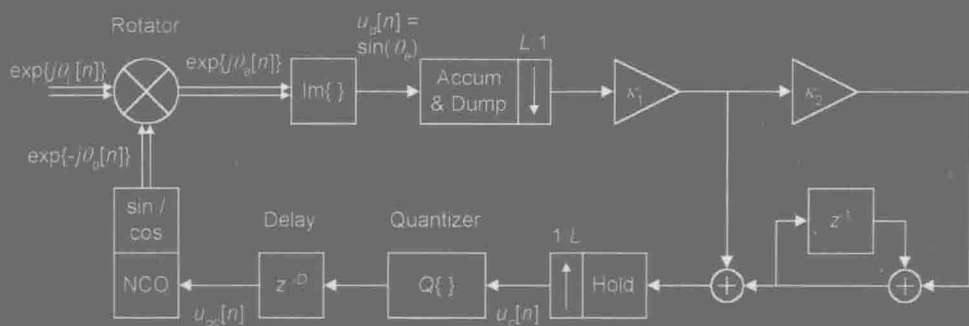


Phaselock Techniques

Third Edition

Floyd M. Gardner



PHASELOCK TECHNIQUES

Third Edition

FLOYD M. GARDNER

Consulting Engineer
Palo Alto, California



A JOHN WILEY & SONS, INC., PUBLICATION

Copyright © 2005 by John Wiley & Sons, Inc. All rights reserved.

Published by John Wiley & Sons, Inc., Hoboken, New Jersey.

Published simultaneously in Canada.

No part of this publication may be reproduced, stored in a retrieval system, or transmitted in any form or by any means, electronic, mechanical, photocopying, recording, scanning, or otherwise, except as permitted under Section 107 or 108 of the 1976 United States Copyright Act, without either the prior written permission of the Publisher, or authorization through payment of the appropriate per-copy fee to the Copyright Clearance Center, Inc., 222 Rosewood Drive, Danvers, MA 01923, (978) 750-8400, fax (978) 750-4470, or on the web at www.copyright.com. Requests to the Publisher for permission should be addressed to the Permissions Department, John Wiley & Sons, Inc., 111 River Street, Hoboken, NJ 07030, (201) 748-6011, fax (201) 748-6008, or online at <http://www.wiley.com/go/permission>.

Limit of Liability/Disclaimer of Warranty: While the publisher and author have used their best efforts in preparing this book, they make no representations or warranties with respect to the accuracy or completeness of the contents of this book and specifically disclaim any implied warranties of merchantability or fitness for a particular purpose. No warranty may be created or extended by sales representatives or written sales materials. The advice and strategies contained herein may not be suitable for your situation. You should consult with a professional where appropriate. Neither the publisher nor author shall be liable for any loss of profit or any other commercial damages, including but not limited to special, incidental, consequential, or other damages.

For general information on our other products and services or for technical support, please contact our Customer Care Department within the United States at (800) 762-2974, outside the United States at (317) 572-3993 or fax (317) 572-4002.

Wiley also publishes its books in a variety of electronic formats. Some content that appears in print may not be available in electronic formats. For more information about Wiley products, visit our web site at www.wiley.com.

Library of Congress Cataloging-in-Publication Data:

Gardner, Floyd Martin, 1929—

Phaselock techniques / Floyd M. Gardner.—3rd ed.
p. cm.

Includes bibliographical references and index.

ISBN-13 978-0-471-43063-6 (cloth)

ISBN-10 0-471-43063-3 (cloth)

1. Phase-locked loops. I. Title.

TK7872.P38G37 2005

621.3815'364—dc22

2004065041

Printed in the United States of America.

10 9 8 7 6 5 4 3 2 1

PREFACE

The first edition of this book was published in 1966 and the second in 1979. Phaselock was an unimaginably exotic subject in 1966, with limited applications and few practitioners. Now phaselock is a mature subject: myriads of phaselock loops are ensconced in the world's electronic devices; numerous applications include phaselock loops; large numbers of practitioners deal with phaselock. No other books on phaselock loops existed when the first edition was published, but more than 20 exist today. Why is a third edition justified at this time?

