ATOMIC ENERGY LEVELS and GROTRIAN DIAGRAMS

Volume I. Hydrogen I - Phosphorus XV

Stanley Bashkin and John O. Stoner, Jr.

ATOMIC ENERGY LEVELS and GROTRIAN DIAGRAMS

Volume I. Hydrogen I - Phosphorus XV

Stanley Bashkin and John O. Stoner, Jr.

Department of Physics, University of Arizona, Tucson, Arizona 85721



1975

NORTH-HOLLAND PUBLISHING COMPANY - AMSTERDAM. OXFORD AMERICAN ELSEVIER PUBLISHING COMPANY, INC. - NEW YORK

© North-Holland Publishing Company - 1975.

All rights reserved. No part of this publication may be reproduced, stored in retrieval system, or transmitted, in any form of by any means, electronic, mechanical, photocopying, recording or otherwise, without the prior permission of the copyright owner.

North_oHolland ISBN: 0 7204 0322 7 American Elsevier ISBN: 0 444 10827 0

Published by:

North-Holland Publishing Company - Amsterdam North-Holland Publishing Company, Ltd. - Oxford

Sole distributors for the U.S.A. and Canada:

American Elsevier Publishing Company, Inc. 52 Vanderbilt Avenue
New York, N.Y. 10017

INTRODUCTION

Energy-level and transition diagrams have been indispensable since their first appearance in the literature of atomic structure. The pioneering work by Grotrian was so important that his name has since been associated with pictorial representations of electronic transitions. In the years following the publication of Grotrian's books, the growth of information was so rapid that subsequent compilations were restricted to special cases, such as transitions of interest to astrophysics, or transitions within a given range of wavelengths. However, our own experience suggested that a collation of all present information concerning electronic transitions in monatomic systems would be useful to the scientific community, and we have attempted to make such a collation.

Despite our concern with the entire area of atomic spectroscopy, we have found it necessary to exclude certain parts from our compilation. Thus we have largely neglected hyperfine effects, radio-frequency spectroscopy, and inner-shell transitions. We have used principally the information contained in the energy-level compilations by Moore ² and Kelly,³ the spectral data in the publications by Kelly and Palumbo ⁴ and by Striganov and Sventitskii,⁵ and a small number of papers not summarized in the foregoing works.

DIAGRAMS

The diagrams are of two kinds. One shows the energy levels, the other the electronic transitions and associated wavelengths.

a) Energy-Level Diagrams

The general format of these diagrams is quite standard — a level is represented by a short, horizontal line which is located by two coordinates. The ordinate is the level's energy, always given in inverse cm, and the abscissa indicates some combination of quantum numbers. With the exception of some hydrogenic and helium-like systems, the levels' energies are derived strictly from experimental spectra.

Preparation of these diagrams was hampered by the fact that there are numerous cases where different authors give different quantum numbers for the same level. We have simply used the values compiled by Kelly 3 and kindly supplied by him from his unpublished work. In a few instances, Kelly himself lists two or more values for a given level. Here we have either taken the most recent data, or we have indicated by, "*see Kelly", that a unique value has not yet been determined.

For the abscissa, we have used familiar combinations of spin and orbital angular momenta, in most cases, taking the final designation given by Kelly³ with a certain exception noted below. In a number of systems, there are discrepancies between the designations listed by Kelly³ and those used by Striganov and Sventitskii.⁵ For example, in Si I, Kelly describes many levels in terms of j,l or j,j coupling, whereas the other authors use LS coupling. We have followed Kelly and have transposed the designations of Ref. 5 into those given by Kelly.

The exception mentioned above is that we have adopted the "primed" symbols in Moore's tables,² whereas Kelly omits primes entirely. Sometimes Ref. 5 uses primes which do not conform to the pattern followed by Moore; we have used Moore's notation.

It became apparent with our first diagrams that the variety of levels is so great that no single format can serve to represent all of them. It was also clear that some level systems are too densely packed to permit inclusion of all the data. We have tried to exhibit each system

according to a format which seems best for it, sometimes avoiding any redundancy, and sometimes deliberately including duplicate information, so as to give a clear picture. When level densities are inconveniently high, we have indicated the topmost level and one or two below until the density is at such a value that all the lower levels can be shown. The level energy as derived from experiment is given to the full precision with which it is listed in the literature. However, some of the calculated levels are given with less precision than is stated in the original source.

In many ions, a number of different core configurations produce similar final configurations. Often a single diagram suffices for displaying all the levels, but there are also instances where each core contributes so many different configurations that each core is given a separate diagram. The cores are then indicated in the title and corner labels for the diagrams. Where different cores occur, they have been specifically defined on the diagrams.

Each level diagram contains a key which defines the various symbols. We include, as well, information on the ionization level, taken from Ref. 4, and the ground configurations of the ion and the next higher ion. The j,l and j,j intermediate coupling schemes are represented by different brackets, namely, [] and {}, respectively. All level listings are in order of increasing excitation, and all j-values are in order of increasing excitation. When intermediate coupling occurs, the intermediate-coupling angular momenta are shown in a vertical array, again, in order of increasing excitation, from bottom to top. While j-values are shown inside parentheses, we had to account for the fact that sometimes a single energy is listed for two or more different values of j. For example, the 3d ⁴D term of Na V is listed as:

which means that the lower number is common to the first two j-values and the upper number belongs to j = 1/2.

