IN TRODUCTION TO BUSINESS STATISTICS



RONALD M. WEIERS

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INTRODUCTION TO BUSINESS STATISTICS



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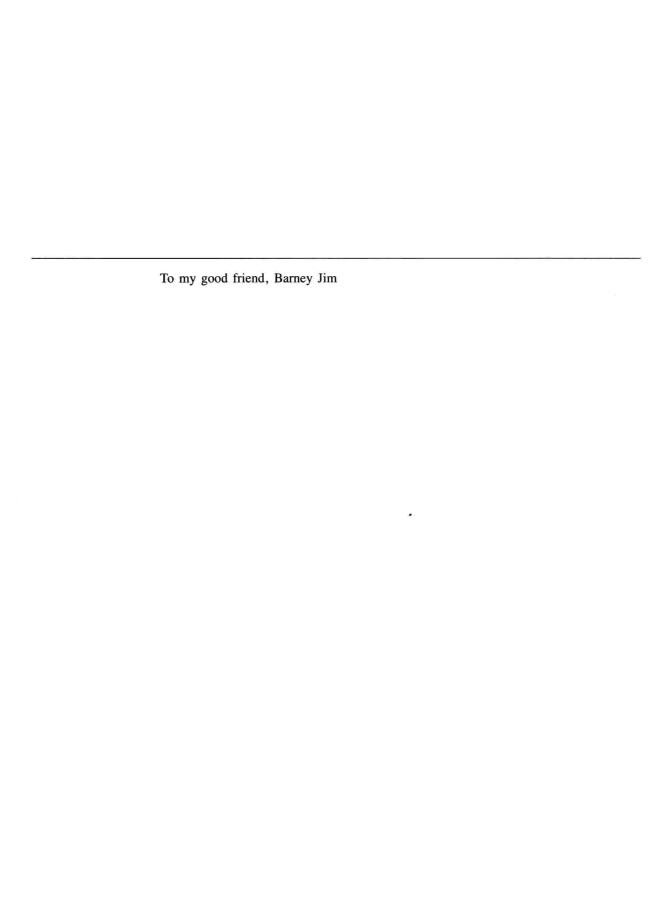
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Philosophies and Goals of the Text: A Message to the Student

A book is a very special link between author and reader. In a mystery novel, the author presents the reader with a maze of uncertainty, perplexity, and general quicksand. Intellectual smokescreens are set up all the way to the "whodunit" ending. Unfortunately, many business statistics texts seem to be written the same way — except for the "whodunit" section. This text is specifically designed to be different. Its goals are: (1) to be a friendly guide as you learn about business statistics, (2) to avoid quicksand that could inhibit either your interest or your learning, and (3) to earn and retain your trust in our ability to accomplish goals 1 and 2.

The chapters that follow are designed to be both informal and informative, as befits an introductory text in business statistics. You will not be expected to have had mathematical training beyond simple algebra, and mathematical symbols and notations will be explained as they become relevant to our discussion. Following an introductory explanation of the purpose and the steps involved in each technique, you will be provided with several down-to-earth examples of its use. Each section has a set of exercises based on the section contents. At the end of each chapter you'll find a summary of what you've read and a listing of equations that have been introduced, as well as a demonstration problem, chapter exercises, a minicase, and a computer database exercise to help you practice your skills. A self-test is provided to help you evaluate how well you've learned the material.

Features of the Text

The Use of Examples

Each chapter is packed with examples to illustrate the techniques within, and, whenever possible, they are of a scale that permits solution with a pocket calculator. In addition to describing a technique and presenting a pocket calculator example of its application, we will typically present one or more MINITAB printouts that show how the problem can be handled with this popular statistical package. This pedagogical strategy is used so the reader will have a greater appreciation for what's going on inside the computer when it must be applied to problems of a larger scale.

As pocket calculators have become more advanced, the need for statistical tables has been reduced. For example, we will assume that the reader's pocket calculator is capable of such functions as computing logarithms and generating squares and square roots. In

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days gone by, it was not unusual for statistics texts to include separate tables for capabilities that are now offered in even the lower echelon of pocket calculators.

The Use of Real Data

The value of statistical techniques becomes more apparent through the consistent use of real data in the text. Data sets, gathered from such publications as *Fortune 500*, *Newsweek*, and *The Wall Street Journal*, are used in more than 500 exercises and examples to make statistics both relevant and interesting for students.

The Computer

The combination of more powerful microcomputers and the statistical software designed specifically for them has revolutionized the world of statistics and data analysis. Statistical packages such as SPSS, SAS, SYSTAT, and MINITAB are among those formerly available only for mainframe computers, but which now can be applied by the microcomputer user. While the principles are the same, the convenience is markedly improved. In addition, strictly microcomputer packages are proliferating at a rapid rate.

