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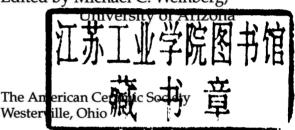
# Geramic transactions

NUCLEATION AND CRYSTALLIZATION IN LIQUIDS AND GLASSES Michael C. Weinberg

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NUCLEATION AND CRYSTALLIZATION IN LIQUIDS AND GLASSES

Edited by Michael C. Weinberg,



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# <u>preface</u>

The collection of papers presented herein were presented at the Nucleation and Crystallizaton symposium at the Glass and Optical Materials Division Meeting of the American Ceramic Society, held August 16-19, 1992, at Stone Mountain, GA.

This symposium was the fourth in a series held approximately every ten years. It was similar to the third symposium in that a combination of review and research papers were presented. The three major topics of this meeting were nucleation, crystallization, and crystallized glass applications, as in the third symposium.

On the other hand, the present meeting had certain distinct aspects that set it apart from previous symposia. First and foremost, there was the participation of a number of scientists and engineers from diverse disciplines, such as ceramic engineering, theoretical and experimental chemistry, metallurgy, astrophysics, and glass and polymer science. Second, the outlook was somewhat broader than in previous symposia, especially with regard to the topic of nucleation. Finally, on the last day of the meeting, a panel discussion was held on the topic of nucleation. During this session, assessments were given of the experimental and theoretical triumphs and deficiencies regarding crystal nucleation from the melt.

I am grateful to all of the authors for their wonderful cooperation in the preparation of this volume. In addition, I wish to extend special gratitude to Professors D.R. Uhlmann, K. Kelton, I. Gutzow, D. Oxtoby, P. James, and J. Perepezko for their insightful contributions. I extend special gratitude to the sponsors of this symposium: the Division of Microgravity Sciences and Applications of the National Aeronautics and Space Administration, Corning Incorporated, and Heraeus Amersil. Finally, I wish to thank Lori Kozey, of the American Ceramic Society, for her help and guidance.

Michael C. Weinberg

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# Section I. Nucleation

## EXPERIMENTAL STUDIES OF CRYSTAL NUCLEATION IN GLASSES

PF James Department of Engineering Materials, University of Sheffield, UK

## **ABSTRACT**

Recent studies of nucleation kinetics in oxide glasses are briefly discussed, including the following topics; Volume and surface nucleation, trends in homogeneous nucleation in stoichiometric compositions, nucleating agents in silicate and phosphate systems, and nucleation in melt-derived and sol-gel derived glasses.

#### INTRODUCTION

Nucleation and growth govern the glass forming tendencies of melts and so are of practical importance in the manufacture of a wide range of stable glass compositions. These processes are also essential steps in the conversion of glasses into fine grain crystalline glass-ceramics, materials with a variety of well established applications. In melts that do not require extremely high cooling rates to form glasses, the rates of nucleation and growth are relatively low. Thus in high viscosity oxide systems crystallization at high temperatures can be 'frozen in' by fast cooling and the kinetics Hence glasses are ideal media for conveniently determined. fundamental quantitative studies and provide a unique opportunity to test many of the predictions of classical theories. The topic of the present paper is nucleation. Although significant advances have been made since the last Symposium in this series in 1981 [1] many important questions remain unresolved. Here some recent studies are highlighted. Various important topics such as the effects of amorphous phase separation on crystal nucleation have been recently reviewed elsewhere [2-4].

### SUMMARY OF CLASSICAL NUCLEATION THEORY

It is helpful to summarize the relevant theory to aid later discussion.

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The rate of homogeneous steady state nucleation (I) at absolute temperature T in a one-component supercooled liquid is given, according to classical theory [5] by

$$I = A \exp - [(W* + \Delta G_D)kT] \qquad \dots (1)$$

where W\* and  $\Delta G_D$  are the thermodynamic and kinetic free energy barriers respectively and k the Boltzmann constant. The pre-exponential factor A is given to a good approximation by

$$A = n_{v}(kT/h) \qquad \dots (2)$$

where  $n_v$  is the number of atoms, or strictly, 'formula units' of the crystallizing component phase per unit volume of liquid and h is Planck's constant. A is typically  $10^{41}$  -  $10^{42}$  m<sup>-3</sup>s<sup>-1</sup> and is effectively constant over the observed temperature range of nucleation. For a spherical nucleus

$$W^* = 16\pi\sigma^3 Vm^2/3\Delta G^2 \qquad \dots (3)$$

where  $\sigma$  is the crystal-liquid interfacial free energy per unit area,  $V_m$  the molar volume of the crystal phase and  $\Delta G$  the bulk free energy change per mole in crystallization.  $\Delta G_D$  can be expressed in terms of an effective diffusion coefficient D by

$$D = (kT\lambda^2/h) \exp(-\Delta G_D/kT) \qquad \dots (4)$$

where  $\lambda$ , the 'jump distance' is of the order of atomic dimensions. D may be related to Viscosity  $\eta$  by the Stokes-Einstein relation

$$\dot{D} = kT/3\pi\lambda\eta \qquad \dots (5)$$

or obtained from crystal growth measurements, assuming the kinetic barriers for nucleation and growth are the same [1-3].

