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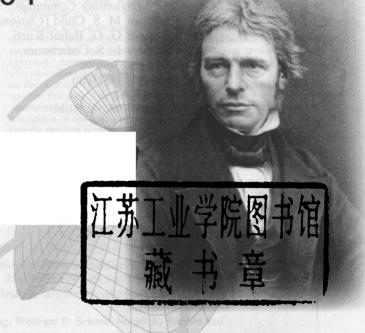
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Non-Adiabatic Effects in Chemical Dynamics

Non-Adiabatic Effects in Chemical Dynamics

University of Oxford April 5–7, 2004

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Non-Adiabatic Effects in Chemical Dynamics

A General Discussion on Non-Adiabatic Effects in Chemical Dynamics, was held at the University of Oxford, UK on 5th, 6th and 7th April 2004.



Cover

See W. Fuß, W. Rettig, W. E. Schmid, S. A. Trushin and T. Yatsuhashi, p. 23.

To describe how an electronically excited molecule finds its way to a lower state, the traditional approach assumed a vertical transition, governed by matrix elements and densities of states. The more modern "pathway approach" assumes large distortions of the molecule, usually connected with photochemical reactions, and tries to follow the path of a wave packet on the potential energy surfaces. Femtosecond spectroscopy allows us to monitor this path. The last slope often (also in the given case) stimulates vibrations in the final potential well. If they are identified, they give a component of the reaction coordinate. The investigated case is a charge-transfer reaction between two excited states. The arrows show, after passing through a conical intersection, branching of the path, one branch making a detour (right-hand side) via the charge-transfer state; vibrations are observed in the final potential well that has double minima along two coordinates.

Image kindly supplied by Dr Werner Fuß, Max-Planck-Institut für Quantenoptik, Garching, Germany.

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Introductory lecture: Nonadiabatic effects in chemical dynamics

Ahren W. Jasper, Chaoyuan Zhu, Shikha Nangia and Donald G. Truhlar

Department of Chemistry and Supercomputing Institute, University of Minnesota, Minneapolis MN 55455-0431, USA

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Recent progress in the theoretical treatment of electronically nonadiabatic processes is discussed. First we discuss the generalized Born-Oppenheimer approximation, which identifies a subset of strongly coupled states, and the relative advantages and disadvantages of adiabatic and diabatic representations of the coupled surfaces and their interactions are considered. Ab initio diabatic representations that do not require tracking geometric phases or calculating singular nonadiabatic nuclear momentum coupling will be presented as one promising approach for characterizing the coupled electronic states of polyatomic photochemical systems. Such representations can be accomplished by methods based on functionals of the adiabatic electronic density matrix and the identification of reference orbitals for use in an overlap criterion. Next, four approaches to calculating or modeling electronically nonadiabatic dynamics are discussed: (1) accurate quantum mechanical scattering calculations, (2) approximate wave packet methods, (3) surface hopping, and (4) self-consistent-potential semiclassical approaches. The last two of these are particularly useful for polyatomic photochemistry, and recent refinements of these approaches will be discussed. For example, considerable progress has been achieved in making the surface hopping method more applicable to the study of systems with weakly coupled electronic states. This includes introducing uncertainty principle considerations to alleviate the problem of classically forbidden surface hops and the development of an efficient sampling algorithm for low-probability events. A topic whose central importance in a number of quantum mechanical fields is becoming more widely appreciated is the introduction of decoherence into the quantal degrees of freedom to account for the effect of the classical treatment on the other degrees of freedom, and we discuss how the introduction of such decoherence into a self-consistent-potential approximation leads to a reasonably accurate but very practical trajectory method for electronically nonadiabatic processes. Finally, the performances of several dynamical methods for Landau-Zener-type and Rosen-Zener-Demkov-type reactive scattering problems are compared.

1 Introduction

Electronically nonadiabatic processes (also called non-Born-Oppenheimer or non-BO processes) are defined as those in which the electronic state changes nonradiatively during the dynamical event. Electronically nonadiabatic processes are essential parts of visible and ultraviolet photochemistry, collisions of electronically excited species, chemiluminescent reactions, and many recombination reactions, heterolytic dissociations, and electron transfer processes. Often electronic

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excitation energies are much greater than the energies of nuclear motions, and electronically excited species have different valence properties than ground-state species; consequently electronically activated chemical systems may have dynamical mechanisms significantly different from those of thermally activated systems.