The text includes computer output from several statistical packages, primarily MIN-ITAB, one of the most popular packages used in the teaching of business statistics. Printouts from MICROSTAT and MYSTAT (the student version of SYSTAT) are also provided. MINITAB and MYSTAT are "command-driven" in that the user must communicate with the computer by means of specific commands telling it what data manipulations or analyses to perform. Each printout from these packages is accompanied by the command(s) that generated the output. MICROSTAT, designed strictly for the microcomputer, is "menu-driven" and the user need only select from a list of alternatives displayed on the screen. Depending on which choice is made from the main menu, other menus will appear as they become appropriate, and the user need only type in a letter or number to proceed to the next stage of data handling or analysis.

Each of the approximately 200 computer printouts is completely interpreted and linked to a concept or example presented earlier in its respective chapter. Whether or not the reader is using a computer statistical package in conjunction with the course, he or she should find that these printouts enhance the learning process. To illustrate the principles of the techniques discussed in the text, many of our examples will be on a scale that allows hand calculation. However, in many of these cases the corresponding computer output will also be presented, as a means of supplementing the student's learning experience with a "computer's-eye" view of the same analysis.

The text also follows the continuing saga of Grandfather (Luke) and Grandson (Ted) Thorndike in their application of chapter concepts to Thorndike Sports Equipment. At the end of each chapter, the reader will have the opportunity to help them apply statistical concepts to their business. In many of the Thorndike adventures, a computer statistical package will be a helpful, but optional, partner.

Computer database exercises provide the opportunity to apply chapter concepts and a computer statistical package to a real-world database, the Springdale Shopping Survey. Only the names have been changed, and the numbers represent the opinions and behaviors of real people in a real community. The entire database contains 38 variables for 200 respondents. With 7600 data points, the database is large enough to allow a wide variety of statistical questions, but small enough that the reader will not have to take a nap while his or her microcomputer is working on them. This and additional databases (including shortened versions for those using the student editions of computer statistical packages

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such as MINITAB) are also available on the data diskette, to be discussed in the Ancillary Items section.

Unique Chapters

In our competitive global economy, product quality is increasingly important to manufacturers and consumers alike, and Chapter 17, Statistics in Quality Control, introduces the student to selected techniques that are in widespread use in the quality control field. As in the core chapters, heavy emphasis is given to the application of computer statistical packages in assisting quality control personnel. While the chapter is not intended to prepare the reader for an immediate position in a quality control department, he or she will gain a new perspective regarding the importance of quality control and the role that statistics plays in it.

Whether carrying out one's own investigation or evaluating a study that was done by someone else, it's helpful to have at least an introductory knowledge of how business research is typically carried out. Chapter 19, Business and Survey Research, discusses primary versus secondary data, the research process, survey research and questionnaire design, and the conduct of experiments and observational research. A brief summary of some of the more well-known published and other secondary data sources is provided, along with a discussion of how to go about evaluating the applicability and the quality of such information. Chapter 19 is intended to reinforce the fact that data such as those presented in exercises and examples throughout the book do not simply materialize: They are the result of business research efforts relevant to a real-world business problem or situation.

To the knowledge of the author and publisher, never before has an introductory business statistics textbook included a separate chapter like Chapter 20, Ethics in Statistical Analysis and Reporting. In the United States, polling seems to have become a national obsession, and unscientific surveying and sampling methods abound—e.g., "900-number" polls and "person-on-the-street" interviews. Also, the results of data analysis are often strategically clouded with jargon that is specifically designed to sell a conclusion while at the same time masking the path through which it was reached. In sum, Chapter 20 is designed to promote healthy skepticism and to facilitate personal self-defense for the consumer of statistical findings offered by others.

Organization of the Text

The text can be used in either a one-term or a two-term course. For one-term applications, Chapters 1 through 9 are suggested. For two-term use, it is recommended that the first term include Chapters 1 through 9, and that the second term include Chapters 10 through 16. In either one- or two-term use, the number and variety of chapters allows for instructor flexibility in designing either a course or a sequence of courses that will be of maximum benefit to the student. This flexibility includes the possibility of including one or more of the four remaining chapters, four of which are in the Special Topics section of the text.

Chapter 1 provides an introductory discussion of business statistics and its relevance to the real world. Chapter 2 covers descriptive statistics and the visual summarization methods used in presenting statistical information. In Chapters 3 through 5, we discuss the basic notions of probability and go on to introduce the discrete and continuous probability distributions upon which many statistical analyses depend. In Chapters 6 and 7, the philosophies and methods of sampling and generalizing upon sample findings are discussed.

Chapters 8 through 12 focus on the use of sample data to reach conclusions regarding the phenomena that the data represent. In these chapters, the reader will learn how to use statistics in deciding whether or not to reject statements that have been made concerning these phenomena. In Chapters 13 and 14, methods are introduced that allow us to employ equations in describing how one variable tends to change in response to changes in one or more others.

Chapters 15 and 16 examine time series, forecasting, and index number concepts used in analyzing data that occur over a period of time. Chapter 17 examines the application of statistics to quality control, while Chapter 18 discusses the role of statistics in decision theory. Chapter 19 examines some of the popular approaches by which statistical data are collected or generated.

