

# Lecture Notes in Computer Science

759

Nabil R. Adam    Bharat K. Bhargava (Eds.)

## Advanced Database Systems



Springer-Verlag

A 264 Nabil R. Adam Bharat K. Bhargava (Eds.)

# Advanced Database Systems

**Springer-Verlag**  
Berlin Heidelberg New York  
London Paris Tokyo  
Hong Kong Barcelona  
Budapest

# Lecture Notes in Computer Science

759

Edited by G. Goos and J. Hartmanis

Advisory Board: W. Brauer D. Gries J. Stoer



# Contents

<b>I</b>	<b>Object-Oriented Databases</b>	<b>1</b>
<b>1</b>	<b>COMPOSE: A System for Composite Specification and Detection</b>	<b>3</b>
	by <b>N. Gehani, H.V. Jagadish, O. Shmueli</b>	
1.1	Introduction . . . . .	3
1.2	Event Expressions . . . . .	4
1.2.1	Basic Operators . . . . .	5
1.2.2	Additional Operators . . . . .	5
1.2.3	Regular Expressions . . . . .	6
1.3	Examples . . . . .	7
1.3.1	Simple Examples . . . . .	7
1.3.2	Discount Rate Cut . . . . .	7
1.3.3	Attributes and Masks . . . . .	8
1.3.4	Parameters . . . . .	9
1.3.5	Correlation Variables . . . . .	10
1.4	Composite Event Detection . . . . .	10
1.4.1	Design Decisions . . . . .	11
1.4.2	Masks . . . . .	11
1.4.3	Generic Automaton For Implementing Events With Parameters . . . . .	12
1.5	Compose System . . . . .	12
1.6	Examples of Automata Generated by Compose . . . . .	13
1.7	Conclusion . . . . .	14
<b>2</b>	<b>Access Controls in OO Database Systems – Some Approaches and Issues</b>	<b>17</b>
	by <b>E. Bertino, S. Jajodia, P. Samarati</b>	
2.1	Introduction . . . . .	17
2.2	Object-oriented Data Model . . . . .	19
2.3	Mandatory Access Control . . . . .	21
2.4	Discretionary Access Control . . . . .	25
2.4.1	The ORION Authorization Model . . . . .	25
2.4.2	Content-dependent Authorizations . . . . .	34
2.4.3	Accessing Objects Through Methods . . . . .	35
2.5	Research Issues in Mandatory Access Control . . . . .	38
2.5.1	Modeling Multilevel Entities as Single-level Objects . . . . .	38

2.5.2	Object Updates and Secure Garbage Collection Mechanisms	40
2.5.3	Polyinstantiation . . . . .	41
2.5.4	Comparison With Relevant Work . . . . .	42
2.6	Research Issues in Discretionary Access Control . . . . .	43
2.7	Conclusion . . . . .	44
<b>3</b>	<b>The Decomposition Property of Non-Deterministic Databases</b>	<b>45</b>
	by <b>K. Vadaparty, S. Naqvi</b>	
3.1	Introduction . . . . .	45
3.2	Basic Notions . . . . .	49
3.2.1	Entailment, and Data Complexity . . . . .	49
3.2.2	Choices and Data Complexity . . . . .	50
3.3	Size and Density of a Witness . . . . .	52
3.3.1	Size of a Witness . . . . .	53
3.3.2	Density of Witnesses . . . . .	56
3.4	Modulewise Evaluation . . . . .	56
3.5	Future Extensions . . . . .	63
<b>4</b>	<b>The Architectures of an Object Base Environment for Simulation</b>	<b>65</b>
	by <b>P.C.-Y. Sheu, L.J. Peterson</b>	
4.1	Introduction . . . . .	65
4.2	Related Work . . . . .	66
4.3	Object Representation . . . . .	67
4.3.1	Complex Objects . . . . .	67
4.3.2	Active Objects and Models . . . . .	68
4.4	Management of Active Objects . . . . .	71
4.4.1	State Space and Criteria . . . . .	71
4.4.2	Adding and Removing A State . . . . .	71
4.4.3	Adding and Removing A Rule . . . . .	72
4.4.4	Adding and Removing An Attribute . . . . .	73
4.4.5	Adding and Removing A Method or A Class . . . . .	73
4.5	Simulation . . . . .	73
4.5.1	Rule Processing . . . . .	73
4.5.2	Logic of The Simulator . . . . .	78
4.5.3	Parallel Processing . . . . .	79
4.5.4	Example . . . . .	80
4.6	Object-Oriented Evaluation of Rule Networks . . . . .	81
4.6.1	Structures of Extensional Databases and Query Networks	81
4.6.2	Object-Oriented Rule Evaluation . . . . .	83
4.7	Conclusion . . . . .	85