The Born-Oppenheimer (BO) separation of electronic and nuclear motions and the use of classical mechanics to model the nuclear part of the problem have allowed for the development and successful application of a variety of theoretical electronic structure¹ and dynamics² methods designed for the electronically adiabatic case where the entire effect of the electronic subsystem is embedded in a potential energy surface that governs nuclear motion. The generalization of these theoretical methods to handle non-BO events adds new considerations and often significantly increases the computational demands of the calculation. From the point of view of the electronic subsystem, the computation of excited-state electronic wave functions and energies usually requires an open-shell formalism and expanded basis sets, and a consistent treatment of the active space is required in configuration interaction calculations.³⁻⁸ Furthermore, computing the couplings between the electronic states requires specialized methods, and the electronic couplings are singular, rapidly varying, high-dimensional vectors. From the point of view of the nuclear subsystem, the treatment is complicated by the need to consider a different potential energy surface for each electronic state and transitions between these surfaces. When conical intersections are present. nuclear motion on the adiabatic surfaces also involves geometric phases. 10,11 Although great progress has been made in the quantum mechanical treatment of nuclear motion on coupled potential energy surfaces, the practical treatment of systems with a large number of nuclear degrees of freedom is greatly facilitated by using classical mechanics. Since the light mass and antisymmetry requirements of the electrons preclude a classical treatment, one then requires a semiclassical treatment that combines quantum mechanics for the electron motion with classical mechanics for the nuclear motion. A particularly subtle issue that reaches to the heart of the probabilistic interpretation of quantum mechanics¹² (sometimes called quantum information theory or quantum measurement theory) is the loss of coherence in the quantal (electronic) subsystem due to its intersection with the classical subsystem (i.e., nuclear motion). ^{13–15} In recent work, considerable progress has been made in sorting out these issues, and we can now present a more satisfactory theory than was possible a few years ago.

A brief theoretical discussion is presented in Section 2. In Sections 3–5, recent progress in the theoretical treatment of non-BO chemistry is discussed along three related lines: the calculation of potential energy surfaces and their couplings (Section 3), the development of methods for computing accurate quantum mechanical scattering dynamics (Section 4), and the testing, application, and systematic improvement of semiclassical methods for simulating non-BO dynamics (Section 5). Section 6 is a summary.

Although the specific examples considered in the present paper are processes initiated by collisions, the methods are general and can also be applied to unimolecular processes.

2 General theoretical considerations and definitions

The Hamiltonian for a molecular system may be written

$$H(\mathbf{R}, \mathbf{r}) = T_{\mathbf{R}} + H_{e}(\mathbf{R}, \mathbf{r}), \tag{1}$$

where R and r are vectors of the nuclear and electronic coordinates, respectively, T_R is the nuclear kinetic energy operator, and H_e is the electronic Hamiltonian, which contains the electronic kinetic energy operator and all Coulomb interactions, as well as the spin-orbit interaction if appropriate.

Some chemical systems may be modeled adequately within the framework of the Born-Oppenheimer (BO) approximation. $^{16-19}$ This approximation recognizes the large mass disparity of nuclei and electrons and allows their different-time-scale motions to be decoupled. Nuclear motion is then governed by a single BO potential energy surface V, which describes the variation of the ground-state electronic energy with changes in the nuclear geometry, *i.e.*, the ground-state nuclear wave function ψ_0 solves the equation,

$$[T_{\mathbf{R}} + V(\mathbf{R}) - E]\psi_0(\mathbf{R}) = \mathbf{0}, \tag{2}$$

$$V(\mathbf{R}) = \langle \phi_0 | H_e(\mathbf{R}, \mathbf{r}) | \phi_0 \rangle_{\mathbf{r}}, \tag{3}$$

 T_R is nuclear kinetic energy, H_e is the rest of the Hamiltonian, E is total energy, ϕ_0 is the ground-state electronic wave function, and the integration in eqn. (3) is over the electronic coordinates r.

For non-BO processes, more than one electronic state is important in the overall dynamics, and the single-surface treatment described by eqn. (2) is qualitatively incorrect. A proper theoretical framework may be developed in terms of a basis set of electronic wave functions ϕ_i , where *i* labels the electronic states, and optionally (but not necessarily) one may choose this basis so that ϕ_0 has the same meaning as above. By analogy with the BO approximation, one may define potential energy surfaces for each electronic state, *i.e.*,

$$V_{ii}(\mathbf{R}) = \langle \phi_i | H_e(\mathbf{R}, \mathbf{r}) | \phi_i \rangle_{\mathbf{r}}, \tag{4}$$

as well as off-diagonal matrix elements of the electronic Hamiltonian, which are in general non-zero.

$$V_{ii}(\mathbf{R}) = \langle \phi_i | H_e(\mathbf{R}, \mathbf{r}) | \phi_i \rangle_{\mathbf{r}}. \tag{5}$$

By expanding the multi-state wave function Ψ in terms of the electronic basis, i.e.,

$$\Psi(\mathbf{R}, \mathbf{r}) = \sum_{i} \phi_{i}(\mathbf{R}, \mathbf{r}) \psi_{i}(\mathbf{R}), \tag{6}$$

one obtains a set of coupled equations analogous to the BO result in eqn. (2), 20-22

$$\left[T_{R} + V_{ii}(\mathbf{R}) + T_{ii}^{(2)}(\mathbf{R}) - E\right]\psi_{i}(\mathbf{R}) = -\sum_{j \neq i} \left[T_{ij}^{(1)}(\mathbf{R}) + T_{ij}^{(2)}(\mathbf{R}) + V_{ij}(\mathbf{R})\right]\psi_{j}(\mathbf{R}),\tag{7}$$

where

$$T_{ij}^{(1)} = \frac{-\hbar^2}{2\mu} \left\langle \phi_i | \nabla_R | \phi_j \right\rangle \cdot \nabla_R = \frac{-\hbar^2}{2\mu} d_{ij} \cdot \nabla_R, \tag{8}$$

$$T_{ij}^{(2)} = \frac{-\hbar^2}{2\mu} \left\langle \phi_i | \nabla_R^2 | \phi_j \right\rangle, \tag{9}$$

 μ is the reduced mass for the nuclear system, and ∇_R is the nuclear gradient operator. The terms in eqns. (8) and (9) arise from the action of the nuclear momentum and kinetic energy operators on electronic basis functions and may be called the "momentum" and "kinetic energy" nonadiabatic coupling terms, respectively. Note that $T_{ii}^{(1)}$ is zero because d_{ij} is anti-Hermitian, and $T_{ij}^{(2)}$ (for both i=j and $i\neq j$) is often neglected. The matrix elements of the nuclear gradient operator d_{ij} are called nonadiabatic coupling vectors, and $T_{ij}^{(1)}\psi_j$ is called a nonadiabatic coupling term (NACT).

