

JAMES L. KIRTLEY



ELECTRIC POWER PRINCIPLES

SOURCES, CONVERSION, DISTRIBUTION AND USE

Companion Website

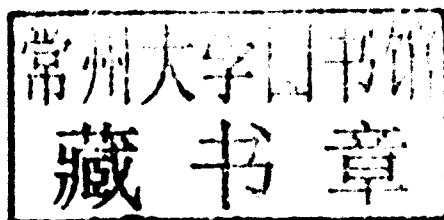
 **WILEY**

ELECTRIC POWER PRINCIPLES

Sources, Conversion, Distribution and Use

James L. Kirtley

Massachusetts Institute of Technology, USA



 **WILEY**

A John Wiley and Sons, Ltd., Publication

This edition first published 2010
© 2010 John Wiley & Sons, Ltd

Registered office

John Wiley & Sons Ltd, The Atrium, Southern Gate, Chichester, West Sussex, PO19 8SQ, United Kingdom

For details of our global editorial offices, for customer services and for information about how to apply for permission to reuse the copyright material in this book please see our website at www.wiley.com.

The right of the author to be identified as the author of this work has been asserted in accordance with the Copyright, Designs and Patents Act 1988.

All rights reserved. No part of this publication may be reproduced, stored in a retrieval system, or transmitted, in any form or by any means, electronic, mechanical, photocopying, recording or otherwise, except as permitted by the UK Copyright, Designs and Patents Act 1988, without the prior permission of the publisher.

Wiley also publishes its books in a variety of electronic formats. Some content that appears in print may not be available in electronic books.

Designations used by companies to distinguish their products are often claimed as trademarks. All brand names and product names used in this book are trade names, service marks, trademarks or registered trademarks of their respective owners. The publisher is not associated with any product or vendor mentioned in this book. This publication is designed to provide accurate and authoritative information in regard to the subject matter covered. It is sold on the understanding that the publisher is not engaged in rendering professional services. If professional advice or other expert assistance is required, the services of a competent professional should be sought.

MATLAB[®] is a trademark of The MathWorks, Inc., and is used with permission. The MathWorks does not warrant the accuracy of the text or exercises in this book. This book's use or discussion of MATLAB[®] software or related products does not constitute endorsement or sponsorship by The MathWorks of a particular pedagogical approach or particular use of MATLAB[®] software.

Library of Congress Cataloging-in-Publication Data

Kirtley, James L.

Electric power principles: sources, conversion, distribution and use / James L. Kirtley.
p. cm.

Includes index.

ISBN 978-0-470-68636-2 (cloth)

1. Electric power production. I. Title.

TK1001.K544 2010

621.3-dc22

2010010755

A catalogue record for this book is available from the British Library.

ISBN: 978-0-470-68636-2

Typeset in 10/12pt Times by Aptara Inc., New Delhi, India

Printed in Singapore by Markono Print Media Pte Ltd

ELECTRIC POWER PRINCIPLES

Preface

At the time of this writing (autumn of 2009), there appears to be a heightened awareness of the importance of energy to our social welfare. There are, in my opinion, two reasons for this. First, there is an awareness of the finite supply of fossil fuels stored beneath the surface of our planet, and that one day we will have to make do with sustainable sources of energy. The other is the fact that use of these fossil fuels releases carbon back into the atmosphere, leading to possible changes in heat transfer from the surface of the earth to space with attendant climate change. For both of these reasons the traditional methods for producing electric power may have to change, and this will mean the need for well educated, innovative engineers to build the power systems of the future.

In addition to the need for engineering of the electric power system itself is the plain fact that electric power, in the broad sense, is being used for a wider range of applications as time goes on. Virtually all rail transportation employs electric propulsion; hybrid electric automobiles have become important items of commerce and promise to become part of our energy future. Reduction of the need for energy (that is conservation) requires enhanced efficiency and effectiveness of the use of energy, and very often that involves the use of electricity.