<b>5</b>	<b>Transition from a Relation to Object Model Implementation</b>	<b>87</b>
	by <b>B. Bhargava, Y. Jiang, J. Srinivasan, P. Dewan</b>	
5.1	Modeling Complex Data . . . . .	87
5.2	Survey of Extended Relational Systems . . . . .	88
5.3	O-Raid System Design and Implementation . . . . .	90
	5.3.1 Expand Query Language . . . . .	90
	5.3.2 Extend Data Definition Facility . . . . .	91
	5.3.3 Data Manipulation Language (DML) . . . . .	97
5.4	Performance Studies . . . . .	99
5.5	Research Issues . . . . .	102
<b>6</b>	<b>An Object-Oriented Knowledge Model for KBMS-Supported Evolutionary Prototyping of Software Systems</b>	<b>105</b>
	by <b>S.Y.W. Su, Y. Shyy</b>	
6.1	Introduction . . . . .	105
	6.1.1 Motivation . . . . .	105
	6.1.2 Related Works . . . . .	106
6.2	Knowledge Model Overview . . . . .	107
	6.2.1 Classes . . . . .	107
	6.2.2 Objects and Instances . . . . .	108
6.3	Structural Abstraction . . . . .	108
	6.3.1 Structural Association Definitions . . . . .	108
	6.3.2 Encapsulation and Inheritance . . . . .	109
	6.3.3 Extensible Kernel Model . . . . .	109
	6.3.4 Structural Association Patterns . . . . .	110
6.4	Behavioral Abstraction . . . . .	111
	6.4.1 Method Model and Control Associations . . . . .	112
	6.4.2 Method_model Object and Evolutionary Prototyping . . . . .	115
	6.4.3 Rule Definition . . . . .	116
6.5	Conclusions . . . . .	117
<b>7</b>	<b>Applying OOAD in the Design and Implementation of an Intelligent Geographic Information System</b>	<b>127</b>
	by <b>R. Subramanian, N.R. Adam</b>	
7.1	Introduction . . . . .	127
7.2	Modeling & Query Processing . . . . .	128
7.3	Spatial Data Modeling . . . . .	130
	7.3.1 The Design Methodology . . . . .	130
7.4	The Responsibility-Driven Approach . . . . .	131
7.5	Developing the Data Model . . . . .	132
	7.5.1 The Exploratory Phase . . . . .	132
	7.5.2 The Analysis Phase . . . . .	139
7.6	Implementation . . . . .	144
7.7	Conclusion . . . . .	145