In 1966, a simple, short introduction to the basics of the subject was needed for an audience for whom phaselock was strange and new. Today, phaselock loops are firmly established in the mainstream of electronics engineering. Much new information on phaselock loops has accumulated over the years, and several topics once thought important have proved to be ephemeral. Experience has taught me that certain explanations would be better presented from revised viewpoints.

There is no need for another introductory text; that function is well served by a number of the books listed in Section 1.3 and probably others as well. Instead, this book reexamines the traditional phaselock topics in greater depth than previously. In addition, much new material has been included, some of it never before published. Examples of additions include revised and expanded material on transfer functions, two chapters related to phase noise, two chapters related to digital phaselock loops, a chapter on charge-pump phaselock loops, expanded material on phase detectors, and a chapter on anomalous phaselocking.

As in the earlier editions, only minimal space has been devoted to circuits. The book is concerned with underlying principles, which remain valid despite technology advances, not with implementations, which change drastically as technology changes. Several parts of the second edition have been omitted: the chapters on

optimization and synchronization, and the mathematical appendix. Formal optimization has not proved to be as important to design as was earlier anticipated; instead, a designer is much more likely to perform a trade-off among the few parameters available in a practical phaselock loop. The mathematical appendix has been omitted on the premise that the level of mathematics presented here should be comfortable for all electrical engineering graduates. Synchronization (recovery of carrier and clock from data signals), a major discipline of its own, was deemed to have grown too large to cover adequately in a book on phaselock loops. See Section 17.1 for a brief guide to synchronization.

Simulation is another absent topic. Information presented in several chapters is based on simulations, certain kinds of new data can be gathered only by simulation, and simulation is crucial for design and verification of integrated circuits. Nonetheless, the book does not tell how to conduct simulations of phaselock loops. That topic deserves a separate book of its own; it is too extensive to include here.

Many thousands of articles and books on phaselock have appeared worldwide over the years, far too many to cite individually. Although many pertinent references have been cited in the individual chapters of the book, it is not possible to discover every valuable publication written on each topic. Nor, after many years of work on the subject, is it possible always to remember who originated every technique that is presented. I apologize in advance to anyone who may have been slighted; the omission is not deliberate.

Several guidelines have been followed in selecting reference citations for each chapter: The reference is to an original work; wherever possible, the reference appeared in a public, archival publication; the reference treats lasting principles rather than transitory details of implementation. A reader will observe a preponderance of citations to IEEE publications and to books published in the United States. This choice reflects the omnipresence of IEEE publications and also the contents of my personal library.

I want to thank my many clients over the years who have afforded me the opportunities to learn so much about such a fascinating subject.

FLOYD M. GARDNER

*Palo Alto, California
October 2004*

NOTATION

A	Amplitude
B_i	Bandwidth (Hz) of an input bandpass filter
B_L	Noise bandwidth (Hz) of a PLL
b	Number of bits in a digital word
b	Ratio of frequency of a pole to frequency of a zero
f	Frequency (Hz)
f	Transform variable of Fourier transforms
f_c	Comparison frequency (Hz) at a phase detector
f_{ck}	Clock frequency (Hz)
f_m	Frequency (Hz) of modulation
f_s	Sampling frequency (Hz), $= 1/t_s$
Δf	Peak frequency deviation (Hz)
Δf	Frequency offset (Hz) from a carrier
δf	Frequency increment (Hz) in a quantized-tuning oscillator
D	Delay (sample intervals)
$E(f)$	$= E(s) _{s=j2\pi f}$
$E(s)$	Closed-loop error transfer function of a PLL
$F(s)$	Transfer function of a loop filter
$FP[x]$	Fractional part of x
$G(s)$	Open-loop transfer function of a PLL
$H(f)$	$= H(s) _{s=j2\pi f}$
$H(s)$	Closed-loop system transfer function of a PLL
$Im[x]$	Imaginary part of x
$IP[x]$	Integer part of x
i	Subscript denoting “input”