The implications for education are clear: we in the academic world must educate engineers to be the leaders in designing, building and operating new types of electric power systems. Perhaps even more important, we must also educate a broader class of students who will become leaders in the industrial and political realms to understand at least the rudiments and implications of energy, including electric power.

This book is the descendant of sets of lecture notes that I have used in two subjects at the Massachusetts Institute of Technology: 6.061, *Introduction to Electric Power Systems* and 6.685, *Electric Machines*. These notes have existed in various forms for about three decades, and they have benefited from the experience of being used by multiple generations of MIT undergraduate and graduate students.

It is my hope that this book be used by students who want to gain a broad understanding of how electric power is generated, transmitted, distributed and used. Thus there is material here beyond the traditional electric power system and electric machinery disciplines. That said, this book does have chapters that discuss some of the traditional material of electric power systems: per-unit normalizations, symmetrical components and iterative load flow calculations. In keeping with my feeling that fundamental understanding is important, I have included chapters on the principles of electromechanical energy conversion and on magnetic circuits. To round out the power systems story is a fairly extensive chapter on synchronous machines, which are still the most important generators of electric power. There are also

short discussions of the different types of power plants, including both traditional plants and those used for extracting sustainable energy from wind and sun, and topics important to the power system: protection and DC transmission. On the usage side there is a chapter on power electronics and chapters on the major classes of electric motors: induction and direct current. MATLAB is included, and each of the chapters is accompanied by some problems with a fairly wide range of difficulty, from quite easy to fairly challenging.

The material in this book should be accessible to an undergraduate electrical engineering student at the third year level. I have assumed the reader of this book will have a basic but solid background in the fundamentals of electrical engineering, including an understanding of multivariable calculus and basic differential equations, a basic understanding of electric circuit theory and an understanding of Maxwell's equations.

This book could be used for subjects with a number of different areas of emphasis. A 'first course' in electric power systems might use Chapters 1 through 4, 6, 7, 10 and 11. Chapter 7 has an appendix on transmission line inductance parameters that can probably be safely skipped in an introductory subject.

Chapter 9 is about synchronous machines and instructors of many power systems subjects would want to address this subject. Chapter 12 is an introduction to power electronics and this, too, might be considered for a course in power systems.

A 'first course' that deals primarily with electric machines could be taught from Chapters 4, 5, 8, 9 and 12 to 15. Tutors can find solutions for end-of-chapter problems at www.wiley.com/go/kirtley_electric.

The number of students who have influenced, hopefully for the better, the subject material in this book is so large that there would be no hope in calling them all out. However, I must acknowledge a few of the people who have taught me this material and influenced my professional career. These include Herb Woodson, Jim Melcher, Gerald Wilson, Alex Kusko, Joe Smith, Charles Kingsley, Steve Umans and Steve Leeb.

I would also like to thank Steve Sprague of the Electric Motor Education and Research Foundation for the electrical sheet steel data graphics.

Contents

Preface	xi
1 Electric Power Systems	1
1.1 Electric Utility Systems	2
1.2 Energy and Power	3
1.2.1 Basics and Units	3
1.3 Sources of Electric Power	3
1.3.1 Heat Engines	4
1.3.2 Power Plants	5
1.3.3 Nuclear Power Plants	8
1.3.4 Hydroelectric Power	9
1.3.5 Wind Turbines	10
1.3.6 Solar Power Generation	12
1.4 Electric Power Plants and Generation	15
1.5 Problems	15
2 AC Voltage, Current and Power	17
2.1 Sources and Power	17
2.1.1 Voltage and Current Sources	17
2.1.2 Power	18
2.1.3 Sinusoidal Steady State	18
2.1.4 Phasor Notation	19
2.1.5 Real and Reactive Power	19
2.2 Resistors, Inductors and Capacitors	21
2.2.1 Reactive Power and Voltage	22
2.2.2 Reactive Power Voltage Support	23
2.3 Problems	26
3 Transmission Lines	31
3.1 Modeling: Telegrapher's Equations	32
3.1.1 Traveling Waves	33
3.1.2 Characteristic Impedance	33
3.1.3 Power	35
3.1.4 Line Terminations and Reflections	35