**II Temporal/Historical Database Systems 151**

**8 Indexical Databases 153**  
 by J. Clifford

8.1 Motivation . . . . . 153

8.2 The Indexical Database Model . . . . . 155

8.2.1 The Structures . . . . . 155

8.2.2 Discussion of the Structures . . . . . 156

8.2.3 An Indexical Example: The Watergate Database . . . . . 158

8.2.4 The Operations . . . . . 159

8.2.5 Partial Functions . . . . . 168

8.3 Instances of the Indexical Database Model . . . . . 172

8.3.1 HRDM . . . . . 172

8.3.2 Bitemporal Database Models . . . . . 173

8.4 Summary and Conclusions . . . . . 173

**9 A Temporal Query Language for a Conceptual Model 175**  
 by R. Elmasri, V. Kouramajian

9.1 Introduction . . . . . 175

9.2 Representing Time . . . . . 176

9.3 The Temporal Data Model . . . . . 176

9.3.1 Conceptual Objects: Entities . . . . . 176

9.3.2 Temporal Objects: Roles . . . . . 177

9.3.3 Temporal Constraints among Roles . . . . . 178

9.3.4 Non-Temporal Attributes . . . . . 178

9.3.5 Temporal Attributes . . . . . 178

9.3.6 Classes and Superclass/Subclass Relationships . . . . . 179

9.3.7 Conceptual Relationships . . . . . 179

9.3.8 Temporal Relationships . . . . . 180

9.3.9 Temporal Constraints among Relationships . . . . . 180

9.3.10 An Example . . . . . 180

9.4 Temporal Query Language Constructs . . . . . 181

9.5 The Temporal Query Language . . . . . 183

9.5.1 Temporal Projection . . . . . 184

9.5.2 Temporal Selection . . . . . 187

9.5.3 Temporal Version Restriction Operators . . . . . 188

9.5.4 Temporal Scope Operators . . . . . 190

9.6 Conclusions . . . . . 190

**10 A Data Model for Time-Series Analysis 191**  
 by A. Segev, R. Chandra

10.1 Introduction . . . . . 191

10.2 Main Features of The Data Model . . . . . 192

10.2.1 Relevant Research . . . . . 193

10.3 Vector Based Data Model . . . . . 194

10.4 Concepts . . . . .	198
10.5 Rules . . . . .	203
10.6 Calendar . . . . .	204
10.7 Temporal Query Language . . . . .	205
10.8 Special Operators for Time-Series Database . . . . .	206
10.9 Handling of Missing Values . . . . .	208
10.10 User Environment . . . . .	208
10.11 Conclusion . . . . .	209
<b>11 A Relational Model and SQL-like Query Language for Spatial Databases</b>	<b>213</b>
by S.K. Gadia, V. Chopra	
11.1 Introduction . . . . .	213
11.1.1 Related Works . . . . .	213
11.1.2 Our Concept of A Spatial Region . . . . .	214
11.1.3 Weak Data Typing . . . . .	215
11.1.4 Uniformity of Attribute Values . . . . .	215
11.1.5 Experience From Temporal Databases . . . . .	215
11.2 Our Model . . . . .	216
11.2.1 Spatial Regions . . . . .	216
11.2.2 Attribute Values . . . . .	216
11.2.3 Value Navigation . . . . .	217
11.2.4 Spatial Tuples . . . . .	217
11.2.5 Spatial Relations . . . . .	218
11.2.6 Weak Equality and Restructuring . . . . .	219
11.3 Querying in The Model . . . . .	219
11.3.1 Spatial Expressions . . . . .	219
11.3.2 Boolean Expressions . . . . .	220
11.3.3 Relational Expressions . . . . .	220
11.3.4 Examples . . . . .	221
11.4 Seamlessness of SpaSQL . . . . .	222
11.5 Algebraic Nature of SpaSQL . . . . .	224
11.6 Conclusion . . . . .	224
<b>III Query Processing in Database Systems</b>	<b>227</b>
<b>12 Parallel Query Processing</b>	<b>229</b>
by P.S. Yu, M.-S. Chen, J.L. Wolf, J. Turek	
12.1 Introduction . . . . .	229
12.2 Preliminaries . . . . .	230
12.3 Issues . . . . .	231
12.3.1 Intra-operator Parallelism . . . . .	232
12.3.2 Inter-operator Parallelism . . . . .	232
12.3.3 Inter-query Parallelism . . . . .	233
12.3.4 Remarks . . . . .	234
12.4 System Architectures . . . . .	234

