Andrea Corradini Hartmut Ehrig Ugo Montanari Leila Ribeiro Grzegorz Rozenberg (Eds.)

# **Graph Transformations**

Third International Conference, ICGT 2006 Natal Rio Grande do Norte, Brazil, September 2006 Proceedings





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## **Preface**

ICGT 2006 was the 3rd International Conference on Graph Transformation, following the previous two in Barcelona (2002) and Rome (2004), and a series of six international workshops between 1978 and 1998. ICGT 2006 was held in Natal (Rio Grande do Norte, Brazil) on September 17-23, 2006, co-located with the Brazilian Symposium on Formal Methods (SBMF 2006), under the auspices of the Brazilian Computer Society (SBC), the European Association of Software Science and Technology (EASST), the European Association for Theoretical Computer Science (EATCS) and the IFIP WG 1.3 on Foundations of Systems Specification. The conference obtained partial support from Formal Methods Europe and IFIP TC 1 on Foundations of Computer Science.

The scope of the conference concerned graphical structures of various kinds (like graphs, diagrams and visual sentences) that are useful when describing complex structures and systems in a direct and intuitive way. These structures are often enriched with formalisms that model their evolution via suitable kinds of transformations. The field of the conference was concerned with the theory, applications, and implementation issues of such formalisms. Particular emphasis was put on metamodels which can accommodate a variety of graphical structures within the same abstract theory.

The theory is strongly related to areas such as graph theory and graph algorithms, formal language and parsing theory, the theory of concurrent and distributed systems, formal specification and verification, logics, and semantics. The application areas include all those fields of computer science, information processing, engineering, biology and the natural sciences where static and dynamic modelling using graphical structures and graph transformations, respectively, play important roles. In many of these areas tools based on graph transformation technology have been implemented and used.

The proceedings of ICGT 2006 consist of two parts. The first part contains the contributions of the invited speakers followed by 28 accepted papers that were selected out of 62 carefully reviewed submissions. The topics of the papers range over a wide spectrum, including graph theory and graph algorithms, theoretic and semantic aspects, modelling, contributions to software engineering and global computing, applications to biology, and tool issues. The second part contains a short description of a tutorial on foundations and applications of graph transformations, and short presentations of the satellite events of ICGT 2006.

We would like to thank the members of the program committee and the secondary reviewers for their enormous help in the selection process. Moreover, we would like to express our gratitude to the local organizers who did a great job, in particular to the Organizing Committee chair Anamaria Martins Moreira.

July 2006 — Andrea Corradini, Hartmut Ehrig, Ugo Montanari (PC co-chair) Leila Ribeiro (PC co-chair), Grzegorz Rozenberg

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# **Nested Quantification in Graph Transformation Rules**

#### Arend Rensink

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**Abstract.** In this paper we describe a way to integrate Taentzer's rule amalgamation with the recently proposed notions of nested graph conditions. The resulting so-called *quantified graph transformation rules* include (universally and existentially) quantified sub-structures in a flexible way. This can be used for instance to specify a larger-step operational semantics, thus improving the scalability of graph transformation as a technique for software verification.

#### 1 Introduction

The idea presented in this paper is motivated by the goal to use graph transformation as a technique for specifying, and eventually verifying, the dynamic behaviour of software systems. In this setup, each transformation rule corresponds to a single computation step of the system, in which, for instance, a method is called or a variable is assigned. We have observed in previous work, e.g., [13], that such a computation step frequently involves acting upon a structure whose size is not *a priori* known, but instead involves sub-structures of which there may be arbitrarily many copies.

A typical example of this is the encoding of parameter transfer from a method caller to the called method. Obviously this is the same mechanism for all methods, and so we would like to have a single rule that captures it. Unfortunately, the number of parameters is not the same for all methods: in fact, the parameters indeed form a sub-structure with a varying and a priori unknown number of copies. For this reason, it is not possible, using the standard graph transformation formalism, to capture the parameter transfer mechanism in a single rule. Fig. 1 shows an example rule for two parameters.

Although there are workarounds, typically involving the use of auxiliary edges which successively mark all copies of the substructure involved, these have undesirable consequences (besides being inelegant). In particular, such a solution results in a number of small steps that is linear in the number of substructures involved. In particular in a setting where the system under analysis has parallelism, these steps get interleaved with independent actions in other parts of the system, contributing to the state space blowup (which is the most urgent problem in verification methods in the first place). This,

<sup>\*</sup> The work reported in this paper was carried out in the context of the Dutch NWO project GROOVE (project number 612.000.314).

<sup>&</sup>lt;sup>1</sup> To be more precise, the number of parameters is fixed and known for each individual method, but not from the more global perspective of our semantics, in which calls to all methods are to be treated as instances of the same mechanism.

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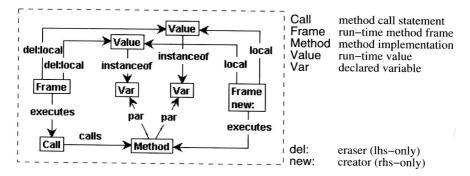


Fig. 1. Method call rule for two parameters

in turn, may be alleviated by further modifying the formalism, for instance by imposing priorities or other forms of control on the set of rules, but at the price of increased complexity of the formalism and hence of the verification task itself.

To make the example even more challenging: if we are interested in a data-flow analysis, we want the method call rule to be enabled if and only if all the arguments to the method are available (and not when control has explicitly reached the point in the program where the method is called). This involves a further condition on the rule, involving the existence of all relevant substructures — in this case, values for all method parameters. This is *not* a standard (positive or negative) application condition, since, once more, the number of substructures that are required to exist is not a priori known.