i	An integer
$J_n(x)$	Bessel function of the first kind, order n , and argument x
j	$\sqrt{-1}$
K	Loop gain (rad/sec) of a PLL
K'	Normalized (dimensionless) loop gain, $= K\tau_2$
K_d	Gain (V/rad or A/rad) of a phase detector
K_{DC}	DC gain (rad/sec) of a PLL
K_i	Gain coefficient in analog PLL, $i = 1, 2, \dots$
K_m	Gain (V^{-1}) of a multiplier
K_o	Gain (rad/sec·V) of a VCO
K_p	Gain (V/cycle) of a phase detector $= 2\pi K_d$
K_v	Gain (Hz/V) of a VCO, $= K_o/2\pi$
k	An integer
$L\{x\}$	Laplace transform of x
$\mathcal{L}(f)$	Normalized one-sided RF spectrum of a signal
m, M	An integer
$m(t)$	Modulation waveshape
N_0	One-sided spectrum (V^2/Hz) of white noise
n, N	An integer
$n(t)$	Noise voltage (V)
$n_c(t), n_s(t)$	Baseband quadrature components of bandpass noise (V)
o	Subscript denoting “output” or “oscillator”
$P_{\text{RF}}(f)$	Spectrum analyzer representation of the one-sided spectral density of an RF signal
P_s	Signal power (W)
p	Normalized Laplace variable, $= s\tau_2$
Q	Quality factor of a resonator
Q	Number of quantization levels
Q	Division ratio
$\text{Re}[x]$	Real part of x
$r(t)$	Received signal
$s = \sigma + j\omega$	Transform complex variable of a Laplace transform
SNR	Signal-to-noise ratio
SNR_L	Signal-to-noise ratio in PLL noise bandwidth $2B_L$
t	Time (sec)
t_s	Sampling interval (sec), $= 1/f_s$
$u_c[n]$	Sample- n control input (dimensionless) to an NCO
$u_d[n]$	Sample- n output (dimensionless) of a digital phase detector
V_o	Peak output voltage (V) of a VCO
V_s	Peak voltage (V) of an input signal
$v_c(t), V_c(s)$	VCO control voltage (V)
$v_d(t), V_d(s)$	Phase detector output (V)
$W_{n'}(f)$	One-sided spectral density (rad^2/Hz) of the equivalent noise out of a phase detector

$W_{\theta no}(f)$	One-sided spectral density of the VCO phase (rad^2/Hz) due to the noise input to a PLL
$W_{\text{RF}}(f)$	Measured one-sided spectral density (V^2/Hz) of an RF signal
$W_{vo}(f)$	Theoretical one-sided spectral density (V^2/Hz) of an oscillator output
$W_{\phi}(f)$	One-sided baseband spectrum (rad^2/Hz) of phase noise
z	Transform variable of z -transforms

Greek Symbols

α	Signal suppression factor (dimensionless) in a limiter
β	Modulation index (rad) of angle modulation
γ	Crest factor of a signal
$\varepsilon[n]$	Sample n of phase (cycles)
ζ	Damping factor of a second-order PLL
θ	Phase angle (rad)
θ_a	Steady-state phase error (rad) due to frequency-ramp input
θ_e	Phase error (rad) between an input signal and a VCO, $= \theta_i - \theta_o$
θ_i	Phase angle (rad) of an input signal
θ_{no}	Fluctuation of VCO phase (rad) caused by noise
θ_o	VCO phase (rad)
θ_v	Steady-state phase error (static phase error; loop stress) due to frequency offset
$\Delta\theta$	Phase deviation (rad)
$\Delta\theta$	Amplitude (rad) of phase step
κ	Loop gain (dimensionless) in a digital PLL
κ_d	Gain (rad^{-1}) of a digital phase detector
κ_i	Gain coefficient in a digital PLL, $i = 1, 2, \dots$
κ_o	Gain (rad) of a NCO
κ_p	Gain (cycle^{-1}) of a digital phase detector, $= 2\pi\kappa_d$
κ_v	Gain (cycles) of an NCO, $= \kappa_o/2\pi$
Λ	Rate of change (rad/sec^2) of frequency, $= d\omega/dt$
ρ	Signal-to-noise ratio
σ_x	Standard deviation of x
τ	Timing error (sec)
τ	Delay (sec)
τ_i	Time constant (sec), $i = 1, 2, \dots$
τ_2	Time constant (sec) of stabilizing zero in a type 2 PLL
$\phi(t)$	Phase noise (rad)
ψ	Angle (rad) around a unit circle
ψ	Normalized frequency (dimensionless), $= \omega t_s$
$\psi(s)$	Phase (rad) of a transfer function
ψ_{gc}	Normalized unity-gain crossover frequency $\omega_{gc}t_s$ of open-loop transfer function of sampled PLL, $ G(e^{j\psi_{gc}}) = 1$