12.5	Data Skew and Intra-operator Parallelism . . . . .	235
12.5.1	Conventional Algorithm . . . . .	238
12.5.2	Dynamic Algorithms . . . . .	239
12.5.3	Sophisticated Algorithms . . . . .	240
12.6	Complex Multi-join Query . . . . .	242
12.6.1	Join Methods without Pipelining . . . . .	243
12.6.2	Join Methods with Pipelining . . . . .	248
12.7	Scheduling Multiple Complex Queries . . . . .	252
12.7.1	A Hierarchical Approach to Inter-Query Parallelism . . . . .	253
12.7.2	Scheduling Independent Tasks . . . . .	255
12.8	Summary . . . . .	258
<b>13</b>	<b>Towards Flexible Distributed Information Retrieval</b> . . . . .	<b>259</b>
	by D.W. Flater, Y. Yesha	
13.1	Introduction . . . . .	259
13.2	Information Retrieval Techniques . . . . .	260
13.2.1	Tag-Based Retrieval . . . . .	260
13.2.2	Partial Content-Based Retrieval . . . . .	261
13.2.3	Full Content-Based Retrieval . . . . .	261
13.3	Thesauri and Dictionaries . . . . .	261
13.3.1	Thesauri . . . . .	262
13.3.2	Dictionaries . . . . .	263
13.4	Fuzzy Retrieval . . . . .	263
13.4.1	Partial Content-Based Methods . . . . .	264
13.5	Distributed Approaches to Information Retrieval . . . . .	265
13.5.1	Current Research Issues . . . . .	266
13.6	Architecture . . . . .	267
13.6.1	Preliminaries . . . . .	267
13.6.2	Query Routing . . . . .	268
13.6.3	Cooperative Caching . . . . .	268
13.6.4	Simulation Results . . . . .	269
13.6.5	Implementation . . . . .	272
13.7	Concluding Remarks . . . . .	276
<b>14</b>	<b>Efficient Parallel Recovery in Replicated Databases</b> . . . . .	<b>277</b>
	by R. Tewari	
14.1	Introduction . . . . .	277
14.2	Consistency Control Algorithm . . . . .	278
14.3	Parallel Merge Protocol . . . . .	279
14.4	Extension of the Parallel Merge Protocol . . . . .	285
14.5	Incorporating Parallelism in the Merge Protocol . . . . .	285
14.6	Performance Analysis of the Parallel Merge Algorithm . . . . .	286
14.7	Conclusion . . . . .	287

<b>15 Document Allocation in Multiprocessor Information Retrieval Systems</b>	<b>289</b>
by H.T. Siegelmann, O. Frieder	
15.1 Introduction . . . . .	289
15.2 MDAP is NP-Complete . . . . .	290
15.3 Related Efforts . . . . .	292
15.3.1 Previous Approximations of the Mapping Problem . . . . .	293
15.3.2 Related Information Retrieval Systems . . . . .	293
15.4 A Genetic Algorithm for MDAP . . . . .	294
15.5 Theoretical Foundations . . . . .	298
15.6 Experimental Evaluation . . . . .	301
15.7 Conclusions and Future Directions . . . . .	309
<b>IV Heterogeneity/Interoperability/Open System Architectures/Multimedia Database Systems</b>	<b>311</b>
<b>16 Amalgame: A Tool for Creating Interoperating, Persistent, Heterogeneous Components</b>	<b>313</b>
by J.-C. Franchitti, R. King	
16.1 Introduction . . . . .	313
16.1.1 The Persistent and Heterogeneous Applications . . . . .	313
16.1.2 Goals and Novelty of the Amalgame System . . . . .	316
16.2 Related Work . . . . .	316
16.2.1 Interoperability Support . . . . .	316
16.2.2 Architectural Representation Languages and Megaprogramming . . . . .	317
16.2.3 Extensible Reusable Heterogeneous Frameworks . . . . .	318
16.3 An Overview of Amalgame . . . . .	318
16.3.1 A Motivating Example . . . . .	318
16.3.2 The Designer's View of the Amalgame Toolkit . . . . .	319
16.3.3 Practical Use of the Amalgame Toolkit . . . . .	320
16.3.4 The Internal Architecture of the Amalgame Toolkit . . . . .	325
16.4 An Arcadia Demonstration Scenario . . . . .	330
16.4.1 High-level Description of the Arcadia Experiment . . . . .	330
16.4.2 Implementation . . . . .	331
16.4.3 Benefits of The Amalgame Approach . . . . .	332
16.5 Future Directions . . . . .	333
16.5.1 A Joint Arcadia and Prototech Demonstration Scenario . . . . .	333
16.5.2 An Interoperability Experiment with Chiron . . . . .	333
16.5.3 An International "Library" of Deployed "Wrapped" Persistent Applications . . . . .	334
16.6 Conclusion . . . . .	334
16.7 Acknowledgments . . . . .	334

