

HANDBOOK OF SMALL ELECTRIC MOTORS



WILLIAM H. YEADON, P.E. ALAN W. YEADON, P.E.

HANDBOOK OF SMALL ELECTRIC MOTORS

William H. Yeadon, P.E. Editor in Chief Alan W. Yeadon, P.E. Associate Editor

Yeadon Energy Systems, Inc Yeadon Engineering Services, P.C.

McGraw-Hill

New York Chicago San Francisco Lisbon London Madrid Mexico City Milan New Delhi San Juan Seoul Singapore Sydney Toronto

Library of Congress Cataloging-in-Publication Data

Handbook of small electric motors / William H. Yeadon, editor in chief, Alan W. Yeadon, associate editor.

p. cm.

ISBN 0-07-072332-X

1. Electric motors, Fractional horsepower. I. Yeadon, William H. II. Yeadon, Alan W.

TK2537 .H34 2001

621.46-dc21

00-048974

McGraw-Hill



A Division of The McGraw-Hill Companies

Copyright © 2001 by The McGraw-Hill Companies, Inc. All rights reserved. Printed in the United States of America. Except as permitted under the United States Copyright Act of 1976, no part of this publication may be reproduced or distributed in any form or by any means, or stored in a data base or retrieval system, without the prior written permission of the publisher.

1234567890 DOC/DOC 07654321

ISBN 0-07-072332-X

The sponsoring editor for this book was Scott Grillo and the production supervisor was Sherri Souffrance. It was set in Times Roman by North Market Street Graphics.

Printed and bound by R. R. Donnelley & Sons Company.

McGraw-Hill books are available at special quantity discounts to use as premiums and sales promotions, or for use in corporate training programs. For more information, please write to the Director of Special Sales, Professional Publishing, McGraw-Hill, Two Penn Plaza, New York, NY 10121-2298. Or contact your local bookstore.

This handbook is intended to be used as a reference for information regarding the design and manufacture of electric motors. It is not intended to encourage or discourage any motor type, design, or process. Some of the configurations or processes described herein may be patented. It is the responsibility of the user of this information to determine if any infringement may occur as a result thereof.

Information contained in this work has been obtained by The McGraw-Hill Companies, Inc. ("McGraw-Hill") from sources believed to be reliable. However, neither McGraw-Hill nor its authors guarantee the accuracy or completeness of any information published herein, and neither McGraw-Hill nor its authors shall be responsible for any errors, omissions, or damages arising out of use of this information. This work is published with the understanding that McGraw-Hill and its authors are supplying information but are not attempting to render engineering or other professional services. If such services are required, the assistance of an appropriate professional should be sought.

HANDBOOK OF SMALL ELECTRIC MOTORS

This handbook is dedicated to my wife, Luci Yeadon, who took most of the photographs for it.

William H. Yeadon Editor in Chief

CONTRIBUTORS

Larry C. Anderson American Hoffman Corporation (Sec. 3.14)

John S. Bank Phoenix Electric Manufacturing Company (Sec. 3.15)

Warren C. Brown Link Engineering Company (Sec. 3.10.6)

Joseph H. Bularzik Magnetics International, Inc. (Sec. 2.5)

Peter Caine Oven Systems, Inc. (Sec. 3.16)

David Carpenter Vector Fields, Ltd. (contributed the finite-element plots in Chap. 4)

John Cocco Loctite Corporation (Sec. 3.17)

Philip Dolan Oberg Industries (Sec. 3.10.5)

Birch L. DeVault Cutler-Hammer (Sec. 10.6)

Brad Frustaglio Yeadon Energy Systems, Inc. (Sec. 6.4)

Francis Hanejko Hoeganaes Corporation (Sec. 2.6)

Duane C. Hanselman University of Maine (Secs. 5.1.4 and 10.11)

Daniel P. Heckenkamp Cutler-Hammer (Sec. 10.6)

Leon Jackson LDJ Electronics (Sec. 3.19)

Dan Jones Incremotion Associates (Secs. 5.1.3, 10.12, and 10.13)

Douglas W. Jones University of Iowa (Secs. 5.2.10 and 10.8 to 10.10)

Mark A. Juds Eaton Corporation (Secs. 1.1 to 1.12)

Robert R. Judd Judd Consulting Associates (Secs. 2.2 and 2.3)

Ramani Kalpathi Dana Corporation (Sec. 10.7)

John Kauffman Phelps Dodge Magnet Wire Company (Sec. 2.10)

Todd L. King Eaton Corporation (Sec. 10.6)