ω	Angular frequency (rad/sec), $= 2\pi f$
ω_c	Comparison frequency (rad/sec) at a phase detector, $= 2\pi f_c$
ω_{gc}	Unity-gain crossover frequency (rad/sec) of open-loop transfer function, $ G(j\omega_{gc}) = 1$
ω_m	Modulating frequency (rad/sec)
ω_n	Natural frequency (rad/sec) of a second-order PLL
ω_π	Phase crossover frequency (rad/sec), $\text{Arg}[G(j\omega_\pi)] = -\pi$
$\Delta\omega$	Frequency offset or frequency step (rad/sec)
$\Delta\omega_H$	Hold-in limit (rad/sec) of a PLL
$\Delta\omega_L$	Lock-in limit (rad/sec) of a PLL
$\Delta\omega_P$	Pull-in limit (rad/sec) of a PLL

CONTENTS

PREFACE	xvii
NOTATION	xix
1 INTRODUCTION	1
1.1 Salient Properties of PLLs / 2	
1.1.1 Bandwidth / 2	
1.1.2 Linearity / 3	
1.2 Organization of the Book / 3	
1.3 Annotated Bibliography / 3	
1.3.1 Books / 3	
1.3.2 Reprint Volumes / 4	
1.3.3 Journal Special Issues / 5	
2 TRANSFER FUNCTIONS OF ANALOG PLLs	6
2.1 Basic Transfer Functions / 6	
2.1.1 Transfer Functions of Individual Elements / 7	
2.1.2 Combined Transfer Functions / 8	
2.1.3 Characteristic Equation / 9	
2.1.4 Nomenclature, Coefficients, and Units / 9	
2.2 Second-Order PLLs / 10	
2.2.1 Loop Filters / 10	
2.2.2 Order and Type / 12	

- 2.2.3 Loop Parameters / 12
- 2.2.4 Frequency Response / 15
- 2.3 Other Loop Types and Orders / 20
 - 2.3.1 General Definition of Loop Gain K / 20
 - 2.3.2 Examples of Type 1 PLLs / 22
 - 2.3.3 Examples of Type 2 PLLs / 24
 - 2.3.4 Higher-Type PLLs / 28
- Reference / 28

3 GRAPHICAL AIDS

29

- 3.1 Root-Locus Plots / 30
 - 3.1.1 Description of Root-Locus Plots / 30
 - 3.1.2 Stability Criterion / 33
 - 3.1.3 Root Loci of Type 1 PLLs / 33
 - 3.1.4 Root Loci of Type 2 PLLs / 33
 - 3.1.5 Root Loci of Type 3 PLLs / 34
 - 3.1.6 Root Loci of Higher-Order PLLs / 35
 - 3.1.7 Effect of Loop Delay on Root Locus / 38
- 3.2 Bode Plots / 38
 - 3.2.1 Presentation Options / 38
 - 3.2.2 Stability / 39
 - 3.2.3 Bode Plots of Type 1 PLLs / 40
 - 3.2.4 Bode Plots of Type 2 PLLs / 43
 - 3.2.5 Bode Plots of Type 3 PLLs / 48
- 3.3 Nyquist Diagrams / 49
- 3.4 Nichols Charts / 49
 - 3.4.1 Stability Criterion / 49
 - 3.4.2 M -Contours / 50
 - 3.4.3 Examples of Nichols Charts / 50
- 3.5 Closed-Loop Frequency-Response Curves / 52
- Appendix 3A: Salient Features of Root Loci / 52
 - 3A.1 Branches of Root Loci / 53
 - 3A.2 Locus on the Real Axis / 53
 - 3A.3 Locus Intersections with Axes / 54
- Appendix 3B: Formats of the Open-Loop Transfer Function $G(s)$ / 56
 - 3B.1 Proportional-Plus-Integral Section / 56
 - 3B.2 High-Frequency Section / 60
 - 3B.3 Calculations / 60