The ionization level is shown as a horizontal dashed line. The ionization level is simply the energy difference between the ground term and the bottom of the continuum for the terms having the ground-term core.

b) Grotrian Diagrams

Diagrams showing transitions from one spectroscopic term to another are called, "Grotrian Diagrams". We have shown most of the transitions listed by Kelly and Palumbo⁴ and by Striganov and Sventitskii, ⁵ as well as a few others taken from more recent publications. Sometimes the line density is too great for every line to be drawn with clarity. In such cases, we have shown the line of shortest wavelength, and as many of the others as could be done conveniently. The decision as to what to omit was arbitrary. In a number of instances, the Grotrian diagram was divided into two or more. In most instances, but not all, the same energy scale has been used for the Grotrian and energy-level diagrams.

The precision with which wavelengths have been measured is often gratifyingly high, but it was impossible to incorporate the full precision into our pictures. We have usually given wavelengths with one significant figure less than that in the literature, but there are a few cases, especially for systems drawn in the early days of this project, where all decimals have been omitted. When there are two lines in a multiplet, two numbers are given, separated by a comma; when there are more than two lines, the extreme wavelengths are given, separated by a dash. Wavelengths are in vacuum for values shorter than 2000 Å, and in air for longer values.

FUTURE WORK

We are extending the present work into the elements of higher atomic number. Drawings for the second volume are now in preparation. In addition, we hope to make revisions of the present drawings as corrections, new information, and other improvements are brought to our attention. We look forward to receiving comments from the scientific community.

SOURCES

The bibliography which is given for each stage of ionization is to be taken as an addition to the general references which are listed below. For those stages of ionization for which no bibliography appears, the information was taken entirely from the following references. Occasionally, a research paper has been identified on a particular energy-level or Grotrian diagram.

The general references are:

- 1. W. Grotrian, Graphische Darstellung der Spektren, J. Springer (Berlin 1928).
- 2. C.E. Moore, *Atomic Energy Levels*, Circular 467, National Bureau of Standards, Vol. 1 (1949), reprinted as NSRDS-NBS 35, Vol. 1.
- 3. R.L. Kelly, Tabulation of Energy Levels for Atoms and Ions, unpublished.
- 4. R.L. Kelly and L.J. Palumbo, Atomic and Ionic Emission Lines Below 2000 Angstroms, Hydrogen Through Krypton, (U.S. Govt. Printing Office, Washington, D.C., Stock No. 0851-00061, 1973).
- 5. A.R. Striganov and N.S. Sventitskii, *Tables of Spectral Lines of Neutral and Ionized Atoms*, IFI/Plenum (New York, 1968).
- 6. C.E. Moore and P.W. Merrill, Partial Grotrian Diagrams of Astrophysical Interest, Appendix A of Lines of the Chemical Elements in Astronomical Spectra, (Carnegie Institution of Washington Publication 610, 1958 reprinted as NSRDS-NBS-23).

ACKNOWLEDGEMENTS

Most of the drawing and much of the assembly of bibliographies were carried out by undergraduate students and drafting assistants, nearly all of them as part-time helpers. Chief among those who had significant responsibility for the final preparation of the drawings were Christopher Hogg, John Howe, and Frank Ripley. Others in the group included: D. Abels, R. Bright, F. Camacho, A. Carlin, J. Enz, M. Ferrer, M. Gizzi, S. Heising, E. Ikeda, R. Johnson, E. Jones, G. Lim, B. Littlefield, R. Lundin, E. Meinel, R. Sherry, J. Slightom, W. Tilton, D. Toy, G. Westland, P. Wittman, R. Wong, The cover was designed by J. Howe.

We owe special thanks to the many investigators who sent us line lists and partial diagrams, often in advance of publication. Our debt to Dr. Raymond Kelly in this respect is large indeed. Useful suggestions were also received from W.S. Bickel, J.D. Garcia, J.A. Leavitt, W.C. Martin, L.J. Radziemski, Jr., and others. All of the secretarial work was done by Mrs. Lois Davis. Financial support was received from the U.S. Air Force, NASA, ONR, and NSF.

List of Illustrations

Please note that there has been some deliberate duplication of energy level and Grotrian diagrams. This has been done especially when the transitions have been divided among a number of Grotrian diagrams, for this arrangement permits one to see the level scheme that is appropriate for each of the Grotrian diagrams. In one case in N IV it was found convenient to use separate drawings for the singlet energy levels but one Grotrian diagram. Consequently, that Grotrian diagram appears twice.

