

# **Mechanical evaluation strategies for plastics**

**D R Moore and S Turner**

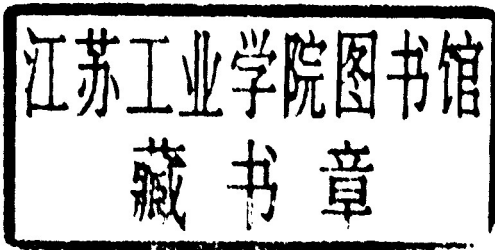


**WOODHEAD PUBLISHING LIMITED**

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CRC Press

Boca Raton Boston New York Washington, DC

WOODHEAD PUBLISHING LIMITED

Cambridge England

Published by Woodhead Publishing Limited, Abington Hall,  
Abington  
Cambridge CB1 6AH, England  
[www.woodhead-publishing.com](http://www.woodhead-publishing.com)

Published in North and South America by CRC Press LLC,  
2000 Corporate Blvd, NW  
Boca Raton FL 33431, USA

First published 2001, Woodhead Publishing Ltd and CRC Press LLC  
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British Library Cataloguing in Publication Data  
A catalogue record for this book is available from the British Library.

Library of Congress Cataloging in Publication Data  
A catalog record for this book is available from the Library of Congress.

Woodhead Publishing ISBN 1 85573 379 X  
CRC Press ISBN 0-8493-0842-9  
CRC Press order number: WP0842

Cover design by The ColourStudio  
Typeset by Best-set Typesetter Ltd., Hong Kong  
Printed by TJ International Ltd, Cornwall, England

## Mechanical evaluation strategies for plastics

This book examines strategies for experimental approaches to stiffness, strength and toughness testing. There are numerous options in these activities and one of the aims of the book is to critically consider beneficial approaches in the context of multiple objectives. How test results are interpreted may be more important than the physical validity of the test procedure in some instances. A good test strategy can compensate for imperfections or insufficiencies in a particular procedure and integrate the results from individual test components into an entity that is more informative than the simple sum of the individual parts. Thus, whilst various classes of test have to be segregated for the convenience of a reader, they cannot be so segregated in testing practice because one class of test may support another via correlations that might surprise or offend the purist, but that are invaluable at the sharp end of commercial competitiveness.

The book divides mechanical evaluation into two areas: modulus measurement and strength/ductility measurement. Each area is then considered in terms of the type of input function, namely constant deformation rate, sinusoidal excitation, step-function tests and impulse excitation. Consequently, all of the usual procedures in mechanical property evaluations are accommodated; universal test machine tests, creep modulus, dynamical mechanical modulus, stiffness anisotropy, general fracture toughness, long-term strength, strength in aggressive environments, fatigue and impact toughness.

The presentational style of the book is novel. The 11 chapters dealing with modulus and strength/ductility are quite short. They provide a condensed opinion of what is beneficial and what is mythical, but largely without formal review since much of that is covered in other texts. Consequently, there is no attempt at citing detailed references nor is there a formal account of the many test methods. However, there is a copious section on other recommended reading.

Each chapter contains small but numbered sections. Throughout these sections there are opportunities to provide illustration of a point. These

illustrations appear as referenced supplements at the end of each chapter, e.g. Supplement 1.4 discusses samples, specimens and tests. By placing them as appendices, each chapter can be read without deviation in order to obtain an overall view on what is a vast topic. On the other hand, the supplements (which exceed 50 in number) can be a source of specific study in using the book, each one standing essentially self-contained.

The book is aimed at a broad audience of material scientists and engineers. For those in industry, whether involved as material suppliers, processors or end-users, there is an account of the approaches that they can use in characterizing mechanical properties as well as utilizing mechanical properties in end-product application or in contemplating the influence of processing on properties. Students in engineering, materials science or polymer science departments will benefit from the short, yet broad-ranging, chapter content, but also be guided by the many illustrations of application of a principle or an approach.

Both authors have worked in the Mechanical Property Group in ICI's Research Department. They overlapped for 10 years but covered a total span of 50 years from which much of their knowledge and experience has developed. During this long period they had the benefit of working with a large number of colleagues. This was a rich experience, and both authors acknowledge the pleasure, benefits and learning that emerged from the constructive interactions.