Appendix 3C: Closed-Loop Frequency Responses /	61
3C.1 Frequency-Response Formulas /	61
3C.2 Example Frequency-Response Graphs /	61
References /	64

4 DIGITAL PLLs: TRANSFER FUNCTIONS AND RELATED TOOLS

65

4.1 Distinctive Properties of Digital PLLs /	65
4.2 Digital Transfer Function /	66
4.2.1 Configuration of a Digital PLL /	66
4.2.2 Difference Equations /	67
4.2.3 z -Transforms of the Loop Elements /	69
4.2.4 Loop Filter /	70
4.2.5 Loop Transfer Functions /	71
4.2.6 Poles and Zeros /	71
4.3 Loop Stability /	73
4.3.1 Type 1 DPLLs /	73
4.3.2 Type 2 DPLLs /	73
4.3.3 Type 3 DPLLs /	74
4.4 Root-Locus Plots /	74
4.4.1 Root Loci of Type 1 DPLLs /	75
4.4.2 Root Loci of Type 2 DPLLs /	75
4.4.3 Root Loci of Type 3 DPLLs /	78
4.5 DPLL Frequency Responses: Formulation /	79
4.6 Bode Plots and Nichols Charts /	80
4.6.1 Basis of Bode Plots /	80
4.6.2 Bode Stability Criteria /	81
4.6.3 Bode Plots of Example DPLLs /	81
4.6.4 Nichols Chart Example /	83
4.7 Time-Continuous Approximation for a DPLL /	85
4.8 Frequency-Response Examples /	86
4.8.1 Effect of Delay /	86
4.8.2 Effect of Bandwidth /	87
4.9 Lowpass Filters in the Loop /	88
4.9.1 Infinite Impulse Response Lowpass Filter /	88
4.9.2 Finite Impulse Response Lowpass Filter /	90
Appendix 4A: Stability of Digital Phaselock Loops /	91
4A.1 Type 1 DPLL /	92
4A.2 Type 2 DPLL /	93
Reference /	96

5 TRACKING**97**

- 5.1 Linear Tracking / 97
 - 5.1.1 Steady-State Phase Errors / 98
 - 5.1.2 Transient Response / 100
 - 5.1.3 Response to Sinusoidal Angle Modulation / 109
- 5.2 Nonlinear Tracking: Lock Limits / 112
 - 5.2.1 Phase-Detector Nonlinearity / 112
 - 5.2.2 Steady-State Limits / 112
 - 5.2.3 Transient Limits / 114
 - 5.2.4 Modulation Limits / 118
- References / 121

6 EFFECTS OF ADDITIVE NOISE**123**

- 6.1 Linear Operation / 123
 - 6.1.1 Noise Model of a Phase Detector / 123
 - 6.1.2 Noise Transfer Function / 129
 - 6.1.3 Noise Bandwidth / 129
 - 6.1.4 Signal-to-Noise Ratio in a PLL / 131
 - 6.1.5 Optimality / 132
- 6.2 Nonlinear Operation / 132
 - 6.2.1 Observed Behavior / 133
 - 6.2.2 Nonlinear Analysis of Phase Error / 135
 - 6.2.3 Probability Density and Variance / 136
 - 6.2.4 Cycle Slips / 137
 - 6.2.5 Experimental and Simulation Results / 138
 - 6.2.6 Approximate Analyses / 138
 - 6.2.7 Miscellaneous Features / 139
- References / 141

7 EFFECTS OF PHASE NOISE**143**

- 7.1 Properties of Phase Noise / 144
 - 7.1.1 Oscillator Model / 144
 - 7.1.2 Neglect of Amplitude Noise / 144
 - 7.1.3 Variance / 144
 - 7.1.4 Nonstationarity / 144
- 7.2 Spectra of Phase Noise / 146
 - 7.2.1 Theoretical Spectrum $W_{vo}(f)$ / 146
 - 7.2.2 Normalized Spectrum $\mathcal{L}(\Delta f)$ / 147
 - 7.2.3 RF Spectra $W_{RF}(f)$ and $P_{RF}(f)$ / 147
 - 7.2.4 Phase-Noise Spectrum $W_{\phi}(f)$ / 149