3.1.5	<i>Sinusoidal Steady State</i>	40
3.2	Problems	42
4	Polyphase Systems	45
4.0.1	<i>Two-Phase Systems</i>	45
4.1	Three-Phase Systems	47
4.2	Line–Line Voltages	49
4.2.1	<i>Example: Wye and Delta Connected Loads</i>	50
4.2.2	<i>Example: Use of Wye–Delta for Unbalanced Loads</i>	52
4.3	Problems	54
5	Electrical and Magnetic Circuits	57
5.1	Electric Circuits	57
5.1.1	<i>Kirchoff's Current Law (KCL)</i>	57
5.1.2	<i>Kirchoff's Voltage Law (KVL)</i>	58
5.1.3	<i>Constitutive Relationship: Ohm's Law</i>	58
5.2	Magnetic Circuit Analogies	60
5.2.1	<i>Analogy to KCL</i>	60
5.2.2	<i>Analogy to KVL: Magnetomotive Force</i>	61
5.2.3	<i>Analogy to Ohm's Law: Reluctance</i>	61
5.2.4	<i>Simple Case</i>	62
5.2.5	<i>Flux Confinement</i>	63
5.2.6	<i>Example: C-Core</i>	63
5.2.7	<i>Example: Core with Different Gaps</i>	64
5.3	Problems	66
6	Transformers	71
6.1	Single-phase Transformers	71
6.1.1	<i>Ideal Transformer</i>	72
6.1.2	<i>Deviations from Ideal Transformer</i>	73
6.2	Three-Phase Transformers	75
6.2.1	<i>Example</i>	77
6.3	Problems	80
7	Polyphase Lines and Single-Phase Equivalents	85
7.1	Polyphase Transmission and Distribution Lines	85
7.1.1	<i>Example</i>	87
7.2	Introduction To Per-Unit Systems	88
7.2.1	<i>Normalization Of Voltage and Current</i>	88
7.2.2	<i>Three-Phase Systems</i>	90
7.2.3	<i>Networks with Transformers</i>	90
7.2.4	<i>Transforming from one base to another</i>	91
7.2.5	<i>Example: Fault Study</i>	92
7.3	Appendix: Inductances of Transmission Lines	94
7.3.1	<i>Single Wire</i>	94
7.3.2	<i>Mutual Inductance</i>	96

7.3.3	<i>Bundles of Conductors</i>	96
7.3.4	<i>Transposed Lines</i>	97
7.4	Problems	98
8	Electromagnetic Forces and Loss Mechanisms	103
8.1	Energy Conversion Process	103
8.1.1	<i>Principle of Virtual Work</i>	104
8.1.2	<i>Coenergy</i>	108
8.2	Continuum Energy Flow	110
8.2.1	<i>Material Motion</i>	111
8.2.2	<i>Additional Issues in Energy Methods</i>	112
8.2.3	<i>Electric Machine Description</i>	116
8.2.4	<i>Field Description of Electromagnetic Force: The Maxwell Stress Tensor</i>	118
8.2.5	<i>Tying the MST and Poynting Approaches together</i>	120
8.3	Surface Impedance of Uniform Conductors	124
8.3.1	<i>Linear Case</i>	124
8.3.2	<i>Iron</i>	128
8.3.3	<i>Magnetization</i>	128
8.3.4	<i>Saturation and Hysteresis</i>	129
8.3.5	<i>Conduction, Eddy Currents and Laminations</i>	131
8.3.6	<i>Eddy Currents in Saturating Iron</i>	133
8.4	Semi-Empirical Method of Handling Iron Loss	136
8.5	Problems	139
9	Synchronous Machines	145
9.1	Round Rotor Machines: Basics	146
9.1.1	<i>Operation with a Balanced Current Source</i>	147
9.1.2	<i>Operation with a Voltage Source</i>	147
9.2	Reconciliation of Models	150
9.2.1	<i>Torque Angles</i>	150
9.3	Per-Unit Systems	151
9.4	Normal Operation	152
9.4.1	<i>Capability Diagram</i>	153
9.4.2	<i>Vee Curve</i>	153
9.5	Salient Pole Machines: Two-Reaction Theory	154
9.6	Synchronous Machine Dynamics	157
9.7	Synchronous Machine Dynamic Model	159
9.7.1	<i>Electromagnetic Model</i>	159
9.7.2	<i>Park's Equations</i>	160
9.7.3	<i>Power and Torque</i>	164
9.7.4	<i>Per-Unit Normalization</i>	164
9.7.5	<i>Equivalent Circuits</i>	167
9.7.6	<i>Transient Reactances and Time Constants</i>	168
9.8	Statement of Simulation Model	169
9.8.1	<i>Example: Transient Stability</i>	170

