bivariate Cross-tabulations .....</b>		<b>172</b>
<b>Chapter 8: Comparison of Means and <math>t</math> Test.....</b>		<b>175</b>
8.1	Box-and-Whiskers Diagrams/Differences Between Means....	176
8.2	$t$ Test for the Difference Between Means.....	179
8.3	Assumptions and Cautions Concerning $t$ Test.....	186
8.4	One-Tailed and Two-Tailed Tests .....	188
8.5	Confidence Intervals for Differences Between Means .....	190
8.6	Summing Up Chapter 8.....	192
<b>Writing Statistics 4: Comparison of Means and <math>t</math> Test.....</b>		<b>195</b>
<b>Chapter 9: Analysis of Variance .....</b>		<b>197</b>
9.1	Box-and-Whiskers Diagrams/Differences Among Means.....	198
9.2	Purpose and Assumptions of Analysis of Variance.....	201
9.3	The Logic of Analysis of Variance.....	202
9.4	The ANOVA Table.....	211
9.5	The Correlation Ratio ( $E^2$ ).....	211
9.6	Two-Way Analysis of Variance (and Beyond) .....	213
9.7	Three Cautions About Statistically Significant $F$ Ratios .....	214
9.8	Summing Up Chapter 9.....	215
<b>Writing Statistics 5: Analysis of Variance .....</b>		<b>218</b>
<b>Chapter 10: Regression and Correlation .....</b>		<b>221</b>
10.1	Scatterplots .....	222
10.2	Scatterplots and the Strength of Relationships .....	225
10.3	Some Limitations of Scatterplots.....	228
10.4	Regression and Least-Squares Lines.....	229
10.5	Calculating Regression Coefficients .....	233
10.6	Correlation Coefficient ( $r$ ) .....	234
10.7	$r^2$ as Proportion of Variation Explained .....	239

10.8	Correlations Between Dichotomous Variables.....	241
10.9	Association <i>Still</i> Does Not Imply Causation .....	242
10.10	Linear and Nonlinear Relationships.....	242
10.11	Test of Significance for a Correlation Coefficient.....	243
10.12	Correlation Matrix.....	245
10.13	Summing Up Chapter 10.....	247

Writing Statistics 6: Regression and Correlation .....	251
--	-----

## **Part III: Multivariate Analyses**

Chapter 11: Multivariate Cross-tabulation .....	255
11.1 The Logic of Causal Relationships .....	256
11.2 Spurious Relationships .....	258
11.3 Some Terminology.....	261
11.4 Examples of Spurious Relationships .....	262
11.5 Replication.....	263
11.6 Somewhere Between Explanation and Replication.....	264
11.7 Specification .....	265
11.8 Suppressor Variables.....	266
11.9 Controlling for an Intervening Variable.....	269
11.10 Partial Gamma .....	271
11.11 An Overview of Elaboration.....	272
11.12 Elaboration and Problems of Small Ns .....	273
11.13 The Relationship of Multivariate Analysis to Experiment Design .....	274
11.14 Summing Up Chapter 11 .....	276

Writing Statistics 7: Multivariate Cross-tabulation.....	279
--	-----

Chapter 12: Multiple Regression and Correlation.....	281
12.1 Extending the Regression Model .....	281
12.2 Multiple Correlation Coefficient .....	287
12.3 Standardized Regression Coefficients (Beta Coefficients).....	289
12.4 Significance Tests for Multiple Correlation Coefficients.....	291
12.5 Regression with Dichotomous and Dummy Variables.....	292
12.6 Summing Up Chapter 12.....	295

Writing Statistics 8: Multiple Regression and Correlation.....	299
--	-----

## **Appendix: Statistical Tables**

Table 1: The Chi-Square Distribution .....	303
Table 2: The <i>t</i> Distribution.....	304
Table 3A: The <i>F</i> Distribution: $p = .05$ .....	305



---

Table 3B: The $F$ Distribution: $p = .01$ .....	306
Table 3C: The $F$ Distribution: $p = .001$ .....	307
<b>Glossary</b> .....	309
<b>Bibliography</b> .....	325
<b>Index</b> .....	329