## Abbreviations

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ABS	acrylonitrile butadiene styrene
APC	aromatic polymer composite
ASTM	American Society for Testing and Materials
BPDA	3, 4, 3', 4' biphenyl tetracarboxylic dianhydride
BSI	British Standards Institute
BTL	Bell Telephone Laboratory
CLS	cracked lap shear
COD	crack opening displacement
CT	compact tension
c.v.	coefficient of variation
DCB	double cantilever beam
DDE	diamino diphenyl ether
DIN	Deutsches Institut für Normung
DMA	dynamical mechanical analyser
ENF	end-notched flexure
ESC	environmental stress cracking
ESIS	European Structural Integrity Society
HD	high density as in high density polyethylene
HDT	heat distortion temperature
HDPE	high density polyethylene
ISO	International Organization for Standardization
LEFM	linear elastic fracture mechanics
MEK	methyl ethyl ketone
MFI	melt flow index
NDT	non-destructive testing
NPL	National Physical Laboratory
PEEK	poly(ether ether ketone)
PES	poly(ethersulphone)
PMDA	pyromellitic dianhydride
PMMA	poly(methyl methacrylate)
PP	polypropylene

PTFE	poly(tetrafluoroethylene)
PTMT	poly(tetramethylene terephthalate)
PVC	poly(vinyl chloride)
R-curve	plot of fracture toughness vs. crack length
SEN	single edge notched
$\tan \delta$	tangent of the loss angle $\delta$
TC4	Technical Committee 4
3D	three dimensional
w/w	weight/weight concentration



## Symbols

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$a$	crack length
$a$	half-length of intrinsic defect
$a$	radius of a support ring (re impact equipment)
$a$	lateral dimension
$a_1, a_2$	side dimension of a rectangular plate
$a_{0...n}$	coefficients
$a_f$	effective crack length
$A$	shape factor
$A$	cross-sectional area
$A$	constant
$A$	coefficient
$A_i$	a series of coefficients $A_1, A_2, \dots$
$\alpha$	highest temperature transition (with respect to loss processes)
$b$	specimen width
$b_{0...m}$	coefficients
$b_{\min}$	minimum value of specimen width for plane strain conditions
$B$	coefficient
$B(\sigma, t)$	bulk compliance which is stress and time dependent
$\beta$	next to highest temperature transition (re loss processes)
$\beta(b, h)$	shape factor for torsion of a beam
$c$	$\cos \theta$
$c^*$	complex compliance for a Voigt element
$c', c''$	real and imaginary components of compliance associated with a Voigt element
$C$	stiffness $[E/(1-\nu^2)]$
$\bar{C}$	transform compliance
$\bar{C}_c(p)$	Laplace creep function
$C^*(\omega)$	complex compliance (dependent on angular frequency)

$C(t)$	time dependent compliance also creep compliance function
$C_c(t)$	creep function
$C^*$	complex compliance
$C', C''$	real and imaginary components of complex compliance
$C(\sigma, t)$	uniaxial compliance dependent on stress and time
$C_{ijkl}$	stiffness coefficients where $i, j, k, l$ can have values of 1, 2 or 3
$C_{ij}$	stiffness coefficients for an applied stress with the direction of the normal to the surface being $i$ and a strain axis $j$ (where $i, j$ can be 1, 2 or 3)
$cv$	coefficient of variation
$d$	tank wall thickness
$d$	diameter of a cylinder
$d$	displacement
$da/dn$	crack growth per cycle
$D$	flexural rigidity ( $EI$ )
$D$	ductility factor
$\delta$	deflection of a beam
$\delta$	phase angle associated with complex modulus
$\delta$	crack opening displacement
$\delta_l$	increase in length
$\delta(t)$	time dependent deflection
$\delta_b$	deflection due to bending
$\delta_s$	deflection due to shear
$\delta_{crit}$	critical value of crack opening displacement
$\Delta$	crack length correction
$\Delta V$	change in volume
$\Delta H$	activation energy
$\Delta T$	temperature increment
$\Delta P$	force difference (re fatigue testing)
$\Delta K$	difference in stress field intensity factor (re fatigue testing)
$\Delta\sigma_R$	change in remote stress (re fatigue testing)
$e$	exponential function
$E$	axial modulus also known as Young's modulus and as modulus of elasticity
$(EI)$	flexural rigidity
$E(t)$	time dependent modulus
$E_c(t)$	tensile creep modulus
$E_t$	modulus at time $t$
$E_c$	composite modulus
$E_f$	fibre modulus
$E_m$	matrix modulus