### **EXPERIMENTAL METHODS**

The two stage method of measuring nucleation rates involving heat treatments at the nucleation temperature  $T_N$  for a given time and then at a higher (growth) temperature  $T_G$  to develop the crystal nuclei to observable dimensions is discussed elsewhere [1]. The number of crystals per unit volume  $N_V$  may be determined by reflection optical microscopy of polished and etched sections through the glass, and from plots of  $N_V$  against time the nucleation rate I at a given temperature obtained. For higher nucleation rates scanning electron microscopy (SEM) may be employed. It is essential to ensure that during heat treatment at  $T_N$  a large proportion of the nuclei have time to grow into small crystals and

will not redissolve on heating up to, and holding, at TG, i.e. the nuclei will attain a size larger than the critical nucleus size at T<sub>G</sub>. The measured N<sub>V</sub> will then closely approximate the number of nuclei formed at TN. The choices of both nucleation time and TG. To minimise dissolution effects the difference are important. between TG and TN should be as small as possible, consistent with a reasonable growth rate and negligible nucleation rate at TG. When correctly employed the method gives accurate and reproducible results [1]. It has the advantages that it is direct, is an absolute method, and can readily distinguish between nucleation in the volume and at the surface of the glass, but is time consuming. In some cases it is possible to dispense with the second stage growth treatment provided the growth rate is high enough at the nucleation temperature, for example at temperatures well above the nucleation maximum. A thorough discussion of the errors in the determination of N<sub>V</sub> by optical microscopy has recently been given [6]. Other methods, faster than microscopy techniques, for determining information on nucleation rates have been developed using differential thermal analysis (DTA) [7,8]. These methods, based on measurements of the temperature and height of the DTA crystallization peak, should prove particularly useful, for example for rapid comparisons of the nucleation behaviour of compositions and determining the effectiveness of nucleating agents. The validity of these techniques has been analysed theoretically [9].

### **VOLUME AND SURFACE NUCLEATION**

Most glasses show only surface nucleation on heat treatment. many cases volume nucleation may be produced by adding a suitable nucleating agent but for certain compositions no such additions are required. Most of the glasses in Table 1 are 'simple' stoichiometric, compositions, the crystallizing phase having the same composition Typical nucleation curves in Figure 1 as the parent glass. demonstrate the large variation in maximum nucleation rates (from 1.9 x 10<sup>12</sup> m<sup>-3</sup>s<sup>-1</sup> for BS<sub>2</sub> to only 1.7 x 10<sup>6</sup> m<sup>-3</sup>s<sup>-1</sup> for CS). The maximum nucleation temperatures (T<sub>M</sub>) are all close to T<sub>g</sub> (taken here as corresponding to a viscosity of 10<sup>12</sup> Pas). Striking trends are evident from Table 1. The consistent set of seven T<sub>M</sub>/T<sub>m</sub> values in the narrow range 0.54-0.58, for the stoichiometric compositions showing volume nucleation, and the high undercoolings involved, suggest homogeneous nucleation. Moreover, the systems showing volume nucleation tend to exhibit, with one exception, lower values of T<sub>g</sub>/T<sub>m</sub> (less than 0.6) than in the systems showing only surface nucleation (T<sub>g</sub>/T<sub>m</sub> more than 0.6). This trend can be understood from theory. As  $T_g$  is defined here in terms of a fixed viscosity, D and  $\Delta G_D$  are essentially constant at  $T_g$  and the driving force at  $T_g$ is given approximately [1] by

Table 1. Examples of glasses having (a) volume and surface or (b) only surface nucleation; Temperatures (K) of maximum nucleation rate  $(T_M)$ , liquidus  $(T_m)$  and glass transformation  $(T_g)$ .

Key: Ba(BaO), B(B $_2$ O $_3$ ), C(CaO), K(K $_2$ O), L(Li $_2$ O), M(MgO), N(Na $_2$ O), P(P $_2$ O $_5$ ), S(SiO $_2$ ), Sr(SrO).

Data from [2] and [10-12] as indicated.