ΗI	Grotrian Diagram. Doublets.		2
	Energy Levels. Doublets.	•	3.
	Energy Levels. Fine Structure, Hyperfine Structure, Lamb S	hifts, $n = 1, 2, 3, 4$.	5
He I	Grotrian Diagram. Singlets and Triplets.		8
	Energy Levels. Singlets and Triplets.		9
•	Grotrian Diagram. Doubly-Excited Singlets and Triplets.		. 10
٠.	Energy Levels. Doubly-Excited Singlets and Triplets.		11
He II	Grotrian Diagram. Doublets.		12
•	Energy Levels. Doublets.	•	13
Li I	Grotrian Diagram. Doublets.		16
	Energy Levels. Doublets.		17
	Grotrian Diagram. Doubly-Excited Quartets.		18
•	Energy Levels. Doubly-Excited Quartets.		19
Li II	Grotrian Diagram. Singlets and Triplets.		20
	Energy Levels. Singlets and Triplets.	,	21
Li III	Grotrian Diagram. Doublets.		22
	Energy Levels. Doublets.		23
Be I	Grotrian Diagram. Singlets.		28
	Energy Levels. Singlets.		29
	Grotrian Diagram. Triplets.	•	30
	Energy Levels. Triplets.		31
Be II	Grotrian Diagram. Doublets.		32
	Energy Levels. Doublets.		33
	Grotrian Diagram. Doubly-Excited Quartets.		34
	Energy Levels. Doubly-Excited Quartets		35
Be III	Grotrian Diagram. Singlets and Triplets.		36
	Energy Levels. Singlets and Triplets.		37
Be IV	Grotrian Diagram. Doublets.		38
	Energy Levels. Doublets.		39
BI.	Grotrian Diagram. Doublets and Quartets.		42
	Energy Levels. Doublets and Quartets.		43
BII	Grotrian Diagram. Singlets.		44
	Energy Levels. Singlets.		45
	Grotrian Diagram. Triplets.		46
	Energy Levels. Triplets.		47
B III	Grotrian Diagram. Doublets.		48
	Energy Levels. Doublets.		49
B IV	Grotrian Diagram. Singlets and Triplets:		50
	Energy Levels. Singlets and Triplets.		- 51
ΒV	Grotrian Diagram. Doublets.		. 52
	Energy Levels. Doublets.		53

CI	Grotrian Diagram, Singlets.	56
	Energy Levels. Singlets	57
	Grotrian Diagram. Triplets and Quintets. Transitions from the Ground Term to	58
	Excited Triplets and Quintets.	,
	Energy Levels. Triplets and Quintets.	59
	Grotrian Diagram. Triplets and Quintets. Transitions from 3s ³ P ^o , 2s 2p ³ ³ D ^o , and 3p ³ D to Higher Triplets: Quintet—Quintet Transitions.	. 60
	Energy Levels. Triplets and Quintets.	61
	Grotrian Diagram. Triplets. Transitions from 2s ² 2p 3p ³ S, 2s ² 2p 3p ³ P, and 2s 2p ³ 3P° to Higher Triplets.	62
	Energy Levels. Triplets and Quintets.	63
	Energy Levels. Intermediate Coupling and Autoionizing Terms.	65
	Grotrian Diagram. Intercombinations. Transitions between Singlets and Triplets.	66
	Grotrian Diagram. Intercombinations. Transitions between Singlets and Intermediate-Coupling Terms.	68
	Grotrian Diagram. Intercombinations. Transitions from the Ground Term to Excit-	70
	ed Singlets and Quintets.	
	Grotrian Diagram, Intercombinations, Transitions between Excited Triplet Terms	72
c	and Higher Singlets and Intermediate-Coupling Terms,	-
C II	Grotrian Diagram. Doublets.	74
	Energy Levels. Doublets.	75
	Grotrian Diagram. Quartets.	76
	Energy Levels. Quartets.	77
	Grotrian Diagram. Intercombinations. Transitions between Doublets and Quartets.	78
C III	Grotrian Diagram, Singlets.	. 80
	Energy Levels. Singlets.	≒ 81
	Grotrian Diagram. Triplets, 1s ² 2s nl Terms.	82
,	Energy levels. Triplets, 1s ² 2s nl Terms.	83
	Grotrian Diagram. Triplets, 1s ² 2p nl Terms.	84
	Energy Levels. Triplets, 1s ² 2p nl Terms.	85
	Grotrian Diagram. Intercombinations. Transitions between 1s ² 2s nl Triplets and 1s ² 2p nl Triplets.	86
C IV	Grotrian Diagram. Doublets.	88
	Energy Levels. Doublets.	89
	Grotrian Diagram, Doubly-Excited Quartets,	90
	Energy Levels. Doubly-Excited Quartets.	91
C V	Grotrian Diagram, Singlets.	92
•	Energy Levels. Singlets.	93
	Grotrian Diagram, Triplets.	94
	Energy Levels. Triplets.	95
CVI	Grotrian Diagram. Doublets.	96
	Energy Levels. Doublets.	97
	•	•
N I	Grotrian Diagram. Doublets. Transitions from 2p 2D° to Higher Doublets.	100
	Energy Levels, Doublets.	. 🐪 , 101
	Grotrian Diagram, Doublets, Transitions from 2p 2P° to Higher Doublets.	102
	Energy Levels. Doublets.	103
•	Grotrian Diagram. Doublets. Transitions from Doublets with $n = 3$ to Higher Doublets.	` _{_} 104
-	Energy Levels. Doublets.	105
	Grotrian Diagram. Quartets and Sextets.	106
	Energy Levels, Quartets and Sextets.	107
		107
	Energy Levels. Intermediate Coupling.	110
	Grotrian Diagram. Intercombinations. Transitions from Doublets to Quartets.	110
	Grotrian Diagram, Intercombinations, Transitions from Quartets to Doublets. Grotrian Diagram, Intercombinations, Transitions from Doublets and Quartets to	114
	Intermediate Coupling Terms	