<b>17 Correctness and Enforcement of Multidatabase Interdependencies</b>	<b>337</b>
by G. Karabatis, M. Rusinkiewicz, A. Sheth	
17.1 Introduction . . . . .	337
17.2 Background . . . . .	338
17.2.1 Specification of Interdependent Data . . . . .	338
17.2.2 Conceptual System Architecture . . . . .	340
17.3 Correctness of Dependency Specifications . . . . .	341
17.3.1 Dependency Graph . . . . .	341
17.3.2 Correctness Requirements Involving Consistency Predicates	343
17.3.3 Correctness Requirements Involving Dependency Predicates	344
17.4 Polytransactions . . . . .	345
17.5 Consistency of Interdependent Data . . . . .	348
17.5.1 States of Interdependent Data Objects . . . . .	348
17.5.2 Measures of Consistency . . . . .	349
17.5.3 Updatability of Objects . . . . .	351
17.6 Concurrent Execution of Polytransactions . . . . .	353
17.6.1 Correctness of the Execution of a Single Polytransaction .	353
17.6.2 Conflicts in Polytransactions . . . . .	354
17.6.3 Polytransactions with Temporal Constraints . . . . .	356
17.7 Conclusion . . . . .	357
<b>18 FEMUS: A Federated Multilingual Database System</b>	<b>359</b>
by M. Andersson, Y. Dupont, S. Spaccapietra, K. Yétongnon, M. Tresch, H. Ye	
18.1 Introduction . . . . .	359
18.2 FEMUS . . . . .	360
18.2.1 The ERC+ Approach . . . . .	361
18.2.2 The COCOON Approach . . . . .	362
18.3 The Mapping Process . . . . .	365
18.3.1 Mapping an ERC+ Schema to COCOON . . . . .	366
18.3.2 Mapping a COCOON Schema to ERC+ . . . . .	368
18.3.3 Operators Mapping . . . . .	369
18.4 The Integration Process . . . . .	371
18.4.1 Assertion-driven Integration . . . . .	374
18.4.2 Integration Through Augmentation . . . . .	375
18.5 Negotiation . . . . .	376
18.5.1 Exchanging Metadata . . . . .	376
18.5.2 Exchanging Data . . . . .	377
18.6 Implementation Issues . . . . .	377
18.7 Consistency Requirement . . . . .	378
18.7.1 Detection of Relevant Updates . . . . .	378
18.7.2 Differential Refresh . . . . .	379
18.8 Conclusion and Future Research . . . . .	380

<b>19 Communication and Synchronization Issues in Distributed Multimedia Database Systems</b>	<b>381</b>
by <b>S. Browne</b>	
19.1 Introduction . . . . .	381
19.2 Characteristics and Requirements . . . . .	383
19.3 Communication Approaches . . . . .	385
19.4 Synchronization Approaches . . . . .	388
19.5 Conclusions . . . . .	395
<b>20 Multimedia Database Systems</b>	<b>397</b>
by <b>A. Ghafoor, P.B. Berra</b>	
20.1 Introduction . . . . .	397
20.2 Characteristics of Multimedia Data . . . . .	398
20.2.1 Text and Formatted Data . . . . .	398
20.2.2 Audio and Music Data . . . . .	398
20.2.3 Images and Pictures Data . . . . .	398
20.2.4 Full-Motion Video Data . . . . .	399
20.3 Notion of Time for Multimedia Data . . . . .	399
20.3.1 The Temporal Synchronization Problem . . . . .	399
20.3.2 Modeling Time . . . . .	401
20.4 Conceptual Models for Multimedia Objects . . . . .	402
20.4.1 Graphical Models . . . . .	402
20.4.2 Petri-Net Models . . . . .	403
20.4.3 Object-Oriented Models . . . . .	404
20.4.4 Language Based Models . . . . .	405
20.4.5 Temporal Abstraction Models . . . . .	405
20.4.6 Database Models for Multimedia Synchronization . . . . .	406
20.5 Some Multimedia Database Systems . . . . .	407
20.5.1 Image Database . . . . .	407
20.5.2 Audio Database . . . . .	409
20.6 Challenges in Multimedia Database . . . . .	410
20.7 Conclusion . . . . .	411
<b>Bibliography</b>	<b>413</b>