9.8.2	<i>Equal Area Transient Stability Criterion</i>	170
9.9	Appendix: Transient Stability Code	173
9.10	Appendix: Winding Inductance Calculation	176
9.10.1	<i>Pitch Factor</i>	180
9.10.2	<i>Breadth Factor</i>	180
9.11	Problems	182
10	System Analysis and Protection	185
10.1	The Symmetrical Component Transformation	185
10.2	Sequence Impedances	188
10.2.1	<i>Balanced Transmission Lines</i>	188
10.2.2	<i>Balanced Load</i>	189
10.2.3	<i>Possibly Unbalanced Loads</i>	190
10.2.4	<i>Unbalanced Sources</i>	191
10.2.5	<i>Rotating Machines</i>	193
10.2.6	<i>Transformers</i>	193
10.3	Fault Analysis	197
10.3.1	<i>Single Line–neutral Fault</i>	198
10.3.2	<i>Double Line–neutral Fault</i>	199
10.3.3	<i>Line–Line Fault</i>	200
10.3.4	<i>Example of Fault Calculations</i>	201
10.4	System Protection	205
10.4.1	<i>Fuses</i>	206
10.5	Switches	207
10.6	Coordination	208
10.6.1	<i>Ground Overcurrent</i>	208
10.7	Impedance Relays	208
10.7.1	<i>Directional Elements</i>	209
10.8	Differential Relays	210
10.8.1	<i>Ground Fault Protection for Personnel</i>	211
10.9	Zones of System Protection	212
10.10	Problems	212
11	Load Flow	219
11.1	Two Ports and Lines	219
11.1.1	<i>Power Circles</i>	221
11.2	Load Flow in a Network	222
11.3	Gauss–Seidel Iterative Technique	224
11.4	Bus Admittance	226
11.4.1	<i>Bus Incidence</i>	226
11.4.2	<i>Alternative Assembly of Bus Admittance</i>	227
11.5	Example: Simple Program	228
11.5.1	<i>Example Network</i>	228
11.6	MATLAB Script for the Load Flow Example	229
11.7	Problems	231