Eqn. (7) shows that nuclear motion in each electronic state is governed by the potential energy surface associated with that state as well as the various coupling terms in eqns. (5), (8), and (9). The situation may be simplified somewhat by making certain choices for the electronic basis. If the electronic basis is chosen such that V_{ij} is diagonal, the nuclear motion is coupled only by the action of the nonadiabatic coupling terms in eqns. (8) and (9). This choice for the electronic basis is called the adiabatic electronic basis. Another choice for the electronic basis that is often useful is called the diabatic electronic basis. It is sometimes possible to rotate the electronic states in electronic state space (via a unitary transformation) to obtain a diabatic representation where the nonadiabatic couplings are small enough (for many purposes) to neglect. In the diabatic representation, the electronic Hamiltonian is no longer diagonal, and the nuclear motion is coupled by the diabatic or scalar coupling shown in eqn. (5). Alternatively, one can define or calculate approximate potentials in a diabatic representation and obtain the adiabatic representation by diagonalization of the potential energy matrix V_{ij} , and in that case, if no approximations are made, the adiabatic and diabatic electronic representations yield identical results.

In general, an adiabatic-to-diabatic transformation that makes all of the components of d_{ij} zero is not possible. ^{45,46} Useful diabatic representations may be developed that minimize these terms

or—more generally—that make them small enough to be neglected, and these are often called quasidiabatic representations to emphasize the approximations involved, but we and many others call them diabatic with the understanding that strictly diabatic representations do not exist. It has been shown⁴⁷ that in regions far from conical intersections, although one cannot make the NACTs zero, one can make their effect as negligibly small as for cases where the Born–Oppenheimer approximation is valid.

Finally, it is often possible to restrict theoretical attention to a subset of important electronic states which may be strongly coupled to one another but are only weakly coupled to all of the other electronic states. This procedure is called the generalized Born–Oppenheimer approximation. ^{47,48}

3 Coupled potential energy surfaces

In many theoretical treatments, the first step in modeling a non-BO system is the development of analytic expressions for the potential energy surfaces in eqn. (4) and their couplings. As discussed above, there are two possibilities for representing a set of coupled potential energy surfaces, the unique adiabatic representation or a nonunique diabatic one. They each have strengths and weaknesses. Some strengths of the adiabatic representation are that it is well defined, it lends itself well to using variational and perturbation theory methods to calculate it by electronic structure theory, it often provides a good zero-order picture when the coupling is neglected, and in principle it provides a basis for exact treatments. The diabatic picture, in contrast, inevitably neglects some coupling (because a "strict" diabatic basis does not exist) and is not unique, although it too sometimes provides a good zero-order picture when coupling is neglected. For large systems (organic photochemistry, photocatalysis, etc.) the rigor of the adiabatic representation is not so important, and in fact even for systems with 4–10 atoms, a rigorous treatment is usually not the goal. Therefore it may be very attractive to use a diabatic representation in which the coupling caused by the electronic Hamiltonian dominates the coupling due to nuclear kinetic energy so that the latter may be neglected for practical calculations.

The diabatic representation has an important advantage that increases in attractiveness as systems get large, namely that the coupling is a scalar. For three coupled surfaces, there are three scalars, one coupling surface 1 to surface 2, another coupling 2 to 3, and the third coupling of 1 to 3. In contrast specifying the nonadiabatic coupling requires three 3N-6 dimensional vectors, where N is the number of atoms. Furthermore the diabatic surfaces and couplings are smooth, whereas the adiabatic surfaces have conical intersections and avoided crossings, and the nonadiabatic coupling is often rapidly varying and has singularities, and it requires special attention to consistent treatment of the origin $^{49-52}$ and long-range effects. 50,53,54

For these reasons there has been interest in developing practical methods for working with diabatic representations, and considerable progress was made in this direction. We particularly single out for discussion a new approach called the fourfold way. 43,55,56 The fourfold way allows for the direct calculation of diabatic states and their couplings using the conventional variational and perturbational methods of quantum chemistry. This is particularly important because diabatic representations used for dynamics calculations should not be based on an arbitrary selection of configurations. Rather the variational principle should be used to optimize the space spanned by the strongly coupled electronic state vectors, then the electronic configuration space should be transformed to one that in some sense minimizes the nuclear momentum coupling, at least in regions where the nonadiabatic coupling is large. The fourfold way is designed to accomplish this process in a general way, but the method still requires care that is commensurate with the care required to treat ground-state problems by multi-configuration self-consistent-field methods, which can be chancy. This is not surprising because electronically nonadiabatic photochemistry intrinsically involves open-shell systems, and such systems do not lend themselves to black box approaches. The fourfold way has been developed for configurational wave functions based on complete active space multi-reference Møller-Plesset second order perturbation theory⁴ (CAS-MRMP2) and complete-active-space multi-configuration quasi-degenerate perturbation theory⁵ (CAS-MC-QDPT). The extension to the MC-QDPT version is particularly important because this is a perturb-then-diagonalize approach in which

an effective Hamiltonian is formed by perturbation theory and then diagonalized. This allows the method to be valid for nearly degenerate states and even for truly degenerate states. (Isolated pathologies are possible but should not prevent useful applications of the method for dynamics.)