H. R. Kokal Magnetics International, Inc. (Sec. 2.5)

Robert F. Krause Magnetics International, Inc. (Sec. 2.5)

Barry Landers Electro-Craft Motion Control (Chap. 9)

Roger O. LaValley Magnetic Instrumentation, Inc. (Sec. 3.18)

Bill Lawrence Oven Systems, Inc. (Sec. 3.16)

Andrew E. Miller Software and motor designer (Secs. 4.5, 6.4.3, and 6.4.4)

Stanley D. Payne Windamatics Systems, Inc. (Sec. 3.10.4)

Derrick Peterman LDJ Electronics (Sec. 3.19)

Curtis Rebizant *Integrated Engineering Software* (contributed the boundary element plots in Figs. 5.58 to 5.61)

Earl F. Richards University of Missouri (Secs. 1.14, 4.1, 6.2, 6.3, and 8.4 to 8.8)

Robert M. Setbacken Renco Encoders, Inc. (Secs. 10.1 to 10.5)

Karl H. Schultz Schultz Associates (Secs. 3.1 to 3.9)

Joseph J. Stupak Jr. Oersted Technology Corporation (Sec. 2.8)

Chris A. Swenski Yeadon Energy Systems, Inc. (Secs. 3.6.5, 6.4, and 7.4)

Harry J. Walters Oberg Industries (Sec. 3.10.5)

Alan W. Yeadon Engineering Services, PC (Secs. 3.10, 3.11, and 4.2 to 4.5)

Luci Yeadon Luci's Photography (contributed most of the photographs in this handbook)

William H. Yeadon *Yeadon Engineering Services, PC* (Secs. 1.13, 2.1, 2.9, 2.11, 3.10 to 3.12, 4.3, 4.6 to 4.8, 5.1 to 5.3, 6.1, 6.4, 7.1 to 7.4, and 8.1 to 8.3)

PREFACE

When I was first approached about writing this handbook, it seemed like a fairly straightforward task. There was information available from a variety of sources. There were many capable people in the field who could contribute, and there was historical data from many sources.

The intent of this book is to cover the operating theory, practical design approaches, and manufacturing methods for the most common motors now in use. We have tried to meet this intent by including as much information as possible. The universe of motor information is huge, although most of the information is old. It became apparent that much information would have to be left out. We tried to include the basics along with that information we felt was most necessary and useful to those designing, manufacturing, and using motors. This is not a design course or a highly theoretical text but a place where people can go to get practical answers.

We are setting up a section at our Web site, www.yeadoninc.com, for people to comment about the book and tell us of improvements we can make and things they

would like to have added to the next edition.

ACKNOWLEDGMENTS

Over the course of my career I have had the privilege to meet many of the giants of this industry. Many I have met through my association with the Small Motors and Motion Association (SMMA) and others through business relationships. Included among them are Dr. Cyril G. Veinott, Professor Philip H. Trickey, Dr. Ben Kuo, Dr. Duane Hanselman, and those authors who have contributed to this handbook.

There is, however, one person of whom I must make special mention. He is Dr. Earl Richards, Professor Emeritus of the University of Missouri at Rolla. This man never ceases to amaze me. He is always willing to help out selflessly with projects of this type. I have taught many motor design courses with him. When a student asks questions of him, he can start at the lowest level of understanding necessary and develop in a very understandable way a logical and reasonable answer to the question. His ability to communicate and teach is truly amazing. He has been very helpful in the preparation of this book.

I also need to acknowledge the dedication of my secretary, Kristina Wodzinski.

Without her tireless effort this work would not have been completed.

CONTENTS

Pr	ontributors xi eface xiii eknowledgments xv oter 1. Basic Magnetics	1.1
	Units / 1.1	
	Definition of Terms / 1.6	
1.3.	Estimating the Permeance of Probable Flux Paths / 1.21	
1.4.	Electromechanical Forces and Torques / 1.32 Magnetic Materials / 1.43	
	Losses / 1.52	
1.7.	Magnetic Moment (or Magnetic Dipole Moment) / 1.58	
1.8.	Magnetic Field for a Current Loop / 1.65	
	Helmholtz Coil / 1.67	
	Coil Design / 1.67 Reluctance Actuator Static and Dynamic (Motion) Analysis / 1.78	
1.12.	Moving-Coil Actuator Static and Dynamic (Motion) Analysis / 1.83	
1.13.	Electromagnetic Forces / 1.89	
1.14.	Energy Approach (Energy-Coenergy) / 1.91	
Chap	ter 2. Materials	2.1
21	Magnetic Materials / 2.1	OBJET,
2.2.	Lamination Steel Specifications / 2.4	
2.3.	Lamination Annealing / 2.6	
2.4.	Core Loss / 2.46	
2.5.	Pressed Soft Magnetic Material for Motor Applications / 2.51	
	Powder Metallurgy / 2.59	
	Magnetic Test Methods / 2.71 Characteristics of Permanent Magnets / 2.80	
	Characteristics of Permanent Magnets / 2.80 Insulation / 2.163	
	Magnet Wire / 2.176	
	Lead Wire and Terminations / 2.189	