**Part I**

**Object-Oriented Databases**



# Chapter 1

## COMPOSE: A System For Composite Specification And Detection

Narain Gehani\*, H. V. Jagadish†, O. Shmueli‡

### 1.1 Introduction

An “event” is a happening of interest. Events can be simple such as, the stock price going above a certain price, the beginning of a transaction, the update of an object, or the temperature going above a specified limit. New events can also be formed as a combination of other events, for example, three successive discount rate cuts without an intervening increase, all withdrawals following a large deposit, and the temperature going above a specified limit and staying there for more than some time period. We call such events “composite events”.

We have developed a model for specifying composite events [216, 215]. We were motivated to explore the specification of composite events as part of an effort to design “trigger” facilities for the Ode object database [7, 217]. Triggers are the key facility that distinguishes active databases [138, 524, 40, 378, 556, 395] from passive databases. A trigger consists of an event-action pair. When an event is detected, the associated action is executed.

The use of triggers moves code from the application to the database. This simplifies application writing because the application now does not have to check for the conditions specified by the triggers. Triggers also eliminate duplicate code since the same conditions may have to be checked in multiple applications.

A trigger facility in which triggers fire on the occurrence of composite events is more powerful than one in which triggers fire on the occurrence of simple events because it allows users to write triggers that could not be easily expressed before. Composite event specification is useful for many application domains besides databases:

1. Financial Applications: Trades can be executed in response to an observed pattern of (trading) events in a stock market.

---

\*AT&T Bell Laboratories

†AT&T Bell Laboratories

‡AT&T Bell Laboratories and Technion -Israel Institute of Technology

2. Fraud Detection: Particular sequences of credit card purchases may point to fraudulent use.
3. Production Management: Particular sequences of defects could indicate difficulties that must be brought to the attention of a supervisor.

Composite events are specified as event expressions. Our basic notation for specifying composite events has the same expressive power as regular expressions. Thus the occurrence of a composite event is detected by a finite automaton that implements the event expression. Despite the equivalence of expressive power, our notation is specially suited for specifying composite events. For example, it allows for the easy specification of composite events whose components can overlap and allows uninteresting events to be screened out.

We extend our basic notation with “masks”, correlation variables, and parameters, thereby stepping beyond the domain of regular expressions. However, we can still implement event expressions that use these facilities by using automata augmented with “mask” events and by using “generic” automata. This allows us to use finite automata optimization techniques to generate efficient implementations for recognizing the occurrence of composite events.

We have built a prototype system, COMPOSE, for specifying and detecting composite events. A real-time stock trade feed is used to experiment with specifying and detecting stock market related events.

In this chapter, we describe how composite events are specified, illustrate composite event specification, give an overview of COMPOSE, and describe the construction of the finite automata.

## 1.2 Event Expressions

Primitive events are events that are known to or supported by the database system. Examples of some primitive events, in object-oriented databases [215], are object manipulation actions such as creation, deletion, and update or access by an object method (member function). Events can be specified to happen just prior to or just after the above actions. In addition, events can be associated with transactions and specified to happen immediately after a transaction begins, immediately before a transaction attempts to commit, immediately after a transaction commits, immediately before a transaction aborts, and immediately after a transaction aborts. Examples of other events are time events such as clock ticks, the passage of a day, an hour, a second, or some other time unit. Finally, stock trades and the raising or lowering of interest rates are examples of financial events, and company announcements are examples of news events.