12	Power Electronics and Converters in Power Systems	235
12.1	Switching Devices	235
12.1.1	<i>Diode</i>	236
12.1.2	<i>Thyristor</i>	236
12.1.3	<i>Bipolar Transistors</i>	237
12.2	Rectifier Circuits	239
12.2.1	<i>Full-Wave Rectifier</i>	239
12.3	DC–DC Converters	247
12.3.1	<i>Pulse Width Modulation</i>	249
12.3.2	<i>Boost Converter</i>	249
12.4	Canonical Cell	255
12.4.1	<i>Bidirectional Converter</i>	255
12.4.2	<i>H-Bridge</i>	257
12.5	Three-Phase Bridge Circuits	259
12.5.1	<i>Rectifier Operation</i>	259
12.5.2	<i>Phase Control</i>	261
12.5.3	<i>Commutation Overlap</i>	262
12.5.4	<i>AC Side Current Harmonics</i>	265
12.6	High-Voltage DC Transmission	270
12.7	Basic Operation of a Converter Bridge	271
12.7.1	<i>Turn-On Switch</i>	272
12.7.2	<i>Inverter Terminal</i>	272
12.8	Achieving High Voltage	273
12.9	Problems	274
13	Induction Machines	281
13.1	Introduction	281
13.2	Induction Machine Transformer Model	283
13.2.1	<i>Operation: Energy Balance</i>	289
13.2.2	<i>Example of Operation</i>	294
13.2.3	<i>Motor Performance Requirements</i>	294
13.3	Squirrel-Cage Machines	296
13.4	Single-Phase Induction Motors	297
13.4.1	<i>Rotating Fields</i>	297
13.4.2	<i>Power Conversion in the Single-Phase Induction Machine</i>	298
13.4.3	<i>Starting of Single-Phase Induction Motors</i>	300
13.4.4	<i>Split Phase Operation</i>	301
13.5	Induction Generators	303
13.6	Induction Motor Control	306
13.6.1	<i>Volts/Hz Control</i>	306
13.6.2	<i>Field Oriented Control</i>	307
13.6.3	<i>Elementary Model</i>	308
13.6.4	<i>Simulation Model</i>	309
13.6.5	<i>Control Model</i>	310
13.6.6	<i>Field-Oriented Strategy</i>	311

13.7	Doubly Fed Induction Machines	313
13.7.1	<i>Steady State Operation</i>	315
13.8	Appendix 1: Squirrel-Cage Machine Model	318
13.8.1	<i>Rotor Currents and Induced Flux</i>	319
13.8.2	<i>Squirrel-Cage Currents</i>	320
13.9	Appendix 2: Single-Phase Squirrel Cage Model	325
13.10	Appendix 3: Induction Machine Winding Schemes	326
13.10.1	<i>Winding Factor for Concentric Windings</i>	329
13.11	Problems	331
14	DC (Commutator) Machines	337
14.1	Geometry	337
14.2	Torque Production	338
14.3	Back Voltage	339
14.4	Operation	341
14.4.1	<i>Shunt Operation</i>	342
14.4.2	<i>Separately Excited</i>	343
14.4.3	<i>Machine Capability</i>	345
14.5	Series Connection	346
14.6	Universal Motors	348
14.7	Commutator	349
14.7.1	<i>Commutation Interpoles</i>	351
14.7.2	<i>Compensation</i>	351
14.8	Compound Wound DC Machines	352
14.9	Problems	354
15	Permanent Magnets in Electric Machines	357
15.1	Permanent Magnets	357
15.1.1	<i>Permanent Magnets in Magnetic Circuits</i>	359
15.1.2	<i>Load Line Analysis</i>	360
15.2	Commutator Machines	363
15.2.1	<i>Voltage</i>	365
15.2.2	<i>Armature Resistance</i>	366
15.3	Brushless PM Machines	367
15.4	Motor Morphologies	367
15.4.1	<i>Surface Magnet Machines</i>	367
15.4.2	<i>Interior Magnet, Flux Concentrating Machines</i>	368
15.4.3	<i>Operation</i>	369
15.4.4	<i>A Little Two-Reaction Theory</i>	371
15.4.5	<i>Finding Torque Capability</i>	374
15.5	Problems	380
Index		385

1

Electric Power Systems

There are many different types of power systems, such as the propulsion systems in automobiles and trucks and the hydraulic systems used in some industrial robots and for actuating scoops and blades in digging equipment. All power systems have certain fundamental elements. There is some sort of prime mover (such as a gasoline engine), a means of transport of the power produced (such as the drive shaft, transmission, differential and axles), and a means of using that power (wheels on the road). The focus of this book is on *electric* power systems, in which the means of transporting energy is the flow of electrical current against an electric potential (voltage). There are many different types of electric power systems as well, including the electrical systems in cars and trucks, propulsion systems in electric trains and cruise ships. The primary focus in this book will be the kinds of electric power systems incorporated in public utilities, but it must be kept in mind that all electric power systems have many features in common. Thus the lessons learned here will have applicability well beyond the utility system.