Composition	$T_{\underline{M}}/T_{\underline{m}}$	$T_{\rm g}/T_{\rm m}$	W*/kT (at T <sub>M</sub> )		
(a) Volume and surface nuc	cleation		, M		
BaS <sub>2</sub> Ba <sub>3</sub> S <sub>5</sub>	0.58 0.58	0.57 0.56	27		
CS LB <sub>2</sub> [10,12]	0.58 0.65	0.57 0.64	45		
LS <sub>2</sub> 40L.60S (mole %) [10] 45L.555 (mole %) [10] 48L.52S (mole %) [10]	0.56	0.56 0.51 0.49 0.48	32		
NC <sub>2</sub> S <sub>3</sub> N <sub>2</sub> CS <sub>3</sub> NS SrS	0.56 0.54 0.54 ≈0.55	0.54 0.51 0.50 0.55	30 25 32		
(b) Surface nucleation only					
BaB [10] BaC <sub>2</sub> S <sub>3</sub> [10] BaP [10] CMS <sub>2</sub> [10] CP [11] KS <sub>2</sub> NS <sub>2</sub> LB [10]		0.61 0.63 0.65 0.61 0.61 0.58 0.64 0.62			

$$\Delta G = -\Delta H_f [1 - (T_g/T_m)] \qquad \dots (6)$$

where  $\Delta H_f$  is the heat of fusion per mole. Thus a low ratio  $T_g/T_m$  implies a higher nucleation rate and a greater tendency towards volume nucleation. As the ratio increases volume nucleation becomes less probable until only surface nucleation is detectable for certain systems. This simple argument neglects variations in other factors between compositions such as  $\sigma$ ,  $\Delta H_f$ 

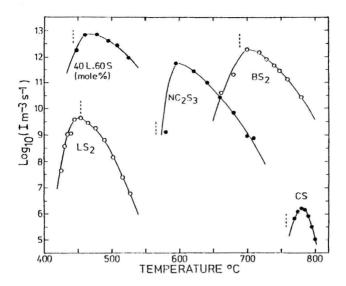


Figure 1:  $Log_{10}(I m^{-3}s^{-1})$  vs temperature (°C) for various compositions (see Table 1). Dashed lines indicate Tg values.

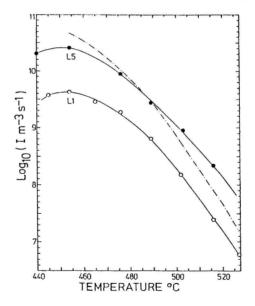


Figure 2:  $Log_{10}(I \text{ m}^{-3}s^{-1})$  vs temperature (°C) for LS<sub>2</sub> glasses; L5, 0.136 wt% H<sub>2</sub>O (O), L1, 0.02 wt% H<sub>2</sub>O (O).

and  $\Delta C_p$ , the difference in specific heats between crystal and liquid, but the general trend is clear from Table 1. A more general criterion for observable volume nucleation depends on W\* (equation (3)). Calculation using equations (1), (2), (4) and (5) indicates that W\*/kT≤40 is required for a 'just detectable' nucleation rate of  $10^6$  m<sup>-3</sup>s<sup>-1</sup> at T = T<sub>g</sub> [2]. The variations in the calculated (Table 1) values of W\*/kT at T<sub>M</sub> for the different compositions reflect the large differences in nucleation rates.

Most of the nucleation rates plotted in Figure 1 represent steady state values. In practice a steady state (constant) nucleation rate is approached gradually, the kinetics of the process being governed by an induction time, which increases with fall in temperature. Non-steady state effects [1] become of increasing importance near and below  $T_{\rm g}$ .

Detailed comparison has been made of measured steady state I values with theory (equations (1) to (5)) for lithium disilicate glass because thermodynamic ( $\Delta G$ ) and viscosity data are available [1-3]. Assuming a constant interfacial energy ( $\sigma$ ) yielded a value of A much higher than expected by theory. However, setting A at the theoretical value, the value of  $\sigma$  required to give agreement with theory varied with temperature from 147 mJm<sup>-2</sup> at 454°C to 158 mJm<sup>-2</sup> at 527°C, an increase of 7%. Similar behaviour has been observed with other compositions [2,3]. Unfortunately, little further progress can be achieved until an independent means of determining  $\sigma$  is available to test this possibility. It has been shown recently that the apparent temperature variation of  $\sigma$  for lithium disilicate may reflect the dependence of  $\sigma$  on the radius of the crystal embryo [13].

#### **NUCLEATING AGENTS**

Nucleating agents are constituents added to a glass which promote volume nucleation and glass ceramic formation. Examples are metallic particles, oxides (such as  $TiO_2$ ,  $ZrO_2$  and  $P_2O_5$ ) commonly used in silicate compositions and non-oxides (such as fluorides and water [3]). Their various possible roles include increasing homogeneous nucleation of a stable or metastable phase by increasing  $\Delta G$  and reducing  $\sigma$  or  $\Delta G_D$  [1,3], but most commonly the agent precipitates, often in combination with another component, initiating heterogeneous nucleation of a major phase [14]. The role of water is particularly interesting in relation to the crystallization of sol-gel derived glasses, which often contain higher hydroxyl levels than melted glasses. Small concentrations of water can increase nucleation and growth kinetics and reduce the viscosity of oxide glasses [1]. For example, nucleation rates in a lithium disilicate glass (L5) containing 0.136 wt% H<sub>2</sub>O were about six times greater than those in a similar glass (L1) containing 0.02 wt% H<sub>2</sub>O