Composite events are specified as event expressions. An *event expression* can be *NULL*, any primitive event *a*, or an expression formed using the basic operators  $\wedge$ ,  $!$  (not), *relative* and *relative+*.

Formally, event expressions are mappings from *histories* (sequences of primitive events) to histories:

$$E : \text{histories} \rightarrow \text{histories}$$

The result of applying an expression *E* to a history *h*, which is also a history, is denoted by  $E[h]$ .

Here are the semantics of some simple event expressions:

1.  $E[\text{null}] = \text{null}$  for any event  $E$ , where  $\text{null}$  is the empty history.
2.  $\text{NULL}[h] = \text{null}$ .
3.  $a[h]$ , where  $a$  is a primitive event, is the maximal subset of  $h$  composed of all event occurrences of the symbol  $a$ .

### 1.2.1 Basic Operators

Let  $E$  and  $F$  denote event expressions and  $h, h_1, h_2$  denote event histories. Here are the semantics of expressions formed using the basic operators:

1.  $(E \wedge F)[h] = h_1 \cap h_2$  where  $h_1 = E[h]$  and  $h_2 = F[h]$ .
2.  $(!E)[h] = (h - E[h])$ .
3.  $\text{relative}(E, F)[h]$  are the event occurrences in  $h$  at which  $F$  is satisfied assuming that the history started immediately following *some* event occurrence in  $h$  at which  $E$  takes place.

Formally,  $\text{relative}(E, F)[h]$  is defined as follows. Let  $E^i[h]$  be the  $i^{\text{th}}$  event occurrences in  $E[h]$ ; let  $h_i$  be obtained from  $h$  by deleting all event occurrences before  $E^i[h]$ . Then  $\text{relative}(E, F)[h] = \bigcup_{i=1}^{E[h]} F[h_i]$ .

4.  $\text{relative} + (E)[h] = \bigcup_{i=1}^{\infty} \text{relative}^i(E)[h]$  where  $\text{relative}^1(E) = E$  and  $\text{relative}^i(E) = \text{relative}(\text{relative}^{i-1}(E), E)$ .

### 1.2.2 Additional Operators

Besides the basic operators, we provide some additional operators that make composite events easier to specify. These operators do not add to the expressive power provided by the basic operators. Consequently, they can be defined in terms of the basic operators.

Let  $h$  denote a non-null history, and  $E, F$ , and  $E_i$  denote event expressions. The new operators are

1.  $E \vee F = !(E \wedge !F)$ .
2. *any* denotes the disjunction of all the primitive events.
3.  $\text{prior}(E, F)$  specifies that an event  $F$  that takes place after an event  $E$  has taken place.  $E$  and  $F$  may overlap. Formally,  $\text{prior}(E, F) = \text{relative}(E, \text{any}) \wedge F$ .
4.  $\text{prior}(E_1, \dots, E_m)$  specifies occurrences, in order, of the events  $E_1, E_2, \dots, E_m$ .  $\text{prior}(E_1, \dots, E_m) = \text{prior}(\text{prior}(E_1, \dots, E_{m-1}), E_m)$ .
5.  $\text{sequence}(E_1, \dots, E_m)$  specifies immediately successive occurrences of the events  $E_1, E_2, \dots, E_m$ :
  - (a)  $\text{sequence}(E_1, \dots, E_m) = \text{sequence}(\text{sequence}(E_1, \dots, E_{m-1}), E_m)$ .
  - (b)  $\text{sequence}(E_1, E_2) = \text{relative}(E_1, !( \text{relative}(\text{any}, \text{any}) )) \wedge E_2$ .

The first operand of the conjunction specifies the first event following event  $E_1$ . The second operand specifies that the event specified by the complete event expression must satisfy  $E_2$ .

6. *first* identifies the first event in a history.  $\text{first} = !\text{relative}(\text{any}, \text{any})$ .