$E_{ij}$	engineering axial modulus where $i, j$ can be 1, 2 or 3
$E_r$	relaxation modulus in tension
$E_\theta$	in plane modulus where typically $\theta = 0^\circ, 45^\circ, 90^\circ$
$E(100)$	100sec axial modulus
$E^*$	complex modulus
$\epsilon_{ij}$	strain in the plane $i, j$ where $i, j$ relate to the rectangular co-ordinates $x, y, z$
$\epsilon$	strain (engineering)
$\epsilon_H$	Henky or logarithmic strain
$\epsilon_{equiv}$	equivalent strain
$\epsilon_{l,w,h}$	axial, width and thickness strains
$\epsilon_{kl}$	strain tensor where $k, l$ can be 1, 2 or 3
$\epsilon_{ij}$	strain tensor where $i, j$ can be 1, 2 or 3
$f$	frequency
$f(\theta)$	angular distribution of stress
$f(h)$	function of specimen thickness
$f(\nu)$	function of Poisson's ratio
$f(a)$	function of crack length
$f(\theta)$	function dependent on the angle $\theta$
$f_0$	constant
$f_1, f_2$	specific frequencies
$f(\sigma)$	function of stress
$F(\sigma, t)$	function of stress and time
$FR$	fractional recovery
$F$	large displacement correction
$\phi$	fibre volume fracture
$\phi$	geometry function
$\phi(\epsilon)$	function of strain
$\phi$	phase angle associated with complex modulus but used in fixed vibration systems ( $\phi \neq \delta$ )
$g$	acceleration due to gravity
$g(t)$	function of time
$G$	shear modulus
$G$	strain energy release rate
$G$	surface energy
$G^*$	complex shear modulus
$G(t)$	time-dependent shear modulus
$G', G''$	real and imaginary components of a complex shear modulus
$G_{ij}$	engineering shear modulus where $i, j$ can be 1, 2 or 3
$G(100)$	100s shear modulus
$G_c$	critical value for strain energy release rate but more usually known as fracture toughness
$G_{Ic}$	opening mode fracture toughness

$\gamma$	fracture surface energy
$\gamma$	third from highest temperature transition (re loss processes)
$\gamma_{ij}$	shear strain where $i, j$ can be 1, 2 or 3
$H$	height of liquid in a cylindrical tank
$h$	specimen depth, thickness
$h$	specimen diameter
$h_{1,2}$	outer and inner specimen diameters, respectively, of a tube
$\eta$	viscosity associated with a dashpot
$\eta_\alpha$	inefficiency factor for imperfectly aligned continuous fibres
$\eta_c$	inefficiency factor for imperfectly discontinuous fibres
$\eta_d$	inefficiency factor for debonded fibres
$I$	area moment of inertia
$J_{2D}$	second invariant of the deviatoric part of the stress tensor
$J_1$	first invariant of the stress tensor
$J_c$	crack resistance
$k$	stress concentration
$k$	spring constant
$k^*$	complex stiffness
$k', k''$	real and imaginary components of stiffness for a Voigt element
$K$	bulk modulus
$K_a$	apparent bulk modulus
$K^*$	complex bulk modulus
$K', K''$	real and imaginary components of a complex bulk modulus
$K^l$	Larsen–Miller creep rupture parameter for equating time and temperature
$K_{I,II,III}$	opening mode, shear mode and antishear mode (tearing mode) for stress field intensity factor, respectively
$K_c$	critical value of stress field intensity factor but better known as fracture toughness
$K_{Ic}$	opening mode fracture toughness
$K_{c1}$	plane strain fracture toughness
$K_{c2}$	plane stress fracture toughness
$l$	gauge length
$l$	length of a cylinder
$l$	decay length (in St Venat's principle)
$l$	specimen height
$l_o$	original gauge length