In Chapter 20, statistics and its practitioners are discussed in terms of larger social and ethical implications. At the end of the text, there is a helpful glossary of the key terms presented in the book, a set of statistical tables, answers to selected exercises, and answers to the self-test questions at the end of each chapter. For convenience, the front and rear endsheets contain the two statistical tables to which the reader will most often be referring: the standard normal distribution and the t distribution.

The problems and examples contained in the text represent an extremely diverse selection of business settings, ranging from airlines to hospitals, marketing to manufacturing, personnel to shipping, and sports teams to zoos. Such diversity is important, since readers will be concentrating on a wide variety of business disciplines and headed for equally diverse business careers.

Ancillary Items

To further enhance the usefulness of the text, a complete package of ancillary items has been assembled.

Instructor's Manual (Weiers).

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This manual contains suggested syllabi, possible class projects and special assignments, and additional discussion and examples, including relevant computer analyses that utilize a second major computer database. The manual also includes approximately 100 transparency masters that are based on key figures and tables in the text and features Student-Edition MINITAB solutions to the Computer Database Exercises.

Solutions Manual (Chaffe-Stengel, Colvin-White, Curtiss, and Weiers).

Solutions to the over 1500 exercises in the textbook, with each exercise classified according to type (definition, computation, and problem-solving), tools required (pencil, calculator, computer), and level of difficulty (easy, medium, difficult). The solutions manual also contains annotated answers to the end-of-chapter self-test questions as well as solutions to the Thorndike Minicases and full MINITAB solutions to the Computer Database Exercises.

Test Bank (Gooden, Berger, Farshidi, and Rizzo).

There are 1500 test questions, with about 100 for each of the core chapters in the text. The questions include true-false, multiple-choice, and problems similar to those at the ends of the chapters. Questions are classified according to level of difficulty and are referenced to a specific page in the text.

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Computerized Test Bank

Adopters with IBM-compatible or Apple computers can use the available ExaMaster software to tailor examinations to their particular students and course format. For a given examination, up to 99 different versions can be printed.

RequesTest.

This additional service, provided by the publisher, allows the instructor to use a toll-free number to receive test masters (by mail or fax) according to question number and/or selection criteria.

Study Guide (Chaffe-Stengel).

A useful and easy-to-read supplement. Each chapter of the *Study Guide* includes an outline in the form of a logical flow chart connecting major text ideas, selected annotated solutions, and additional exercises.

Software Conversions Guide (Young).

Included with every text purchased, this laminated card provides students with the equivalent commands for performing common input/output and analysis procedures with four major statistical software packages: MINITAB, MYSTAT, SAS, and SPSS.

Data Disk (Taiani and Weiers).

Also available to instructors, this diskette includes data for the Springdale Shopping Survey that is the topic of most of the computer database exercises in the text. As a unique feature, the appendix table of random digits is also provided in electronic form as a computer database to facilitate computer analysis and to demonstrate chapter principles. To enhance course flexibility, a database from another real-world survey (Wendy's) is featured in the *Instructor's Manual*, and this database is also included on the data diskette. All three databases are provided in both ASCII and MINITAB worksheet (*.MTW suffix) formats.

For those using the student editions of packages like MINITAB, shortened versions of all three databases are also provided—each in ASCII and MINITAB formats. The following data files are on the data diskette:

README.TXT Text file discussing the files on the data diskette, including format information for the ASCII files. The README.TXT file is an ASCII file accessible with most word processors and contains the latest available information pertaining to the data diskette and the use of its data files.

SHOPPERS.DAT Springdale Shopping Survey ASCII

SHOPLITT.DAT Springdale ASCII (shortened)

SHOPPERS.MTW Springdale MINITAB

SHOPLITT.MTW Springdale MINITAB (shortened, for Student Edition of MINITAB)

RANDNUMB.DAT Table of random digits ASCII

RANDLITT.DAT Table of random digits ASCII (shortened)

RANDNUMB.MTW Table of random digits MINITAB

RANDLITT.MTW Table of random digits MINITAB (shortened, for Student Edition of MINITAB)

Also, pertaining to the *Instructor's Manual* and its additional examples:

WENDYS.DAT Wendy's survey ASCII

WENDLITT.DAT Wendy's ASCII (shortened)

WENDYS.MTW Wendy's MINITAB

WENDLITT.MTW Wendy's (shortened, for Student Edition of MINITAB)

The inclusion of MINITAB-specific data files allows the MINITAB user to avoid having to recode (.) missing-data values to the (*) values that MINITAB expects. To make computer involvement as convenient as possible, additional variants may appear in response to adopter requests, so be sure to view the README.TXT file on the data diskette for the very latest information describing the database files and how to use them.

Available Software EDUSTAT (Young).

The Dryden Press computer statistical package is available free of charge for class reproduction. Also, MYSTAT, the PC version of SYSTAT, will be available as a packaging option for instructors interested in this particular software.

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Ronald M. Weiers, Ph.D. Indiana University of Pennsylvania March 1991

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