A key element in the fourfold way is that the diabatic systems are defined by a unitary transformation of ab initio adiabatic states, where the transformation 36,43 is based on configurational uniformity. (Such a transformation has also been used fruitfully by other workers, based on other criteria.^{37,42}) In order for this to produce useful diabatic states, it is necessary to first re-express the configuration state functions (CSFs) in terms of diabatic molecular orbitals (DMOs), and these are produced by the fourfold way. The essential step in using the fourfold way to obtain DMOs is maximizing a three-parameter functional that involves the sum of the squares of the orbital occupation numbers for all of the states, a state-averaged natural orbital term. 38 and a transition density term. (The DMOs do not depend on tangentially related constructs such as one-electron properties.²⁹) This threefold density criterion is often sufficient, but not in strong interaction regions for excitation from an open shell. In such regions we require the fourth element, which involves maximizing the overlap of one orbital with a reference molecular orbital. The fourfold way is effective at producing diabatic orbitals even in cases where a maximum overlap criterion 35 applied to all orbitals fails. The resulting diabatic orbitals are globally defined and unique (pathindependent) if the dominant configurations and weak coupling regions can be defined unambiguously. The method is general enough to allow for dominant CSF groups to have completely different members in different arrangements, and all ambiguities involving orbital and molecular orientation are solved by specific prescriptions or the introduction of resolution molecular orbitals.

Diabatic representations, with all their advantages for gas-phase processes, are also useful for

condensed-phase photochemistry.44

Although these developments make the generation of diabatic representations more automatic, in some cases there may be practical advantages in working directly in the adiabatic representation because it altogether avoids the nonunique transformation to a diabatic representation. Ideally though, the choice between a diabatic and adiabatic representation should be based not on the convenience of generating the potential energy surfaces and their couplings, but rather on which one is more suitable for dynamics. Although accurate quantum dynamics are independent of representation, approximate methods usually depend on representation, and they will tend to be more accurate if one uses the representation with the smallest coupling between the surfaces; this is problem dependent and the best choice may also be method dependent. Thus two important questions emerge: (1) how can we determine, for a given system and a given approximate dynamics method, which representation will yield the most accurate results; (2) can we develop improved methods that are less dependent on representation than previously existing semiclassical methods? Both questions are addressed in Section 5.

4 Quantum mechanical dynamics

Once an analytic representation for the potential energy surfaces and their couplings is obtained (in either the adiabatic or diabatic representation), one may proceed to modeling or calculating the non-BO dynamics. Quantum mechanical calculations are especially challenging for non-BO systems both because there are open channels on more than one potential energy surface and also because, for typical energy gaps, the kinetic energy is high on at least one surface.

For chemical systems with three or four atoms and two electronic states, the dynamics may be calculated using accurate quantum mechanical techniques. The method that we use to calculate accurate transition probabilities is time-independent quantum mechanical scattering theory. In these calculations we assume that a particular two-state diabatic representation of the potential energy surface is exact, and we neglect electronic angular momentum. After those two assumptions, the rest of the treatment is exact, that is, numerically converged to two or three significant figures. The calculations employ the outgoing wave variational principle forms (OWVP). The OWVP method, as we employ it, is particularly efficient because it divides the scattering problem into two smaller problems. The Schrödinger equation is solved by expanding the outgoing scattering waves in terms of internal-state channel functions for each asymptotic chemical arrangement. (A channel

is defined by a set of quantum numbers, including the arrangement number, that characterizes the state of the completely dissociated reactant or product fragments.) The full Hamiltonian for each chemical arrangement is partitioned into a distortion Hamiltonian that contains some of the channel-channel coupling and causes rotationally-orbitally inelastic scattering and a coupling potential that contains the remainder of the channel-channel coupling. The solutions to the former are called distorted waves. The deviation of the accurate wave function from the distorted-waves is expanded in a basis set consisting of L^2 functions and half-integrated distorted-wave Green's functions (HIGFs), and the deviation of the full scattering matrix from the part contributed by the distorted-waves is obtained by making it stationary with respect to variations of the coefficients of the L^2 basis functions and the HIGFs. The L^2 functions are sums of products of Gaussians. spherical harmonics, and diatomic eigenfunctions. The HIGFs are dynamically optimized by solving the distorted-wave problems on a finite difference grid as nonhomogenous coupled ordinary differential equations with two-point boundary conditions and with the quadrature grid for the matrix elements of the OWVP being a subgrid; this is more stable than forming the Green's functions from irregular solutions, and it avoids working with discontinuities or interpolation. Using this two-step scheme, the full scattering matrix is written as the sum of two terms, where the first term is the distorted-wave Born approximation for the scattering matrix obtained using the distorted-wave functions, and the second term is the contribution from the coupling potential.

