R. Eckmiller, Editor

ADVANCED NEURAL COMPUTERS

North-Holland

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PREFACE

This book is the outcome of the International Symposium on Neural Networks for Sensory and Motor Systems (NSMS) held in Neuss (near Düsseldorf (FRG)) from 22 to 24 March, 1990.

The NSMS symposium assembled 45 invited experts from Europe, America, and Japan representing the fields of Neuroinformatics, Computer Science, Computational Neuroscience, and Neuroscience.
More than 150 additional scientists from various countries representing a number of research institutes and companies with interest in neural computing participated in the discussions and made poster presentations.

The 45 invited contributions in this book are arranged in six sections ranging from Biological Sensory and Motor Systems via Theory of Artificial Neural Networks and Neural Network Simulators to Pattern Recognition and Motor Control with Artificial Neural Networks.

The readibility of this book was enhanced by a number of measures:

* The invited papers are arranged in six sections.
* The collection of References from all Contributions provides an alphabetical list of all references quoted in the individual contributions.
* A separate List of General References serves newcomers in this field to find other recent books.
* Separate Author and Subject Indices facilitate access to various details.

It is hoped that this book as a rapidly published report on the 'State of the Art in Neural Computing' and as a reference book for future research in the highly inter-disciplinary field of 'Theory and Applications of Neural Computers' will provide useful in the endeavour to: *Transfer Concepts of Brain Function and Structure to Novel Neural Computers with Adaptive, Dynamical Neural Net Topologies.*

The editor wishes to thank Claudia Berge, Miriam Buck, and Sandra Winter for their efficient and thorough technical and managerial assistance, which was essential to meet the tight deadline for preparation of the final book manuscript.
The subsequent expert work of the publisher made it possible to make this book available in high quality within less than four months after the NSMS symposium.

Düsseldorf, June 1990 The Editor

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Section 1
General Introduction

Advanced Neural Computers / R. Eckmiller (Editor)

Prolegomena to an Analysis of Form and Structure

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I. INTRODUCTION

1. - This title is meant as an expression of realistic humility, in front of problems whose extension and depth I deem to be much beyond our present grasp. As an example, the task of understanding in full the structure of English or Japanese, and of making an acceptable translation from one into the other, appears of a magnitude comparable to that of the study of cerebral activity. This was in fact the reason that prompted our first researches on the subject in the early 60's [1,2]: our purpose was to learn something about the latter by studying the "produce" of the brain, conceived as a biological machine (almost a heresy at that time) whose inner workings we had just started modeling with mathematical equations describing Neural Nets and their learning mechanisms.

Our methodological approach provided several insights, which were, when possible, subjected to computer analyses (of texts in several languages) that well corresponded to our expectations, thus stimulating further researches, still under way. Implementation with Neural Nets is being also considered, but will not be discussed here. I present it, in sketchy outline but with several improvements with respect to earlier studies, because I think it paradigmatic for many problems of interest to us. E.g., a robot may be described by specifying the "translation" it performs from a "sensory" to a "motor" language: a problem for which the appellative "prolegomena" given to these considerations seems not inappropriate. They may be taken, in a generalized sense, to belong to "mathematical linguistics". The major difference between most approaches in this area and ours is that we consider the language which we happen to study as our "universe", which we treat as a physicist does with his: he cannot change it at will and is forbidden from making a priori assumptions on its laws. Likewise, we demand that what structures, grammars, etc. may exist in a "language" must be found by applying a systematic methodology, not postulated as already known.

The major conceptual difference from earlier works is given by our refounding the whole approach on properties of the Kullback-Leibler entropy. Basic notions become more perspicuous and rigorous, some statements proposed before as heuristic become mathematical corrolaries.
We name this improved version "Procrustes II", since our previous work was called

"Procrustes" (after the name of the first theorist in our history)

2.- The "form of an object is understood as a quality bestowed upon it by the "observer" (a typical Kantian phenomenon). It includes "pattern", "image", etc. . "Form" is thus a "set property"; the "observer" is defined in turn through the set of elements stipulated by him to have the same form (e.g. according to weight, colour, shape, nutritional value...) . It is well known that a "set consisting of a single element" is a quite different object from that single element alone: the difference is the observer! This raises profound system-theoretical questions (think also of Quantum Mechanics), which will not concern us here. The operation performed by the observer when defining a form coincides with "abstraction", typical, in our approach, of learning neural nets [3]. Iteration of this operation creates hierarchies and heterarchies of sets, or forms, or "features" (as such partial sets are often called when seen from a higher level). The study of this global process we call "Structural Analysis". Considerations which we do not report here [4] show that it involves usually a "Quantification" into the discrete (and finite) domain (think of our "seven" notes or colours as contrasted with the underlying physical continuum). We shall assume, as starting point, that the objects we deal with are quantified, either naturally or because of some preliminary pre-processing.

We propose to analyze structures as "nested sequences of substructures". The analogy with a typed linguistic text is cogent; we shall use, proceeding "bottom-up", the words "letter", "syllable", word",...
This may be misleading, because it implies an underlying "linear dimension" as for a typwritten text, i.e. the existence of "complete ordering" relations, which may well not be"natural" in the analysis, say, of pictures. In such cases we assume, for the purpose of the present discussion, such relations to be the result of some prescription, as always possible in the discrete: think of TV scanning, or of the saccadic eye movements of Yarbus. By so doing, we deal in fact with the most complex situation, that of "strings" of elements in which "order" is essential; suppression of order would simplify our treatment into that of "clusters", an easier task not treated here (it would imply a reconsideration of the "codes" discussed next).