N II	Grotrian Diagram. Singlets.	116
•	Energy Levels. Singlets.	117
	Grotrian Diagram. Triplets.	118
	Energy Levels. Triplets.	119
	Grotrian Diagram. Quintets.	120
	Energy Levels. Quintets.	121
	Grotrian Diagram. Intermediate Coupling.	122
	Energy Levels. Intermediate Coupling.	123
	Grotrian Diagram. Intercombinations. Transitions from Singlets to Triplets.	124
	Grotrian Diagram. Intercombinations. Transitions from Singlets to Intermediate- Coupling Terms.	126
	Grotrian Diagram. Intercombinations. Transitions from Triplets to Singlets.	128
	Grotrian Diagram. Intercombinations. Transitions from Triplets to Quintets and Intermediate-Coupling Terms.	130
N III	Grotrian Diagram. Doublets.	132
	Energy Levels. Doublets.	133
	Grotrian Diagram. Quartets.	134
•	Energy Levels. Quartets.	135
	Grotrian Diagram. Intercombinations. Transitions between Doublets and Quartets.	136
N IV	Grotrian Diagram. Singlets. Both 1s ² 2s nl Terms and 1s ² 2p nl Terms.	138
	Energy Levels. Singlets, 1s ² 2s nl Terms.	139
٠.	Grotrian Diagram. Singlets. Both 1s ² 2s nl Terms and 1s ² 2p nl Terms.	140
	Energy Levels. Singlets, 1s ² 2p nl Terms.	141
•	Grotrian Diagram. Triplets. Transitions between 1s ² 2s nl Terms.	142
	Energy Levels. Triplets, 1s ² 2s nl Terms.	143
	Grotrian Diagram. Triplets. Transitions between 1s ² 2p nl Terms.	144
	Energy Levels. Triplets, 1s ² 2p nl Terms.	145
• •	Grotrian Diagram. Intercombinations. Transitions between 1s ² 2s nl Triplet Terms and 1s ² 2p nl Triplet Terms.	146
NV	Grotrian Diagram. Doublets.	148
• • •	Energy Levels. Doublets.	149
N VI	Grotrian Diagram. Singlets and Triplets.	150
	Energy Levels. Singlets and Triplets.	151
N VII	Grotrian Diagram. Doublets.	152
	Energy Levels. Doublets.	153
10	Grotrian Diagram, Singlets.	158 159
	Energy Levels. Singlets.	160
	Grotrian Diagram. Triplets. Transitions between 1s ² 2s ² 2p ³ (² D°) nl Terms.	161
	Energy Levels. Triplets, 1s ² 2s ² 2p ³ (² D°) nl Terms. Grotrian Diagram and Energy Levels. Autoionizing Triplets, 1s ² 2s ² 2p ³ (² P°) nl Terms.	163
	Grotrian Diagram. Triplets and Quintets. Transitions between 1s ² 2s ² 2p ³ (⁴ S ^o) nl Terms.	164
•	Energy Levels. Triplets and Quintets. 1s ² 2s ² 2p ³ (*S°) nl Terms.	165
•	Grotrian Diagram. Intercombinations. Transitions between Triplets with (*S°), (3°P°), and (2°D°) Cores.	166
0 11	Grotrian Diagram. Doublets.	168
	Energy Levels. Doublets.	169
	Grotrian Diagram. Quartets.	170
	Energy Levels. Quartets.	171
	•=-	
	Grotrian Diagram, Sextets.	172
	Grotrian Diagram. Sextets. Energy Levels. Sextets.	172

O III	Grotrian Diagram. Singlets.	176
	Energy Levels. Singlets.	177
	Grotrian Diagram. Triplets.	178
	Energy Levels. Triplets.	179
	Grotrian Diagram, Quintets.	180
	Energy Levels. Quintets and Intermediate-Coupling Terms.	181
	Grotrian Diagram. Intercombinations. Transitions from Singlets to Higher Triplets and Intermediate-Coupling Terms.	182
	Grotrian Diagram. Intercombinations. Transitions from Triplets to Higher Singlets and Intermediate-Coupling Terms.	184
OIV	Grotrian Diagram. Doublets.	186
011		187
	Energy Levels. Doublets.	188
	Grotrian Diagram, Quartets.	189
ΩV	Energy Levels, Quartets.	190
OV	Grotrian Diagram. Singlets. Transitions between 1s ² 2s nl Terms.	191
	Energy Levels. Singlets, 1s ² 2s nl Terms.	192
	Grotrian Diagram. Singlets. Transitions between 1s ² 2p nl Terms.	193
	Energy Levels. Singlets, 1s ² 2p nl Terms.	194
	Grotrian Diagram. Triplets. Transitions between 1s ² 2s nl Terms.	195
	Energy Levels. Triplets, 1s ² 2s nl Terms.	196
	Grotrian Diagram. Triplets. Transitions between 1s ² 2p nl Terms.	190
٠.	Energy Levels. Triplets, 1s ² 2p nl Terms. Grotrian Diagram. Intercombinations. Transitions between 1s ² 2s nl Singlets and	198
	1s ² 2p nl Singlets. Grotrian Diagram. Intercombinations. Transitions between 1s ² 2s nl Triplet Terms	200
0.141	and 1s ² 2p nl Triplet Terms.	202
o vi	Grotrian Diagram. Doublets.	203
A	Energy Levels, Doublets.	204
O VII	Grotrian Diagram, Singlets and Triplets.	205
	Energy Levels. Singlets and Triplets.	206
O VIII	Grotrian Diagram. Doublets. Energy Levels. Doublets.	207
E 1	Creation Diagram Doublets	212
FI	Grotrian Diagram. Doublets. Energy Levels. Doublets.	213
		214
•	Grotrian Diagram, Quartets.	215
	Energy Levels. Quartets. Grotrian Diagram. Intercombinations. Transitions from Doublets to Higher Quar-	216
	tets. Grotrian Diagram. Intercombinations. Transitions from Quartets to Higher Doub-	218
r. 11	lets. Grotrian Diagram. Singlets. Transitions between 1s ² 2s ² 2p ³ (² P°) nl Terms.	220
FII	Energy Levels, Singlets, 1s ² 2s ² 2p ³ (² P ⁶) nl Terms.	221
	Grotrian Diagram. Singlets. Transitions between 1s ² 2s ² 2p ³ (² D°) nl Terms.	222
	Energy Levels. Singlets, 1s ² 2s ² 2p ³ (² D ⁶) nl Terms.	223
	Grotrian Diagram. Triplets. Transitions between 1s ² 2s ² 2p ³ (² P°) nl Terms.	224
	Energy Levels, Triplets, 1s ² 2s ² 2p ³ (² P°) nl Terms.	225
	Grotrian Diagram. Triplets. Transitions between 1s ² 2s ² 2p ³ (² D°) nl Terms.	226
	Energy Levels. Triplets, 1s ² 2s ² 2p ³ (² D°) nl Terms.	227
	Grotrian Diagram. Triplets. Transitions between 1s ² 2s ² 2p ³ (⁴ S°) nl Terms.	228
	Energy Levels, Triplets, 1s ² 2s ² 2p ³ (⁴ S°) nl Terms.	229
	Grotrian Diagram. Quintets.	230
	· · · · · · · · · · · · · · · · · · ·	231
	Energy Levels, Quintets. Energy Levels, Intermediate Coupling.	233
	Grotrian Diagram, Intercombinations, Transitions from Singlets to Higher Singlets	234
	and Triplets. Grotrian Diagram. Intercombinations. Transitions from Triplets and Quintets to Higher Singlets and Triplets.	236