It has become all too easy to take for granted the electric utility service that is ubiquitous in the developed countries. Electric utilities are wired to nearly every business and residence, and standardized levels of voltage and frequency permit a wide range of appliances to be simply ‘plugged in’ and operated. Consumers don’t have to give any thought to whether or not an appliance such as a television set, a computer or an egg beater will work. Not only will these appliances work when plugged in, but the electric power to make them work is quite reliable and cheap. In fact, the absence of useful electric power is quite rare in the developed countries in the world. Widespread failure to deliver electric power has become known as a ‘blackout’, and such events are rare enough to make the nightly news across the country. Even substantial distribution system failures due to weather are newsworthy events and very often cause substantial hardship, because we have all come to depend on electric power to not only keep the lights on, but also to control heating, cooling, cooking and refrigeration systems in our homes and businesses.

At the time of this writing, electric power systems in the United States and most of the developing world use as their primary sources of energy fossil fuels (coal and natural gas), falling water (hydroelectric power), and heat from nuclear fission. There are small but rapidly growing amounts of electric power generated from wind and solar sources and some

electric power is generated from volcanic heat (geothermal energy). These ‘renewables’ are expected to grow in importance in the future, as the environmental impacts of the use of fossil fuels become more noticeable and as the fossil fuels themselves are exhausted. There are some differences between technologies involved in the older, existing power generation sources and the newer, sustainable technologies, and so in this book we will discuss not only how existing utility systems work but also how the emerging technologies are expected to function.

1.1 Electric Utility Systems

A very ‘cartoon-ish’ drawing of a simple power system is shown in Figure 1.1.

Electric power originates in ‘power plants’. It is transmitted by ‘transmission lines’ from the power plants to the loads. Along the way the voltage is first stepped up by transformers, generally within the power plants, from a level that is practical for the generators to a level that provides adequate efficiency for long-distance transmission. Then, near the loads the electric power is stepped down, also by transformers, to a voltage useable by the customer. This picture is actually quite simplified. In modern utility systems there are thousands of power plants connected together through networks, and many more connections to loads than are indicated in Figure 1.1. The connections to actual loads is usually a bit more like what is shown in Figure 1.2. At the distribution level the connection is ‘radial’, in that there is one connection from the source of electric power (the ‘grid’), and that is broken down into many load connections. Usually the distribution primary line is at a voltage level intermediate between the transmission level and the voltage that is actually used by customers.