The steps in the accurate calculations are therefore: (1) decouple the problem into small blocks in single chemical arrangements; (2) solve these multi-channel nonreactive problems to obtain partially coupled HIGFs; (3) calculate intra-arrangement and inter-arrangement matrix elements of the L^2 basis functions and HIGFs; (4) solve a dense matrix problem for the coefficients of the L^2 basis functions and HIGFs.

Several computational refinements are used to make the calculations efficient: (1) The grids used in the initial finite difference step are unevenly spaced so the subgrids used for later quadratures have efficient Gauss–Legendre node spacings. (2) High-order finite difference schemes are used. (3) The intra-arrangement integrals are re-calculated as needed to keep storage manageable (a so called "direct" algorithm). (4) The problem, including boundary conditions, is formulated in a molecule-fixed frame, which allows one to limit the basis set to small values of the body-frame angular momentum projections. (5) The problem is formulated with real boundary conditions and hence real arithmetic until the last step, where complex scattering matrix boundary conditions are used to avoid spurious singularities in the variational principle. (6) In calculating matrix elements, we prescreen both integrals and quadrature points to eliminate unnecessary work.

The OWVP method has been used to obtain fully-converged quantum mechanical scattering results for a variety of electronically nonadiabatic chemical systems. The initial such application was the nonreactive quenching process Na(3p) + H₂ \rightarrow Na(3s) + H₂ for zero⁶²⁻⁶⁵ and unit⁶⁵ total angular momentum using a two-state representation of the NaH₂ system. Accurate quantum mechanical calculations were also carried out⁶⁶ for the spin-orbit-coupled collisions H + HBr \rightarrow H₂ + Br(2 P_{1/2}) and H₂ + Br(2 P_{3/2}). The competition between electronically nonadiabatic reaction and electronic-to-vibrational energy transfer was investigated for the Br(2 P_{1/2}) + H₂ \rightarrow HBr + H reaction. ⁶⁷ Calculations for a series of three-body model systems exhibiting avoided crossings in the vicinity of the reaction barrier showed strong nonadiabatic effects on reaction probabilities due to funnel resonances. ⁶⁸ OWVP calculations have been performed more recently on a variety of model systems, including three qualitatively different types of chemical systems: (1) systems with conical intersections, ⁶⁹⁻⁷³ (2) systems with diabatic surfaces that cross and adiabatic surfaces that do not intersect, ⁷⁴ and (3) systems with wide regions of weak coupling where neither the diabatic nor the adiabatic surfaces cross. ^{75,76} This set of calculations includes reactive ^{69,72,74-76} and nonreactive ^{71,72} scattering collisions as well as unimolecular excited-state decay processes. ^{70,73}

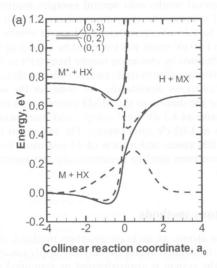
The availability of accurate quantum mechanical results for realistic full-dimensional non-BO systems allows for the systematic study of the accuracy of more approximate methods, and we have identified a subset of the calculations discussed above to serve as benchmark test cases. The systems are defined in the diabatic representation, and the set of diabatic surfaces (eqn. (4)) and their couplings (eqn. (5)) is referred to as a potential energy matrix or PEM. We include three Landau–Zener–Teller-type TPEMs (collectively referred to as the MXH family of PEMs), which feature narrowly avoided crossings where the diabatic surfaces cross but the adiabatic surfaces do not.

The three MXH PEMs differ from one another in the strength and width of their coupling, and all three MXH PEMs describe the reaction

$$M^* + HX \rightarrow \begin{cases} M + HX \\ H + MX' \end{cases} \tag{10}$$

where the excited model metal atom M^* collides with the diatom HX. The system may quench nonreactively to form M+HX or reactively to form H+MX. The masses of the M, X, and H atoms are 6.04695, 2.01565, and 1.00783 amu, respectively. The diabatic and adiabatic energies for one of the MXH systems along the collinear ground-state reaction path are plotted in Fig. 1(a). OWVP calculations with 20659 basis functions were carried out⁷⁴ for all three MXH PEMs at total energies from 1.07 to 1.13 eV.

The second family of PEMs included in the set of benchmark cases is the YRH family, 75 which contains two Rosen–Zener–Demkov-type PEMs, 80–82 featuring wide regions of weakly coupled and nearly parallel surfaces where neither the diabatic surfaces nor the adiabatic surfaces cross.



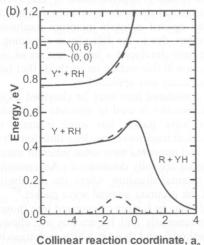


Fig. 1 Adiabatic (solid lines) and diabatic (dashed lines) energies along the collinear ground-state reaction path for (a) one of the MXH systems and (b) one of the YRH systems. The total energies used in the quantum mechanical and semiclassical calculations are shown as dotted lines. The energies of the initial rovibrational states of the diatom used in the set of benchmark test cases are labeled (v, j), where v and j are the vibrational and rotational quantum numbers, respectively. Note: 1 $a_0 = 0.529 \text{ Å}$.