F-III	Grotrian Diagram. Doublets. Transitions from 1s ² 2s ² 2p ³ Terms to Higher Doublets:	238
	Energy Levels. Doublets.	239
	Grotrian Diagram. Doublets. Transitions from 1s ² 2p ⁴ Terms to Higher Doublets.	240
	Energy Levels. Doublets, 1s ² 2s 2p ⁴ ² S and above.	241
	Grotrian Diagram. Doublets. Transitions between Excited Doublets Higher than 1s ² 2s ² 2p ² 3p ² D°.	242
•	Energy Levels. Doublets Higher than 1s ² 2s 2p ⁴ ² S.	243
	Grotrian Diagram. Quartets.	243
	Energy Levels. Quartets.	245
	Grotrian Diagram. Sextets.	246
	Energy Levels. Sextets, (5S°) Core, and Intermediate-Coupling Terms, (1L) Core.	247 247
	Energy Levels. Intermediate-Coupling Terms, (³ P) Core.	249
	Grotrian Diagram, Sextets and Intercombination Transitions Between Doublets and Quartets.	250
	Grotrian Diagram. Intercombinations. Transitions from Doublets to Higher Intermediate-Coupling Terms.	252
* .	Grotrian Diagram. Intercombinations. Transitions from Quartets to Higher Intermediate-Coupling Terms.	254
F IV	Grotrian Diagram. Singlets.	256
•	Energy Levels. Singlets.	257
	Grotrian Diagram, Transitions from the Two Lowest Triplets to Higher Triplets.	258
	Energy Levels, Triplets.	259
	Grotrian Diagram. Transitions between Excited Triplets Higher than the Second	260
	Term.	
	Energy Levels, Triplets.	261
	Grotrian Diagram. Quintets.	262
•	Energy Levels. Quintets and Intermediate Coupling.	263
•	Grotrian Diagram. Intercombinations. Transitions among Singlets, Triplets, and Intermediate-Coupling Terms.	264
FV,	Grotrian Diagram. Doublets.	266
	Energy Levels. Doublets.	267
	Grotrian Diagram. Quartets.	268
•	Energy Levels. Quartets.	269
FVI	Grotrian Diagram. Singlets.	270
	Energy Levels. Singlets.	271
	Grotrian Diagram, Triplets.	272
	Energy Levels. Triplets.	273
FVII	Grotrian Diagram. Doublets.	274
	Energy Levels. Doublets.	275
F VIII	Orotrian Diagram. Singlets and Triplets.	276
*	Energy Levels. Singlets and Triplets.	277
F IX	Grotrian Diagram. Doublets.	278
	Energy Levels. Doublets.	279
Ne I	Grotrian Diagram. Transitions from the Ground Term to Higher Terms.	284
	Energy Levels.	285
	Grotriar Diagram. Transitions from Two Lowest Excited Terms to Higher Terms.	286
	Energy Levels. Grottian Diagram Transitions from the Third Excited Term to Higher Terms	287
	Grotrian Diagram. Transitions from the Third Excited Term to Higher Terms.	288
•	Energy Levels. Grottian Diagram, Transitions from the Fourth Evoited Term to Higher Terms	289
	Grotrian Diagram. Transitions from the Fourth Excited Term to Higher Terms.	290
	Energy Levels. Gratian Diagram Transitions between Terms with n > 4	291
	Grotrian Diagram. Transitions between Terms with $n \ge 4$. Energy Levels.	292
	Energy Levels.	293