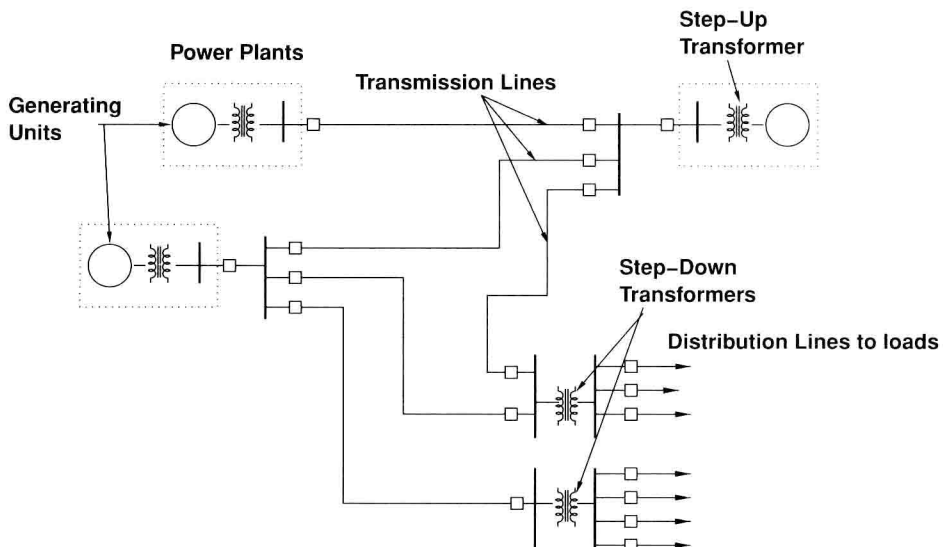


Figure 1.1 Cartoon of a simple power system

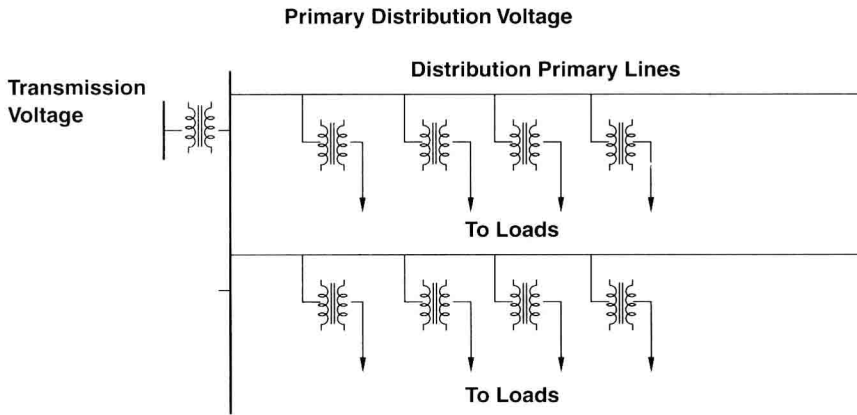


Figure 1.2 Distribution circuits

1.2 Energy and Power

1.2.1 Basics and Units

Before starting to talk about electric power systems it is important to understand some of the basics of energy and power. In the international system of units (SI), there are two basic units of energy. One is the joule (J), which is the energy expended by pushing a newton (N), a unit of force, over one meter. So a joule is a newton-meter. (A kilogram ‘weighs’ about 9.8 newtons at the surface of the earth). The other unit of energy is related to heat, and it is the Calorie. This story is complicated by the fact that there are actually two definitions of the Calorie. One is the heat (amount of energy) required to heat 1 gram of water 1 degree Celsius. This amounts to about 4.184 joules. The second definition is often called the ‘kilogram Calorie’, the amount of energy required to heat 1 kilogram of water 1 degree Celsius. This is obviously just 1,000 of the ‘gram Calories’, or 4,184 joules.

The basic unit of power is the watt, which is one joule/second. As it our predecessors crafted it, 1 watt is also 1 volt \times 1 ampere. The volt is a unit of electrical potential and the ampere is a unit of current flow. Power is expressed in watts, kilowatts, etc., and a basic unit of energy is the kilowatt-hour (kWh), (3.6×10^6 J). Electricity is sold at retail by the kilowatt-hour and, usually, at wholesale by the megawatt-hour.

Another unit of heat that is commonly used in discussing power plants is the British Thermal Unit (BTU), which is the amount of heat required to raise 1 pound of water 1 degree Fahrenheit. This is about 0.252 kilogram calories or 1054 joules. In the United States, fuels are often sold based on their energy content as measured in BTUs, or more commonly in millions of BTU’s (MBTU). See Tables 1.1 and 1.2.