7.2.5	Frequency-Noise Spectrum $W_{\omega}(f)$ /	152
7.2.6	Example Phase-Noise Spectrum /	152
7.3	Properties of Phase-Noise Spectra /	153
7.3.1	Typical Continuous Spectra /	154
7.3.2	Meaning of $W_{\phi}(f)$ /	155
7.3.3	Interpretation of Spectral Displays /	156
7.3.4	Relationship Between $W_{\phi}(f)$ and $\mathcal{L}(\Delta f)$ /	157
7.4	Propagation of Phase Noise /	159
7.4.1	Phase-Noise Propagation in Auxiliary Devices /	159
7.4.2	Phase-Noise Propagation in PLLs /	161
7.5	Integrated Phase Noise in PLLs /	162
7.5.1	Basic Formulas /	162
7.5.2	Excessive Phase Noise /	163
7.5.3	Effect on Coherent Demodulation /	163
7.5.4	Bandwidth Trade-off /	163
7.5.5	Integration /	164
7.5.6	A Paradox /	165
7.5.7	Integration of Spectral Lines /	166
7.5.8	Phase-Noise Specifications /	166
7.6	Timing Jitter /	167
	Appendix 7A: Analysis of Interference in a Hard Limiter /	168
	Appendix 7B: Integrals of Untracked Phase Noise /	169
	7B.1 Integration Procedures /	169
	7B.2 Results of Integrations /	169
	7B.3 Discussion /	171
	Appendix 7C: Numerical Integration of PLL Phase Noise /	171
	7C.1 Definition and Application of Integrated Phase Noise /	172
	7C.2 Data Formats /	172
	7C.3 Data Adjustments /	173
	7C.4 Data Filtering /	174
	7C.5 Numerical Integration /	174
	Appendix 7D: Integration of Discrete Lines in the Phase-Noise Spectrum /	175
	Appendix 7E: Timing Jitter /	177
	7E.1 Jitter Definitions /	177
	7E.2 Jitter in PLLs /	179
	References /	180

8 ACQUISITION OF PHASELOCK**183**

- 8.1 Characterization / 183
- 8.2 Phase Acquisition / 184
 - 8.2.1 First-Order Loop / 184
 - 8.2.2 Hang-up / 186
 - 8.2.3 Lock-in / 186
 - 8.2.4 Aided Phase Acquisition / 188
- 8.3 Frequency Acquisition / 189
 - 8.3.1 Frequency Pull-in / 189
 - 8.3.2 Frequency Sweeping / 195
 - 8.3.3 Discriminator-Aided Frequency Acquisition / 199
 - 8.3.4 Implementation of Frequency Discriminators / 203
- 8.4 Diverse Matters / 204
 - 8.4.1 Lock Indicators / 204
 - 8.4.2 Wide-Bandwidth Methods / 205
 - 8.4.3 Memory / 206
- References / 206

9 OSCILLATORS**209**

- 9.1 Desired Properties / 209
- 9.2 Classes of Oscillators / 210
- 9.3 Phase Noise in Oscillators: Simplified Approach / 210
 - 9.3.1 Leeson's Model / 210
 - 9.3.2 Guides for Oscillator Design / 212
 - 9.3.3 Example Phase-Noise Spectra / 213
 - 9.3.4 Shortcomings of Leeson's Model / 214
- 9.4 Classifications of Oscillators / 215
- 9.5 Phase Noise in Oscillators: Advanced Analysis / 217
 - 9.5.1 Impulse Sensitivity Function / 218
 - 9.5.2 Nonlinear Analyses for Phase Noise / 219
- 9.6 Other Disturbances / 221
- 9.7 Types of Oscillator Tuning / 223
 - 9.7.1 Continuous-Tuning Oscillators / 223
 - 9.7.2 Discrete-Tuning Oscillators / 224
- 9.8 Tuning of Analog VCOs / 226
 - 9.8.1 Tuning Curve / 227
 - 9.8.2 Tuning Methods / 228
 - 9.8.3 Speed of Tuning / 231
- References / 232