The two YRH PEMs differ from one another in the strength of their coupling and describe the

$$Y^* + RH \rightarrow \begin{cases} Y + RH \\ R + YH' \end{cases} \tag{11}$$

where the excited model metal atom Y* collides with the diatom RH. The masses of the Y. R. and H atoms are 10, 6, and 1.00783 amu, respectively. The diabatic and adiabatic energies for one of the YRH systems along the collinear ground-state reaction path is shown in Fig. 1(b). OWVP calculations with 25269 basis functions were carried out⁷⁵ for both YRH PEMs at total energies from 0.99 to 1.13 eV. The various PEMs are distinguished by the strtength of coupling of the diabats, as measured by a parameter U_{12}^{max} .

Quantum mechanical results often display an oscillatory structure as a function of energy, whereas the approximate methods that we wish to test (which are based on classical theories) do not. In order to eliminate the effect of these oscillations when testing the approximate methods, we average the quantum mechanical results over several energies located around the nominal scattering energy. For the MXH systems, the quantum mechanical result at 1.10 eV was obtained by averaging results from 1.07 to 1.13 eV. Quantum mechanical results for the YRH systems were obtained at two energies: the 1.10 eV result was obtained by averaging results from 1.07 to 1.13 eV, and the 1.02 eV result was obtained by averaging results from 0.99 to 1.05 eV. The OWVP method gives the entire state-resolved scattering matrix, and in order to define a manageable test set, we include a subset of these transitions. Specifically, we consider the scattering dynamics of three initial rovibrational states for the diatom in the MXH systems, two initial rovibrational states for the diatom in the YRH systems at 1.1 eV total energy, and one initial rovibrational state for the diatom in the YRH systems at 1.02 eV total energy. The full set of benchmark quantum results includes 9 MXH cases, 3 YRH cases, and a total of 12 test cases with five different PEMs. The MXH and YRH systems have been used to systematically test several approximate methods, as discussed in the next section.

Semiclassical trajectory methods

For systems larger than a few atoms, an accurate quantum mechanical dynamical treatment is not computationally affordable. One must therefore rely on approximate "semiclassical" methods where the full dynamics of the system is approximated or simplified in some way using classical ideas. 83 Although many semiclassical methods have been proposed and reviewed, 21,48,84-87 few have been systematically tested against accurate quantum mechanical calculations for realistic, fully-dimensional chemical systems, due to the difficulty in obtaining quantum mechanical results. As discussed in Section 4, we have developed a broad test set of atom-diatom scattering calculations, and we focus our attention in this section on methods that have been validated using these test cases to determine their accuracy and applicability.

The semiclassical methods considered here may be classified as trajectory ensemble methods, where a swarm of classical trajectories is used to simulate the nuclear motion of the system. A quantum mechanical nuclear wave packet has some inherent width in configuration and momentum space, whereas classical trajectories are delta functions in phase space. (Equivalently, a quantal particle's coordinates and momenta have some inherent uncertainty or spread, whereas in a classical system these quantities are fully determined.) An ensemble of trajectories is therefore required to approximate the quantal situation, where the distribution of the trajectories in the

ensemble mimics the width of the accurate quantal wave packet.⁸⁷

Trajectory ensemble methods may be further categorized into those in which the entire ensemble of trajectories is treated simultaneously and trajectories are allowed to influence each other's motions (coupled trajectory methods), and those in which each trajectory in the ensemble is treated independently (independent trajectory methods). Several coupled-trajectory methods have been developed. 88-99 Some involve "dressing" a classical trajectory with a shape functions such as a Gaussian, and using the overlap of these shape functions to determine the overall dynamics of the system, and others involve using trajectory-derived ensemble-averaged quantities in the equations of motion.

We note that some of the coupled-trajectory methods are very similar to Gaussian wave packet methods in which the centers of the Gaussians follow classical trajectories. These methods are based on early work by Heller. One method that has been systematically tested is the minimal version of the full multiple spawning method 103,104 (FMS-M). In this method, a number of Gaussian-shaped packets are propagated along classical trajectories, and the trajectories occasionally spawn new wave packets, which propagate on other electronic surfaces. Electronic state density is allowed to flow back and forth between the packets, thus simulating the non-BO event. This method strikes a nice balance between including quantum mechanical effects and maintaining computational efficiency, but because one cannot afford to spawn a complete basis set of wave packets moving in all directions, and because one usually makes approximations that force the wave packet centers to follow classical-like paths, the method does not eliminate some of the arbitrariness (see below) that is most troubling in more classical approaches. Furthermore the propagation of a wave packet is more expensive than the propagation of a trajectory, and, as with all wave packet methods, one must be careful to fully sample phase space, a drawback which significantly raises the cost of wave packet methods for large systems.

Another class of wave packet methods is based on the time-dependent multi-configuration time-dependent Hartree method. ^{105,106} These methods are viewed as approximate quantal methods rather than semiclassical methods and will not be discussed here. Coupled-trajectory methods and multiple spawning methods may be used to study the importance of coherent motions, but their computational cost is higher than independent trajectory methods for full-dimensional systems. We

will focus our attention on independent-trajectory methods.