3.5. Shaft Hardening / 3.14

Chapter 3. Mechanics and Manufacturing Methods

3.2. End Frame Manufacturing / 3.43.3. Housing Materials and Manufacturing Processes / 3.10

3.1. Motor Manufacturing Process Flow / 3.1

3.4. Shaft Materials and Machining / 3.12

3.6. Rotor Assembly / 3.15

3.1

viii CONTENTS

3.7.	Wound Stator Assembly Processing / 3.21		
3.8.	Armature Manufacturing and Assembly / 3.22		
3.9.	Assembly, Testing, Painting, and Packing / 3.23		
3.10.	Magnetic Cores / 3.25		
3.11.	Bearing Systems for Small Electric Motors / 3.46		
3.12.	Sleeve Bearings / 3.72		
3.13.	Process Control in Commutator Fusing / 3.79		
3.14.	Armature and Rotor Balancing / 3.87		
3.15.	Brush Holders for Small Motors / 3.99		
3.16.	Varnish Impregnation / 3.103		
	Adhesives / 3.109		
3.10.	Magnetizers, Magnetizing Fixtures, and Test Equipment / 3.124		
3.17.	Capacitive-Discharge Magnetizing / 3.138		
Chap	oter 4. Direct-Current Motors	4.1	
4.1.	Theory of DC Motors / 4.1	1885	
4.2.	Lamination, Field, and Housing Geometry / 4.46		
4.3.	Commutation / 4.84		
4.4.	PMDC Motor Performance / 4.96		
4.5.	Series DC and Universal AC Performance / 4.116		
4.0.	Shunt-Connected DC Motor Performance / 4.130		
4.7.	Compound-Wound DC Motor Calculations / 4.134		
4.0.	DC Motor Windings / 4.138 Automatic Armature Winding Pioneering Theory and Practice / 4.140		
1.5.	Automatic Affiature winding Floneering Theory and Practice / 4.140		
Char	oter 5. Electronically Commutated Motors		
Cital	oter 5. Electronically Commutated Motors	5.1	
5.1.	Brushless Direct-Current (BLDC) Motors / 5.1	Hall I	
5.2.	Step Motors / 5.47		
5.3.	Switched-Reluctance Motors / 5.99		
	3.77		
Chap	oter 6. Alternating-Current Induction Motors	6.1	
	Introduction / 6.1		
6.2.	Theory of Single-Phase Induction Motor Operation / 6.5		
6.3.	Three-Phase Induction Motor Dynamic Equations and Steady-State Equivalent		
	Circuit / 6.38		
6.4.	Single-Phase and Polyphase Induction Motor Performance Calculations / 6.45		
Chan	eter 7. Synchronous Machines		
Citap	tel 7. Synchronous Machines	7.1	
7.1.	Induction Synchronous Motors / 7.1		
7.2.	Hysteresis Synchronous Motors / 7.5		
7.3.	Permanent-Magnet Synchronous Motors / 7.9		
7.4.	Performance Calculation and Analysis / 7.16		
	7 / 120		
Chap	Chapter 8. Application of Motors		
8.1	Motor Application Requirements / 8.1	MED	
	Velocity Profiles / 8.4		
0121	1 1001100 / 0.7		

8.4. 8.5. 8.6. 8.7.	Current Density / 8.9 Thermal Analysis for a PMDC Motor / 8.10 Summary of Motor Characteristics and Typical Applications / 8.32 Electromagnetic Interference (EMI) / 8.32 Electromagnetic Fields and Radiation / 8.35 Controlling EMI / 8.38		
Chap	oter 9. Testing	9.1	
9.2. 9.3. 9.4. 9.5. 9.6. 9.7.	Speed-Torque Curves / 9.1 AC Motor Thermal Tests / 9.5 DC Motor Testing / 9.9 Motor Spectral Analysis / 9.15 Resonance Control in Small Motors / 9.27 Fatigue and Lubrication Tests / 9.36 Qualification Tests for Adhesives and Plastic Assemblies / 9.42 Trends in Test Automation / 9.43		
Chapter 10. Drives and Controls			
10.2. 10.3. 10.4. 10.5. 10.6. 10.7. 10.8. 10.9. 10.10. 10.11.	Measurement Systems Terminology / 10.1 Environmental Standards / 10.4 Feedback Elements / 10.9 Comparisons Between the Various Technologies / 10.42 Future Trends in Sensor Technology / 10.48 Selection of Short-Circuit Protection and Control for Design E Motors / 10.51 Switched-Reluctance Motor Controls / 10.65 Basic Stepping-Motor Control Circuits / 10.70 Current Limiting for Stepping Motors / 10.80 Microstepping / 10.93 Brushless DC Motor Drive Schemes / 10.97 Motor Drive Electronic Commutation Patterns / 10.119 Performance Characteristics of BLDC Motors / 10.122		
References			
Bibliography		B.1	
Index I.1 About the Contributors C.1			