	Grotrian Diagram. High Intermediate Coupling.	294
	Energy Levels, High Intermediate Coupling.	295
	Grotrian Diagram. Doubly-Excited Terms. ³ P Core.	296
	Energy Levels. Doubly-Excited Terms.	297
	Grotrian Diagram. Doubly-Excited Terms. ¹ D, ¹ S Cores.	298
	Energy Levels. Doubly-Excited Terms.	299
Ne II	Grotrian Diagram. Doublets.	300
•	Energy Levels, Doublets.	301
	Grotrian Diagram, Quartets.	302
	Energy Levels, Quartets.	303
	Energy Levels, Intermediate-Coupling Terms.	305
	Grotrian Diagram. Intercombinations. Transitions from Doublets to Quartets.	. 306
	Grotrian Diagram. Intercombinations. Transitions from Quartets to Doublets and	308
•	Intermediate-Coupling Terms.	300
Ne III	Grotrian Diagram. Singlets and Quintets.	210
110 111	Energy Levels. Singlets and Quinters.	310
	Grotrian Diagram. Triplets.	311
	Energy Levels, Triplets.	312
Ne IV	· · · · · · · · · · · · · · · · · · ·	313
146 14	Grotrian Diagram. Doublets.	314
	Energy Levels, Doublets,	315
	Grotrian Diagram. Quartets and Sextets.	316
Ne V	Energy Levels. Quartets and Sextets.	317
	Grotrian Diagram. Singlets.	318
	Energy Levels. Singlets.	319
	Grotrian Diagram. Triplets.	320
•	Energy Levels. Triplets.	321
	Grotrian Diagram. Quintets.	322
Ne VI	Energy Levels. Quintets.	323
MC AT	Grotrian Diagram. Doublets.	324
	Energy Levels. Doublets.	325
	Grotrian Diagram. Quartets.	326
Ne VII	Energy Levels. Quartets.	327
INC A !!	Grotrian Diagram. Singlets.	328
	Energy Levels. Singlets.	329
•	Grotrian Diagram. Triplets.	330
NI. 12010	Energy Levels. Triplets.	331
Ne VIII	Grotrian Diagram. Doublets.	332
	Energy Levels. Doublets.	333
Ne IX	Grotrian Diagram. Singlets and Triplets.	334
	Energy Levels. Singlets and Triplets.	335
Ne X	Grotrian Diagram. Doublets.	336
,	Energy Levels. Doublets.	337
Na I	Grotrian Diagram. Doublets.	342
	Energy Levels. Doublets.	- 343
Na II	Grotrian Diagram. Transitions between Intermediate-Coupling Terms with ² P _{1/2}	344
-	Core.	
	Energy Levels. Intermediate-Coupling Terms with ${}^2P_{1/2}^{\circ}$ Core.	345
	Grotrian Diagram. Transitions between Intermediate-Coupling Terms with ² P _{3/2}	346
	Core.	
•	Energy Levels. Intermediate-Coupling Terms with ${}^2P_{3/2}^o$ Core.	347
	Grotrian Diagram. Intercombinations. Transitions between ${}^2P_{1/2}^{\circ}$ and ${}^2P_{3/2}^{\circ}$ Cores.	^ 348
Na III	Grotrian Diagram. Doublets.	350
	Energy Levels. Doublets.	351
	Grotrian Diagram. Quartets.	352
•	Energy Levels. Quartets.	353
	Grotrian Diagram. Intercombinations. Transitions between Doublets and Quartets.	354

Na IV	Grotrian Diagram, Singlets.	356
	Energy Levels. Singlets.	357
	Grotrian Diagram, Triplets.	358
	Energy Levels. Triplets.	359
Na V	Grotrian Diagram. Doublets.	360
	Energy Levels. Doublets.	361
	Grotrian Diagram. Quartets.	362
	Energy Levels. Quartets.	363
Na VI	Grotrian Diagram. Singlets.	•364
	Energy Levels. Singlets.	365
	Grotrian Diagram. Triplets.	366
	Energy Levels. Triplets.	367
•	Grotrian Diagram. Quintets.	368
	Energy Levels, Quintets.	369
Na VII	Grotrian Diagram. Doublets.	370
	Energy Levels. Doublets.	371
	Grotrian Diagram. Quartets.	372
	Energy Levels. Quartets.	373
Na VIII	Grotrian Diagram. Singlets.	374
	Energy Levels, Singlets.	375
	Grotrian Diagram, Triplets.	376
	Energy Levels, Triplets.	377
Na IX	Grotrian Diagram, Doublets.	378
,	Energy Levels. Doublets.	379
Na X	Grotrian Diagram. Singlets and Triplets.	380
	Energy Levels. Singlets and Triplets.	381
Na XI	Grotrian Diagram. Doublets.	382
	Energy Levels. Doublets.	. 383
Mg I	Grotrian Diagram. Singlets and Triplets.	388
	Energy Levels, Singlets and Triplets.	389
Mg II	Grotrian Diagram. Doublets.	390
•	Energy Levels. Doublets.	391
Mg III	Grotrian Diagram. Singlets and Triplets.	392
	Energy Levels. Singlets and Triplets.	393
	Grotrian Diagram. Transitions between Intermediate-Coupling Terms with ${}^2P_{1/2}^{\circ}$ Core.	394
	Energy Levels. Intermediate-Coupling Terms with ² P _{1/2} Core.	395
	Grotrian Diagram. Transitions between Intermediate-Coupling Terms with ² P _{3/2} Core.	396
	Energy Levels. Intermediate-Coupling Terms with ² P _{3/2} Core.	397
	Grotrian Diagram. Intercombinations. Transitions from Singlets to Intermediate- Coupling Terms.	398
	Grotrian Diagram. Intercombinations. Transitions from Triplets to Intermediate- Coupling Terms.	400
Mg IV	Grotrian Diagram. Doublets.	402
	Energy Levels, Doublets,	403
	Grotrian Diagram. Quartets.	404
	Energy Levels. Quartets.	405
	Grotrian Diagram. Intercombinations. Transitions between Doublets and Quartets.	406
Mg V	Grotrian Diagram. Singlets.	408
~	Energy Levels. Singlets.	409
	Grotrian Diagram. Triplets.	410
*	Energy Levels Triplets	411