3.- We shall call henceforth "language" a given (extensively or potentially, finite or infinite) set of "texts" written in terms of "letters" of an "alphabet" A (e.g. English letters, or Kanji and Kana). Our attention will be concentrated on a single text T (the addition of more texts will enrich later our knowledge). A "code" is a collection of strings (code words) of letters of A. We defined [5] a code "closed" if "left cancellation" of a code word gives again a code word: thus, if $a_1a_2a_3$ is a code word , a_2a_3 and a_3 are also code words .

"Natural codes" are defined as those which contain "terminal letters": in our analysis a subset of them, "closed natural codes" (CNC), will play a relevant role.

"Instantaneous codes" are the subclass of "uniquely decipherable codes" for which the end of a code word is recognizable without exploration of the next letter. We defined "closed instantaneous codes" (CIC) the subclass of instantaneous codes which is closed under left cancellation, except that it does not contain as words suffixes which have code words as prefixes: thus $a_1a_2a_3a_4$; a_3a_4; a_3a_2; a_2; a_4 is a CIC (the suffix $a_2a_3a_4$ is forbidden). CIC's contain terminal symbols also within their code words, and are thus wider than CNC's, in terms of which they can be further analyzed.

The interest of CIC and CNC lies for us in the fact that our algorithm was proved to converge always to one of these two codes (applications to texts written with other types of codes prove this assertion; for a discussion, see ref. [5])

II - Preliminary Remarks

1.- Two main topics are relevant for our structural analysis:

- frequency count;

- search for individual structures, no matter how rare.

We have restricted our attention only to the second, which presented the greater challenge and is a necessary pre-requisite for the first; a study of texts in various languages, especially Italian, substantiated our conclusions. There is of course no doubt that both topics are important in a complete analysis of the type we propose.

2.- Our search for structural levels has to meet two basic demands:

- finding, proceeding bottom-up, a hierarchy of nested substructures, none excluded, in terms of which our texts may be fully described;

- destroying the evident influence of higher structures on the distribution of lower ones. (One may read thus most of Italian literature without ever meeting the word "soqquadro", which denotes a situation of "total upsetting wantonly created", and is the only Italian word to have the sequence "qqua"; yet this string cannot be ignored by our search!)

The second is easily answered at the first two steps:

- transition from the study of "language" to that of a single "text" T .

- transition from the text T to the corresponding "reduced text", or vocabolary, W , which contains each word of T only once.

The latter is paradigmatic for our procedure; the reader may compare our approach, for analogies and differences, with C. Shannon's celebrated analysis of English. Assume level "1" to be given by the alphabet letters (because given, or as a higher level from some binary, or Morse, code); call level "K" that given by all the words of the reduced text W . Think now of two sets of B. Russell's monkeys, one with letter-keyboards, the other with word-keyboards: the first will reproduce all that we want and can of structure at level "1", the second at level "K". How the destruction of the damaging influence of higher levels comes about is quite clear in both cases.

3.- Our aim is to obtain, at whatever levels may exist between "letters" and "words", this same result. It suffices to consider only one intermediate level between the two just named, that of "syllables". It is the old problem of "parsing", when no indications are elicitable from the text on how to divide words into syllables. We can replace monkeys with semigroup theory: we demand that our "syllables", if written as strings of alphabet letters, generate a "submonoid" (that covers W) which is a "free submonoid" of the monoid generated by the letters. Our algorithms must therefore automatically, on reading the text, retrieve the generators of the free submonoid that is smaller than the monoid generated by letters and larger than that generated by words. (We have assumed just one intermediate level, but the extension to whole hierarchies should be evident).

III - Information as Kullback-Leibler Entropy

1.- Our purpose is not to repeat statements and proofs already available in the references, but rather to "distill" out of them, with greater mathematical clarity than was then possible, the crucial points that we deem of value for further investigation; the result ought to be a vast improvement, because the use of "conjectures" then made, turned now into legitimate mathematical statements, will allow great gains in computational speed.

We only discuss here, as an illustration, the paradigm "letter - syllable - word" just quoted. If we denote A* the monoid generated by the alphabet A,
we propose to find a set of syllables S such that:

$A^* \sqsupset \; S^* \sqsupset \; W^*$ (in the strong sense, or else there is no intermediate level between A and W).

2.- We are interested in structures, not in frequencies. We build therefore at each stage probability schemes of "microcanonical" type, as follows. Our search for S must start and stop automatically (words are assumed to have a finite maximal length); it proceeds, by iteration, through the construction of "intermediate provisional alphabets" containing letters, digrams, trigrams..., until the previous alphabet is identically reproduced. It constitutes the wanted S : our procedure, explained next, guaranties that S is a CNC or a CIC.

Call X_α a string of (one or more) letters, y_h the letter next to it at right in the word. Call $p(X_\alpha y_h)$ the probability (to be specified later) that the string $X_\alpha y_h$ exists in W. Consider then the marginal probabilities

$$p(X_\alpha) = \Sigma_h \; p(X_\alpha y_h), \qquad p(y_h) = \Sigma_\alpha \; p(X_\alpha y_h)$$

and the conditional probabilities

$$p(y_h / X_\alpha) = p(X_\alpha y_h) / p(X_\alpha);$$
$$p(X_\alpha / y_h) = p(X_\alpha y_h) / p(y_h);$$

form the entropies

$$H(Y) = -\Sigma_h \; p(y_h) \log p(y_h)$$

$$H(Y / X \;) = -\Sigma_h \; p(y_h / X_\alpha) \; \log p(y_h / X_\alpha)$$

$$H_X(Y) = \Sigma_\alpha \; p(X_\alpha) H(Y / X\alpha) \qquad \text{(equivocation)}$$

and from them the "mutual information", or "divergence", or "Kullback-Leibler entropy" (all synonims; the last concept is the most interesting for us, as it implies a "measure" of how near we are to our aim):