A non-BO process modeled using classical trajectories may be described as follows: as the ensemble of nuclear trajectories evolves in time, the nuclear motion causes a change in the overall electronic state of the system (*via* the nonadiabatic vector momentum (and possibly kinetic energy) couplings or diabatic scalar potential coupling terms) which in turn results in a new effective potential energy felt by the trajectories, affecting the nuclear motion. This nuclear-electronic interaction is the source of nonadiabatic electronic state changes, and to properly treat these non-BO effects a self-consistent treatment of the nuclear-electronic coupling is necessary (*i.e.*, the electronic and nuclear degrees of freedom must be made to evolve simultaneously). Several methods for modeling this self-consistency within the independent-trajectory approximation have been proposed, and we discuss them next.

The electronic motion along each classical trajectory is obtained by propagating the solution to the electronic Schrödinger equation with the appropriate initial conditions. The solution may be represented in the form of an electronic density matrix ρ , where the diagonal element ρ_{ii} is the electronic state probability for state i, and ρ_{ij} for $i \neq j$ are the electronic state coherences. ^{21,107} If the entire system is described in quantum mechanical language, then ρ is the reduced density matrix obtained by tracing the density matrix of the entire system (electrons and nuclei) over the nuclear degrees of freedom. The Schrödinger equation for the wave function reduces (neglecting $T_{ij}^{(2)}$) to the following equation for the reduced density matrix.

ced density matrix:⁹⁵

$$i\hbar \dot{\rho}_{kj} = \sum_{l} \left(\rho_{lj} F_{lj} - \rho_{kl} F_{kl} \right) \tag{12}$$

where

$$F_{ij} \equiv V_{ij} - i\hbar \dot{\mathbf{R}} \cdot \mathbf{d}_{ij} \tag{13}$$

Each trajectory in the ensemble evolves classically according to Hamilton's equations of motion under the influence of a semiclassical effective potential energy function $V_{\rm SC}$, which must be carefully chosen such that the self-consistency discussed above is maintained. The classical treatment of the nuclear motion is not always a good approximation and may introduce significant errors when, for example, the nuclei are light or the observables of interest are sensitive to the quantization of vibrational energy levels or the phases of the nuclear wave functions, as near thresholds and resonances, respectively. However, this approximation is often very useful, even for problems involving hydrogen.

One may anticipate that a successful semiclassical effective potential energy function V_{SC} will be some function of the potential surfaces, their couplings, and ρ . As discussed above, one can express the electronic potential energies and their couplings in either the adiabatic or diabatic

representations, and these two representations are equivalent if no approximations are made. Several of the semiclassical methods that will be discussed next involve approximations that do not preserve representation independence, and one must choose which representation to use for a given simulation. When this is the case, we will discuss a method for choosing the preferred representation. However, for some non-BO problems it may not be possible to assign a single preferred electronic representation. For example, a system may have two or more distinct dynamical regions which differ in their preferred representation. Therefore, it is desirable to develop semiclassical methods that are accurate in both the diabatic and adiabatic electronic representations.

Several semiclassical algorithms have been proposed with differing prescriptions for $V_{\rm SC}$, and the approaches may be divided into two general categories: (1) time-dependent self-consistent-potential methods, and (2) trajectory surface hopping methods. Each category will be discussed briefly.

Semiclassical time-dependent self-consistent-field (TDSCF) theory provides a general framework for incorporating quantum mechanical effects into molecular dynamics simulations. The semiclassical TDSCF method is also known as the semiclassical Ehrenfest (SE) method, the partially classical Ehrenfest model, 108 the time-dependent Hartree method, the time-dependent self-consistent field method, 9,108,109 the self-consistent eikonal treatment, 110 the hemiquantal method, 111 and mean-field theory. In this article we are especially concerned with the use of this method to treat the problem of vibronic effects, that is, the coupling of electronic and nuclear motions when the Born-Oppenheimer approximation breaks down. We group all methods of this type into a general category that we call self-consistent potential methods. The Ehrenfest method converts this problem to classical molecular dynamics on a time-dependent average potential energy surface that is most appropriate for strong interaction regions but leaves the system in an unphysical final state that corresponds to a quantum superposition of pure states. It is well known that an open quantum system, that is a quantum system interacting with an environment (a "bath"), tends to a statistical mixture¹¹² of final states, not a pure state corresponding to a quantal superposition of final states. The quantum mechanical description of this phenomenon is that the off-diagonal elements (which are called coherences) of the reduced density matrix tend to zero. The zeroing of the off-diagonal elements of the density matrix goes by many names including decoherence, transverse or spinlattice relation, and reduction of the wave packet. This general phenomenon has specific relevance to the present problem because the electronic degrees of freedom may be considered to be an open quantum system in the presence of the bath of nuclear degrees of freedom. Thus the nuclear degrees of freedom decohere the electronic density matrix, and this occurs continuously at a finite rate, not suddenly at a surface hop or a detector. When the coherences (i.e., the off-diagonal elements of ρ) decay, the system becomes a statistical mixture, not a pure state. The system should then evolve like a mixture of systems on the different potential surfaces, and the self-consistent potential for the ensemble of trajectories is then an average of the various potential surfaces. This is where the Ehrenfest method fails because it evolves each trajectory on an average potential (which is different for each trajectory) rather than averaging the evolutions on the individual surfaces. We need to introduce an algorithmic decay of mixing by which the electronic density matrices generating the potential energy surfaces for the individual trajectories each lose their mixed character and become a pure state; this decay of mixing must be stochastic or probabilistic such that the fraction of trajectories propagating on each pure surface is equal, on average, to the probability of observing each pure state in the statistical mixture corresponding to the reduced density matrix. Furthermore not only must the nuclear motion be consistent with the electronic density matrix, but also the electronic density matrix is a function of the nuclear trajectory; that is, the theory must be selfconsistent. This is the physical picture behind the coherent switching decay of mixing 113 (CSDM) algorithm and the earlier self-consistent decay of mixing 114 (SCDM) algorithm. These algorithms introduce continuous decoherence toward a pure state, called the decoherent state, and this pure state is stochastically switched from one to another state in a self-consistent 114 or coherent way along the trajectory. In both algorithms the effective potential for nuclear motion is obtained from the self-consistent electronic density matrix, and in the SCDM this self-consistent density matrix also governs the switching of the decoherent state. However, we have found that for some problems the evolution of the electronic density matrix that governs the switching should be more coherent than the evolution of the electronic density matrix that governs the effective potential for nuclear motion, and making this switching coherent for each complete passage of a region of strong interaction of the electronic states makes the CSDM algorithm¹¹³ more accurate than the earlier¹¹⁴