Mg VI	Grotrian Diagram. Doublets.	412
_	Energy Levels. Doublets.	413
	Grotrian Diagram. Quartets.	414
	Energy Levels, Quartets.	415
Mg VII	Grotrian Diagram. Singlets.	416
,	Energy Levels. Singlets.	417
	Grotrian Diagram. Triplets.	418
	Energy Levels. Triplets.	419
	Grotrian Diagram. Quintets.	420
	Energy Levels, Quintets.	421
Mg VIII	Grotrian Diagram. Doublets.	422
	Energy Levels. Doublets.	423
	Grotrian Diagram. Quartets.	424
	Energy Levels. Quartets.	425
Mg IX	Grotrian Diagram. Singlets.	426
	Energy Levels, Singlets.	427
	Grotrian Diagram. Triplets.	428
•	Energy Levels, Triplets.	429
Mg X	Grotrian Diagram. Doublets.	430
6 /	Energy Levels. Doublets.	431
Mg XI	Grotrian Diagram. Singlets and Triplets.	432
	Energy Levels. Singlets and Triplets.	433
Mg XII	Grotrian Diagram. Doublets.	434
mg Att	Energy Levels, Doublets.	435
	Energy Edition, Doublets.	
Al I	Grotrian Diagram. Doublets and Quartets. Transitions from the Two Lowest Terms to Higher Terms.	440
	Energy Levels. Doublets and Quartets.	441
	Grotrian Diagram. Doublets and Quartets. Transitions from the Lowest Quartet to	. 442
	Higher Terms.	
	Energy Levels. Doublets and Quartets.	443
AI II	Grotrian Diagram. Singlets. Transitions from the Three Lowest Singlets to Higher Terms.	444
	Energy Levels, Singlets.	445
	Grotrian Diagram. Singlets. Transitions from Singlets with $n = 4$ to Higher Singlets.	446
	Energy Levels. Singlets.	447
	Grotrian Diagram. Singlets. Transitions from 3d 1 D and Terms with $n \ge 5$ to Higher	448
	Singlets.	
	Energy Levels. Singlets.	449
	Grotrian Diagram. Triplets. Transitions from the First, Second, and Fourth Lowest Triplets to Higher Triplets.	450
	Energy Levels, Triplets.	451
	Grotrian Diagram. Triplets. Transitions from 3p ³ P or Terms ≥ 4p ³ P ^o to Higher Terms.	452
	Energy Levels. Triplets.	453
Al III	Grotrian Diagram. Doublets.	454
	Energy Levels. Doublets.	455
AI IV	Grotrian Diagram. Intermediate-Coupling and Autoionizing Terms.	456
	Energy Levels. Intermediate-Coupling and Autoionizing Terms.	457
Al V	Grotrian Diagram. Doublets and Quartets.	458
•	Energy Levels. Doublets and Quartets.	459
Al VI	Grotrian Diagram. Singlets.	460
	Energy Levels, Singlets.	461
	Grotrian Diagram. Triplets.	462
	Energy Levels. Triplets.	463

Al VII	Grotrian Diagram. Doublets.	464
•	Energy Levels. Doublets.	465
	Grotrian Diagram. Quartets.	466
	Energy Levels. Quartets.	467
Al VIII	Grotrian Diagram. Singlets and Quintets.	468
	Energy Levels. Singlets and Quintets.	469
	Grotrian Diagram. Triplets.	470
	Energy Levels, Triplets.	471
Al IX	Grotrian Diagram. Doublets.	472
	Energy Levels. Doublets.	473
	Grotrian Diagram. Quartets.	474
	Energy Levels. Quartets.	475
Al X	Grotrian Diagram, Singlets.	476
Al A	Energy Levels. Singlets.	477
	Grotrian Diagram. Triplets.	478
	Energy Levels. Triplets.	479
Al XI	Grotrian Diagram. Doublets.	480
AI AI	Energy Levels. Doublets.	481
Al XII	Grotrian Diagram. Singlets and Triplets.	482
ALAII	Energy Levels. Singlets and Triplets.	483
A1 VIII	•••	484
Al XIII	Grotrian Diagram. Doublets.	
	Energy Levels. Doublets.	485
C: T	Contribution Discourse Civilian	400
Si I	Grotrian Diagram. Singlets.	490
•	Energy Levels. Singlets.	491
	Grotrian Diagram. Triplets and Quintets. Transitions from the Ground to Excited Terms.	492
	Energy Levels. Triplets and Quintets.	493
	Grotrian Diagram. Triplets and Quintets. Transitions between Excited Terms.	494
	Energy Levels. Triplets and Quintets.	495
	Energy Levels. Intermediate-Coupling Terms.	496
•	Grotrian Diagram. Intercombinations. Transitions from Singlets to Triplets.	498
	Grotrian Diagram. Intercombinations. Transitions from Singlets to Intermediate-Coupling Terms.	500
	Grotrian Diagram. Intercombinations. Transitions from Triplets to Singlets.	502
	Grotrian Diagram, Intercombinations, Transitions from Triplets to Intermediate-	504
	Coupling Terms.	
Si II	Grotrian Diagram. Doublets.	506
y	Energy Levels. Doublets.	507
	Grotrian Diagram. Quartets.	508
	Energy Levels, Quartets.	509
Si III	Grotrian Diagram. Singlets. Transitions from the Lowest Four Singlets to Higher Singlets.	510
•	Energy Levels, Singlets.	511
	Grotrian Diagram. Transitions from the 4s ¹ S Term to Higher Singlets.	512
	Energy Levels. Singlets,	. 513
	Grotrian Diagram. Triplets. Transitions from Triplets with $n = 3$ to Higher Triplets.	514
	Energy Levels, Triplets.	515
•	Grotrian Diagram. Triplets. Transitions between Triplets with $n \ge 4$.	516
- •	Energy Levels. Triplets.	517
	Grotrian Diagram. Intermediate-Coupling Terms.	518
	Energy Levels. Intermediate-Coupling Terms.	519
Si IV	Grotrian Diagram. Doublets.	520
	Energy Levels. Doublets.	521
Si V	Grotrian Diagram. Intermediate Coupling.	522
	Energy Levels, Intermediate Coupling.	523
***	Ziron Zorom, interingente combinite.	323