About the Editors

CHAPTER 1

BASIC MAGNETICS

Chapter Contributors

Mark A. Juds Earl F. Richards William H. Yeadon

Electric motors convert electrical energy into mechanical energy by utilizing the properties of electromagnetic energy conversion. The different types of motors operate in different ways and have different methods of calculating the performance, but all utilize some arrangement of magnetic fields. Understanding the concepts of electromagnetics and the systems of units that are employed is essential to understanding electric motor operation. The first part of this chapter covers the concepts and units and shows how forces are developed. Nonlinearity of magnetic materials and uses of magnetic materials are explained. Energy and coenergy concepts are used to explain forces, motion, and activation. Finally, this chapter explains how motor torque is developed using these concepts.

1.1 **UNITS***

Although the rationalized mks system of units [Système International (SI) units] is used in this discussion, there are also at least four other systems of units—cgs, esu, emu, and gaussian] that are used when describing electromagnetic phenomena. These systems are briefly described as follows.

MKS. Meter, kilogram, second.

CGS. Centimeter, gram, second.

^{*} Sections 1.1 to 1.12 contributed by Mark A. Juds, Eaton Corporation.

ESU. CGS with $e_0 = 1$, based on Coulomb's law for electric poles.

EMU. CGS with $\mu_0 = 1$, based on Coulomb's law for magnetic poles.

Gaussian. CGS with electric quantities in esu and magnetic quantities in emu. The factor 4π appears in Maxwell's equation.

Rationalized mks. $\mu_0 = 4\pi \times 10^{-7}$ H/m, based on the force between two wires. Rationalized cgs. $\mu_0 = 1$, based on Coulomb's law for magnetic poles. The factor 4π appears in Coulomb's law.

The rationalized mks and the rationalized cgs systems of units are the most widely used. These systems are defined in more detail in the following subsections.

1.1.1 The MKS System of Units

The rationalized mks system of units (also called SI units) uses the magnetic units tesla (T) and amps per meter (A/m), for flux density B and magnetizing force H, respectively. In this system, the flux density B is defined first (before H is defined), and is based on the force between two current-carrying wires. A distinction is made between B and H in empty (free) space, and the treatment of magnetization is based on amperian currents (equivalent surface currents).

Total or normal flux density B, T

$$B = \mu_0 \left(H + M \right) \tag{1.1}$$

Intrinsic flux density B_i , T

$$B_i = \mu_0 M \tag{1.2}$$

Permeability of free space μ_0 , $(T \cdot m)/A$

$$\mu_0 = 4\pi \times 10^{-7} \tag{1.3}$$

Magnetization M, A/m

$$M = \frac{B_l}{\mu_0} = \frac{m}{V} \tag{1.4}$$

Magnetic moment M, J/T

$$m = MV = pl (1.5)$$

Magnetic pole strength p, A·m

$$p = \frac{m}{l} \tag{1.6}$$

1.1.2 The CGS System of Units

The rationalized cgs system of units uses the magnetic units of gauss (G) and oersted (Oe) for flux density B and magnetizing force H, respectively. In this system, the magnetizing force, or field intensity, H is defined first (before B is defined), and is

based on the force between two magnetic poles. No distinction is made between B and H in empty (free) space, and the treatment of magnetization is based on magnetic poles. The unit emu is equivalent to an erg per oersted and is understood to mean the electromagnetic unit of magnetic moment.