less coherent algorithm. The switching is not completely coherent throughout the trajectory but rather coherent during each complete passage of the system through a region of strong interaction of the electronic states. At a point of minimum interaction of the electronic states, between strong coupling regions, the electronic density matrix $(\tilde{\rho})$ that governs the switching is re-set to the one (ρ) that governs nuclear motion.

But toward which pure states should the systems decohere, e.g., toward the adiabatic pure states or the diabatic ones? What is the privileged electronic basis in which the density matrix becomes diagonal? The analog of this question in quantal measurement theory is: what is being measured?¹¹⁵ This is clearly determined by the measuring system, which from the point of view of the quantum system, is the environment. In our problem, the environment is the nuclear degrees of freedom. In quantal measurement theory, the privileged basis selected by the environment is called the pointer basis, 115 and it is determined by the interaction Hamiltonian connecting the two subsystems. In the special case where the environment changes slowly on the natural time scale of the quantal system, the pointer basis becomes the adiabatic basis of the quantal system, 116 i.e., it is determined by the quantal system's internal Hamiltonian, not by the system-environment coupling. Thus for systems where the Born-Oppenheimer approximation is a good zero-order description, the adiabatic basis should be the decoherent basis. However, we are interested in systems with strong interactions between the states, i.e., Born-Oppenheimer breakdown, and in such cases it is not easy to determine the pointer basis, although our physical intuition tells us that when the diabatic representation is a good zero-order approximation, the diabatic basis should be the decoherent basis. One problem though is that the pointer basis may be different at different geometries. A key to resolving the dilemma of how to choose the decoherent basis is provided by recalling that the exact quantum mechanical solution is independent of the basis in which the problem is solved. Therefore we seek a method that gives similar results in the two extreme bases, adiabatic and diabatic. Then the choice of decoherent basis will not be so much of a problem because one will get an accurate answer even if one locally makes the wrong choice.

The starting point for mean-field methods is the quantum Ehrenfest theorem ^{117,118} which states that the expectation values of the position and momentum operators evolve according to classical equations of motion with an effective potential energy function given by the expectation value of the potential energy operator. We define the semiclassical Ehrenfest (SE) independent-trajectory method by taking $V_{\rm SC}$ to be the expectation value of the electronic Hamiltonian: ^{9,48,119}

$$V_{\rm SC} = \sum_{i,j} \rho_{ij} V_{ij}. \tag{14}$$

The SE method has the desirable feature that it is formally independent of electronic representation. 119 Unfortunately, the SE method has many more disadvantages that result from the mean-field assumption.⁸⁶ At any instant along an SE trajectory it is physically meaningful for the nuclear motion of a system to be influenced by some average of the potential energies of all of the electronic states. However, it is not physically meaningful for the nuclear motion corresponding to each electronic state to be described by a single trajectory. If the potential energies of the various electronic states are similar in topography and energy, then the nuclear motions in each state will be such that an average SE trajectory may provide a reasonable approximation. For many chemical systems, however, this is not the case, and it is not possible for a mean-field trajectory to accurately approximate the motion in these different electronic states. An important consequence of this arises in the case of low-probability events. An SE trajectory will be dominated by the character of the high-probability motions, and low-probability motions may not be properly explored. Furthermore, it is not clear how to interpret the final state of an SE trajectory. In general, an SE trajectory will finish the simulation in a coherent superposition of electronic states, whereas physically one expects isolated products to be in pure electronic states (if there is no electronic state coupling in the product region of phase space). The internal energy distribution of products in a superposition of electronic states is not reliable because it does not correspond directly to the internal energy distribution of any single physically meaningful product.

The SCDM¹¹⁴ and CSDM¹¹³ methods, introduced above, are modified SE methods that force the system into a pure electronic state as the system passes through and leaves the strong coupling region. Both methods add decay terms to off-diagonal matrix elements of the electronic density