1.3 Sources of Electric Power

There are two basic ways in which electric power is produced: by generators turned by some sort of ‘prime mover’ or by direct conversion from a primary source such as sunlight, or conversion of chemical energy in fuel cells. The prime movers that turn generators can be heat

Table 1.1 Some of the unit symbols used in this book

Unit	Unit of	Symbol
Ampere	current	A
British Thermal Unit	heat energy	BTU
Coulomb	charge	C
Calorie	heat energy	Cal
degree Celsius	temperature	°C
Farad	capacitance	F
Gauss	flux density	G
Hertz (cycles/second)	frequency	Hz
Henry	inductance	H
hour	time	h
Joule	energy	J
Kelvin	temperature	K
kilogram	mass	kg
meter	length	m
Newton	force	N
volt	electric potential	V
volt-ampere	apparent power	VA
watt	power	W
Weber	flux	Wb

engines such as steam turbines, gas turbines, internal combustion engines burning diesel fuel, natural gas or (rarely) gasoline, or turbines that convert power directly from falling water or wind. Geothermal heat is sometimes used to power heat engines in places where that heat is accessible (this is the major source of electric power in Iceland). Even sunlight has been used as the power input to heat engines.

1.3.1 Heat Engines

Most power plant ‘prime movers’ are heat engines that burn a primary fuel such as coal or natural gas and that use the energy released by combustion to produce mechanical power (generally turning a shaft) that is used to drive a generator to produce electrical power. We

Table 1.2 Multiplying prefixes used in this book

Prefix	Symbol	Multiple
tera	T	10^{12}
giga	G	10^9
mega	M	10^6
kilo	k	10^3
centi	c	10^{-2}
milli	m	10^{-3}
micro	μ	10^{-6}
nano	n	10^{-9}

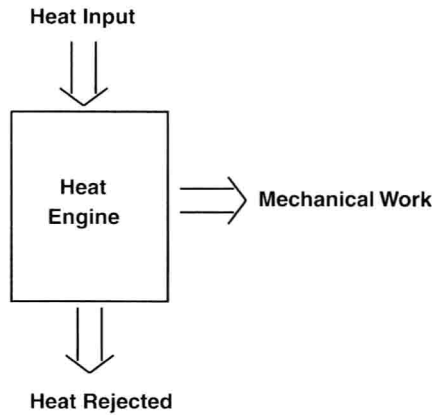


Figure 1.3 Energy balance

will, in later chapters of this book describe how generators work. Heat engines can convert only some of the heat energy that is input to the engines into mechanical work. The details of this are beyond our scope here, but as is shown in Figure 1.3, there will always be waste heat associated with a heat engine. Heat engines take energy at a high temperature and reject heat energy at a lower temperature. The difference between the heat input and rejected heat energy is what is converted to mechanical power, and efficiency is the ratio of mechanical power output to heat power input.

There is a well known bound on efficiency of a heat engine, called the ‘Carnot efficiency’, and that is associated with the temperature of the input heat and the temperature of the rejected heat. This is:

$$W_m < Q_h \frac{T_h - T_\ell}{T_h}$$

where Q_h is the input energy. Mechanical work is the difference between heat input and heat rejected, and the efficiency depends on the heat input temperature T_h and heat rejection temperature T_ℓ . Practical heat engines do not approach this Carnot limit very closely, but this expression is a guide to heat engine efficiency: generally higher heat input temperatures and lower heat rejection temperatures lead to more efficient heat engines.

In discussing power plant efficiency, we often note that one kilowatt-hour is 3.6 MJ or 3,414 BTU. The fuel energy input to a power plant to produce one kilowatt hour is referred to as its ‘heat rate’, and this is inversely related to its thermal efficiency. A power plant that has a heat rate of, say, 10,000 BTU/kWh would have a net thermal efficiency of $\eta = \frac{3414}{10000} \approx 0.3414$.

1.3.2 Power Plants

Figure 1.4 shows a cartoon of a power plant that burns fossil fuels. The heat engine in this case is a steam turbine. Water is first compressed and pumped into a ‘boiler’, where a fire heats it into steam. The steam is expanded through a turbine which turns a generator. The turbine exhaust is then fed to a ‘condenser’ where the waste heat is rejected. There are several