Total or normal flux density B, G

$$B = H + 4\pi M \tag{1.7}$$

Intrinsic flux density B_i , G

$$B_i = 4\pi M \tag{1.8}$$

Permeability of free space μ_0 , G/Oe

$$\mu_0 = 1$$
 (1.9)

Magnetization M, emu/cm3

$$M = \frac{B_i}{4\pi} = \frac{m}{\nu} \tag{1.10}$$

Magnetic moment m, emu

$$m = MV = pl \tag{1.11}$$

Magnetic pole strength p, emu/cm

$$p = \frac{m}{l} \tag{1.12}$$

The magnetization or magnetic polarization M is sometimes represented by the symbols I or J, and the intrinsic flux density B_i is then represented as $4\pi M$, $4\pi I$, or $4\pi J$.

1.1.3 Unit Conversions

Magnetic Flux φ

 $1.0 \text{ Wb} = 10^8 \text{ line}$

 $=10^8$ maxwell

 $= 1.0 \text{ V} \cdot \text{s}$

 $= 1.0 \text{ H} \cdot \text{A}$

 $= 1.0 \text{ T} \cdot \text{m}^2$

Magnetic Flux Density B

 $1.0 T = 1.0 Wb/m^2$

 $= 10^8 \, \text{line/m}^2$

 $=10^8$ maxwell/m²

 $= 10^4 \, \text{G}$

 $=10^{9} \, \text{y}$

1.0 G = 1.0 line/cm²
=
$$10^{-4}$$
 T
= 10^{5} γ
= 6.4516 line/in²

Magnetomotive or Magnetizing Force NI

$$1.0 \text{ A} \cdot \text{turn} = 0.4 \pi \text{ Gb}$$

= $0.4 \pi \text{ Oe} \cdot \text{cm}$

Magnetic Field Intensity H

1.0 (A·turn)/m =
$$4\pi \times 10^{-3}$$
 Oe
= $4\pi \times 10^{-3}$ Gb/cm
= 0.0254 (A·turn)/in
1.0 Oe = 79.5775 (A·turn)/m
= 1.0 Gb/cm
= 2.02127 (A·turn)/in

Permeability µ

1.0 (T·m)/(A·turn) =
$$10^{7}/4\pi$$
 G/Oe
= 1.0 Wb/(A·turn·m)
= 1.0 H/m
= 1.0 N/(amp·turn)²
1.0 G/Oe = $4\pi \times 10^{-7}$ H/m

Inductance L

1.0 H = 1.0 (V·s·turn)/A
= 1.0 (Wb·turn)/A
=
$$10^8$$
 (line·turn)/A

Energy W

1.0 J = 1.0 W·s
= 1.0 V·A·s
= 1.0 Wb·A·turn
= 1.0 N·m
=
$$10^8$$
 line·A·turn
= 10^7 erg

Energy Density w

$$1.0 \text{ MG} \cdot \text{Oe} = 7.958 \text{ kJ/m}^3$$

= 7958 (T·A·turn)/m
 $1.0 \text{ (T·A·turn)/m}^3 = 1.0 \text{ J/m}^3$

Force F

1.0 N = 1.0 J/m= 0.2248 lb 1.0 lb = 4.448 N

Magnetic Moment m

1.0 emu = 1.0 erg/Oe = 1.0 erg/G = 10.0 A·cm² = 10^{-3} A·m² = 10^{-3} J/T = 4π G·cm³ = $4\pi \times 10^{-10}$ Wb·m = 10^{-7} (N·m)/Oe

Magnetic Moment of the Electron Spin $\beta = eh/4\pi m_e$

$$\begin{split} 1.0 \; Bohr \; magneton &= \beta = 9.274 \times 10^{-24} \; J/T \\ &= \beta = 9.274 \times 10^{-24} \; A \cdot m^2 \\ &= \beta = 9.274 \times 10^{-21} \; erg/G \end{split}$$

Constants

Permeability of free space $\mu_0 = 1.0 \text{ G/Oe}$ $\mu_0 = 4\pi \times 10^{-7} \text{ (T·m)/(A·turn)}$ $\mu_0 = 4\pi \times 10^{-7} \text{ H/m}$ Electron charge $e = 1.602177 \times 10^{-19} \text{ C}$ Electron mass $m_e = 9.109390 \times 10^{-31} \text{ kg}$ Plank's constant $h = 6.6262 \times 10^{-34} \text{ J·s}$ Velocity of light $c = 2.997925 \times 10^8 \text{ m/s}$ Pi c = 3.1415926536Acceleration of gravity $c = 9.807 \text{ m/s}^2$

 $= 32.174 \text{ ft/s}^2$ = 386.1 in/s²

number to no

Miscellaneous

Length l 1.0 m = 39.37 in = 1.094 yd 1.0 in = 25.4 mm Time t 1.0 day = 24 h 1.0 min = 60 s

Velocity v 1.0 m/s = 3.6 km/h