$L$	effective beam length or span
$L$	length of a diagonal
$\lambda$	a specific decay length (in St Venat's principle)
$\lambda$	extension ratio
$m$	Paris law integer
$m$	mass of impactor
$m$	an integer in the range $0 \dots m$
$\overline{M}_r(p)$	Laplace creep modulus function
$M_r(t)$	relaxation creep modulus function
$M^*$	complex modulus
$M', M''$	real and imaginary components of complex modulus
$M_o$	instantaneous modulus
$M_t$	applied torque
$\mu$	coefficient of friction
$n$	an integer in the range $0 \dots n$
$n$	$\sin \theta$
$n$	power law coefficient
$N$ or $n$	number of fatigue cycles
$N$	loading block correction
$\nu$	lateral contraction ratio also known as Poisson's ratio
$\nu(t)$	time-dependent lateral contraction ratio
$\nu', \nu''$	real and imaginary components of a complex lateral contraction ratio
$\nu^*$	complex lateral contraction ratio
$\nu(\sigma, t)$	stress and time-dependent lateral contraction ratio
$\nu_{ij}$	engineering lateral contraction ratio where $i, j$ can be 1, 2 or 3
$p$	a variable
$P$	applied force
$P$	peak force
$P_{\max}$	maximum force
$P_{\min}$	minimum force
$Q$	transverse shear stiffness
$\theta$	an angle
$\theta$	angle measured anticlockwise from the line of a crack
$r$	a radius
$r$	an integer from 0 to $r$

$r$	distance from crack tip
$r_p$	plastics zone radius also length of the line zone in a Dugdale model
$r_o'$	effective area of contact between impactor nose and specimen
$r_0$	actual area of contact between impactor nose and specimen
$R$	gas constant (8.314 J/mol K)
$R$	ratio of minimum to maximum force in fatigue
$\rho$	density
$\rho$	notch-tip radius
$s$	$\sin \theta$
$S$	span
$S$	stress
$S_{ijkl}$	are compliance coefficients where $i, j, k, l$ can be 1, 2 or 3
$S_{ij}$	are compliance coefficients for an applied strain with the direction of the normal to the surface being $i$ and the line of action of the stress being $j$ (where $i, j$ can be 1, 2 or 3)
$\sigma$	stress (including true stress)
$\sigma_o$	a step function of stress
$\sigma(t)$	time-dependent stress
$\sigma_a$	applied stress
$\sigma_{ij}$	stress tensor where $i, j$ can be 1, 2 or 3 (also for $\sigma_{kl}$ ) or $x, y$ or $z$
$\sigma_{11}, \sigma_{22}, \sigma_{33}$	normal stresses
$\sigma_{12}, \sigma_{23}, \sigma_{31}$	shear stresses
$\sigma_L(r, \theta)$	local stress at the tip of a crack
$\sigma_R$	applied stress at a point remote from the crack (notch)
$\sigma_y$	yield stress
$\sigma_i$	principal stress where $i$ can be 1, 2 or 3
$\sigma_n$ or $\sigma_{net}$	net stress
$\sigma_{max}$	maximum stress
$\sigma_f$	stress at fracture
$\sigma_m$	stress in the tensile skin layer at mid-span (re bending of a beam)
$\sigma_t, \sigma_c$	tensile and compressive stress, respectively
$\sigma_D$	design stress
$t$	time
$t_R$	reduced time (re creep recovery)
$t_{min}$	minimum creep rupture lifetime
$t_{max}$	maximum creep rupture lifetime
$t_{ON}$	time on load

$T$	temperature
$T_b$	embrittlement temperature
$T_1, T_2$	specific temperatures
$T_g$	glass–rubber transition temperature
$\tau$	a relaxation time; for a spring-dashpot array, it is the ratio of viscosity to spring constant i.e $\eta/\kappa$
$\tau_{ij}$	shear stress where $i, j$ can be 1, 2 or 3 or alternatively $x, y$ or $z$
$\tau_{\max}$	maximum shear stress
$u$	a variable
$U$	stored energy
$Ut$	energy stored by a specimen at any time $t$
$v$	velocity
$v_c$	velocity of crack propagation in glass
$v_t$	velocity of crack propagation in an infinite medium
$v_i$	velocity of an impactor (re instrumented impact equipment)
$v_0$	initial velocity of an impactor
$V$	volume
$\Delta V/V$	volume strain
$w$	width
$w_p$	energy per unit volume
$W$	specimen width
$\omega$	angular frequency
$x$	a variable
$x_t$	displacement of specimen at any time $t$
$Y$	geometry factor in fracture mechanics
$z$	distance from the neutral axis (for a beam specimen)

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