10 PHASE DETECTORS**237**

- 10.1 Multiplier Phase Detectors / 237
 - 10.1.1 Switching Phase Detectors: Principles / 238
 - 10.1.2 Switching Phase Detectors: Examples / 240
 - 10.1.3 Hybrid-Transformer PD / 244
 - 10.1.4 Nonsinusoidal s -Curves / 245
- 10.2 Sequential Phase Detectors / 246
- 10.3 Phase/Frequency Detector / 248
 - 10.3.1 PFD Configuration / 248
 - 10.3.2 Delay in PFD / 250
 - 10.3.3 PFD State Diagram / 251
 - 10.3.4 PFD s -Curve / 252
 - 10.3.5 Frequency Detection in a PFD / 253
 - 10.3.6 Effects of Delay in a PFD / 254
 - 10.3.7 Extra or Missed Transitions / 255
 - 10.3.8 Lock Indicator for a PFD / 256
- 10.4 Behavior of Phase Detectors in Noise / 256
 - 10.4.1 Bandpass Limiters / 256
 - 10.4.2 Phase-Detector Noise Threshold / 258
 - 10.4.3 s -Curve Shape in Noise / 259
 - 10.4.4 Jitter Dependence on s -Curve Shape / 260
- 10.5 Two-Phase (Complex) Phase Detectors / 260
 - Appendix 10A: Phase Modulation Due to Phase-Detector Ripple / 262
 - 10A.1 Ripple Model / 262
 - 10A.2 Basis of Analysis / 263
 - 10A.3 Ripple Examples / 263
 - 10A.4 Ripple Filters / 264
 - References / 265

11 LOOP FILTERS**267**

- 11.1 Active vs. Passive Loop Filters / 267
- 11.2 DC Offset / 268
- 11.3 Transient Overload / 269
 - 11.3.1 Overload from PD Ripple / 269
 - 11.3.2 Overload During Acquisition / 269

12 CHARGE-PUMP PHASELOCK LOOPS**271**

- 12.1 Model of a Charge Pump / 271
- 12.2 Loop Filter / 273

- 12.3 Static Phase Error / 274
- 12.4 Stability Issues / 275
- 12.5 Nonlinearities / 276
- 12.6 Ripple Suppression / 278
- 12.7 Late Developments / 280
- References / 281

13 DIGITAL (SAMPLED) PHASELOCK LOOPS

282

- 13.1 QuasiLinear Sampled PLLs / 283
 - 13.1.1 Digital-Controlled Oscillators / 283
 - 13.1.2 Hybrid Phase Detectors / 286
 - 13.1.3 Complex-Signal Digital Phase Detector / 289
 - 13.1.4 DPLLs in Digital Data Receivers / 290
 - 13.1.5 Loop Stability / 294
- 13.2 Quantization / 294
 - 13.2.1 Lessons from Related Studies / 294
 - 13.2.2 Quantization Considerations in Hybrid PLLs / 295
 - 13.2.3 Effects of Frequency (NCO) Quantization / 296
 - 13.2.4 Quantization in a Phase Detector and an Integrator / 311
- 13.3 Irremediably Nonlinear PLLs / 312
 - 13.3.1 Configuration of a Nonlinear PLL / 312
 - 13.3.2 Operation of the PLL Elements / 314
 - 13.3.3 PLL State Diagrams / 317
 - 13.3.4 Operation of the Nonlinear PLL / 319
 - 13.3.5 Type 2 Nonlinear PLL / 322
 - 13.3.6 Effects of Additive Noise / 324
 - 13.3.7 Application to Bit Synchronizers / 326
- Appendix 13A: Transfer Function of a Multirate DPLL / 327
 - 13A.1 Nomenclature / 327
 - 13A.2 Phase-Detector Operation / 327
 - 13A.3 Accumulate & Dump and the Loop Filter / 327
 - 13A.4 Hold Process / 328
 - 13A.5 NCO, Phase Rotator, and $M:1$ Down-Sampling / 329
 - 13A.6 Transfer Functions / 330
 - 13A.7 Transfer Function of a Hold Filter / 332
 - References / 333