Si VI	Grotrian Diagram, Doublets.	524
	Energy Levels. Doublets.	525
	Energy Levels. Quartets.	527
Si VII	Grotrian Diagram. Singlets.	528
	Energy Levels, Singlets.	529
	Grotrian Diagram, Triplets.	530
	Energy Levels. Triplets.	531
e viii	Grotrian Diagram. Intercombinations. Transitions between Singlets and Triplets.	532
Si VIII	Grotrian Diagram. Doublets.	534
	Energy Levels, Doublets,	535
	Grotrian Diagram. Quartets.	536
	Fnergy Levels, Quartets,	537
Si IX	Grotrian Diagram. Singlets and Quintets.	538
	Energy Levels, Singlets and Quintets.	539
	Grotrian Diagram, Triplets.	540
	Fnergy Levels, Triplets,	541
St X	Grotrian Diagram, Doublets.	542
	Energy Levels. Doublets.	543
•	Grotrian Diagram, Quartets,	544
	Fnergy Levels, Quartets,	545
Si XI	Grotrian Diagram, Singlets.	546
	Energy Levels, Singlets,	547
	Grotrian Diagram, Triplets.	548
	Fnergy Levels. Triplets.	549
Si XII	Grotrian Diagram, Doublets,	550
.71 /411	Energy Levels, Doublets.	551
Si XIII	Grotrian Diagram. Singlets and Triplets.	552
OLAIH		553
Si XIV	Energy Levels, Singlets and Triplets,	
SUAIN	Grotrian Diagram. Doublets.	554
	Energy Levels, Doublets.	55,5
Ρĵ	Carlo Diagram D. 11	560
1. I	Grotrian Diagram. Doublets.	560
	Energy Levels, Doublets,	561
	Grotrian Diagram. Quartets.	562
•	Fnergy Levels. Quartets.	563
	Grotrian Diagram, Intercombinations, Transitions from Doublets to Quartets.	564
	Grotrian Diagram. Intercombinations. Transitions from Quartets to Doublets.	566
PH	Grotrian Diagram. Singlets and Quintets.	568
	Fnergy Levels. Singlets and Quintets.	569
	Grotrian Diagram, Triplets.	570
,	Energy Levels, Triplets.	571
	Grotrian Diagram. Intercombinations. Transitions between Singlets and Triplets.	572
PHI	Grotrian Diagrami, Doublets.	574
	Lnergy Levels, Doublets,	57#
	Grotrian Diagram. Quartets.	576
	Energy Levels. Quartets.	577
PIV .	Grotrian Diagram. Singlets.	578
	Energy Levels, Singlets.	579
	Grotrian Diagram, Triplets.	580
	Energy Levels, Triplets.	581
ν	Grotrian Diagram. Doublets.	582
. •	•	
VI -	Energy Levels, Doublets, Crattian Discourse Singlets Triplets and Intermediate Counting Torres	583
. V 1	Grotrian Diagram. Singlets, Triplets, and Intermediate-Coupling Terms.	584
5 1/11	Energy Levels, Singlets, Triplets, and Intermediate-Coupling Terms.	.585
⁹ VII	Grotrian Diagram. Doublets and Quartets.	586
	Energy Levels, Doublets and Quartets.	587

P VIII	Grotrian Diagram, Singlets.	588
٠,	Energy Levels. Singlets.	589
	Grotrian Diagram, Triplets.	590
	Energy Levels. Triplets.	59
PIX	Grotrian Diagram, Doublets.	59
	Energy Levels. Doublets.	59
	Grotrian Diagram, Quartets.	59-
	Energy Levels. Quartets.	59
PΧ	Grotrian Diagram, Singlets.	59
	Energy Levels. Singlets.	59
	Grotrian Diagram. Triplets.	59
	Energy Levels. Triplets.	59
	Grotrian Diagram. Quintets.	60
,	Energy Levels. Quintets.	60
P XI	Grotrian Diagram. Doublets.	60
	Energy Levels, Doublets.	60
	Grotrian Diagram. Quartets.	, 60
	Energy Levels. Quartets.	60
P XII	Grotrian Diagram. Singlets and Triplets.	60
	Energy Levels. Singlets and Triplets.	60
P XIII	Grotrian Diagram. Doublets.	60
	Energy Levels. Doublets.	60
P XIV	Grotrian Diagram, Singlets and Triplets.	61
	Energy Levels. Singlets and Triplets.	61
P XV	Grotrian Diagram. Doublets.	61
	Fnergy Levels Doublets	61