The problem described above has been studied before. On the practical side, many tools for graph transformation (for instance GREAT [6], FuJaBa [4]) have some notion of graph patterns that may be matched with cardinality greater than 1, i.e., that match to an a priori unknown number of sub-graphs in the host graph. Furthermore, Taentzer [18] has developed an elegant theoretical basis for this type of extension, called *rule amalgamation*. This is based on the concept of an *interaction scheme* which essentially imposes a sub-rule embedding on a set of rules, and a *covering condition* which imposes further conditions on the matches to be considered. Taking the above example, there would be a single so-called *elementary rule* that takes care of the hand-over of a single parameter, and a sub-rule that selects the caller Frame node and creates the called Frame node; the covering condition would be *local-all*, which gathers as many copies of the elementary rule as there are suitable combinations of Var- and Value-nodes attached to the selected Frame-node.

Elegant and natural though this solution is, it does not yet meet all demands. For instance, the data flow analysis rule proposed above cannot be captured by a simple subrule embedding, even in the presence of (standard) negative application conditions: the result would be that the rule as a whole is always enabled, with copies of the elementary rule precisely for those parameters for which an argument value is already available. More generally, the problem is to enforce, in a covering condition, that elementary rules are actually enabled for all sub-structures (in the host graph) of a particular kind, i.e., satisfying a certain application condition. In other words, there are further gains to be made in the appropriate combination of covering conditions and application conditions.

Recently there have been proposals, by ourselves in [16] and independently by Habel and Pennemann in [9], to extend the power of application conditions, by generalising the two-level structures originally introduced in [8] to trees of arbitrary nesting depth. As shown in [16], every further level of nesting effectively corresponds to an additional level of quantification in terms of logic.

The core contribution of this paper is to recognise that the two principles of subrule embedding on the one hand and condition nesting on the other can be fruitfully combined, giving rise to a notion of *quantified graph transformation rule* that is both natural and powerful, and complements the framework for rule amalgamation so as to solve the problem outlined above.

Summarising, in this paper we combine two pre-existing ideas:

**Rule amalgamation**, developed by Taentzer [18] and later applied for, e.g., refactoring [1], parallel graph transformation [3] and multi-formalism simulation [2].

**Nested graph predicates,** recently proposed by Rensink [16] and independently by Habel and Pennemann [9].

In terms of these techniques, a brief explanation of our proposal is that we merge the nesting structure of the nested graph predicates with the sub-rule embeddings of interaction schemes, as used in rule amalgamation, so that the left hand sides of the rules are part of a nested graph predicate that simultaneously acts as an application condition. Another way to put it (slightly more loosely) is to say that we present a way to use nested graph predicates as a language for covering conditions, in the sense of Taentzer [18].

The paper is structured as follows: Sect. 2 provides the necessary technical concepts, Sect. 3 illustrates their use on the basis of a number of examples, and Sect. 4 concludes the paper.

#### 2 Definitions

We first recall the notion of graph predicates from [16] and in passing establish the connection to [9]. We assume some category of graphs Graph with an initial element  $\emptyset$ , objects G, H and morphisms f, g etc. For concrete examples, we will take the common edge-labelled graphs  $\langle N, E, L, s, t, \ell \rangle$ , with N as set of nodes, E a set of edges, E a set of labels, and E and E and E and E and E and E be the source and target mapping and labelling function, respectively; morphisms will be the homomorphisms over this structure.

We characterise graph predicates as rooted diagrams in the category Graph. Given such a diagram d and an object G in d,  $root_d$  will denote the object at the root of d, and  $out_d(G)$  will denote the morphisms in d that originate in G. (Note that a rooted diagram has a well-defined root even if it has no arrows.) Furthermore,  $sub_d(G)$  will denote the reachable sub-diagram rooted in G, and for arbitrary  $f\colon G\to root_d, c=d\circ f$  is the diagram with  $root_c=G$ ,  $init_c=\{g\circ f\mid g\in init_d\}$  and  $sub_c(H)=sub_d(H)$  for all graphs H in d except for  $root_d$ . (In other words,  $d\circ f$  is obtained from d by using f's source as the new root, concatenating f with the initial arrows of d and leaving the remainder of d unchanged.

**Definition 1** (graph predicate). Let  $G \in G$  Graph be arbitrary. A graph predicate over G is a tree-shaped diagram p in Graph rooted in G. p is called ground if  $G = \emptyset$ .

Predicate satisfaction is a binary relation  $\models$  between predicates and graph morphisms:  $p \models f$  expresses that f satisfies  $p \models$  is defined as the smallest relation such that  $p \models f$  whenever the following conditions hold:

- $root_p = H$ ;
- There are  $g: G \to K \in init_p$  and  $h: K \to H$  such that  $f = h \circ g$  and  $sub_p(K) \not\models h$ .

Moreover, if we say that a graph G satisfies p, denoted  $p \models G$ , if  $p \models f : \emptyset \rightarrow G$ . (Note that this implies that p is ground.)

It might take some getting used to that the subjects are morphisms f rather than graphs. The intuition is that the source of f, which corresponds to the root of the predicate diagram, only identifies the common context or pattern; typically a subgraph which is already known to be present. The predicate itself actually states something about the *target* graph of the morphism. This intuition is confirmed by the special case where the source of f is the empty graph: in that case f really contains only the information in its target.

Satisfaction as defined in Def. 1 is slightly tricky in that it seems to rely on a smallest fixpoint construction for a function that is not monotonic, but rather anti-monotonic, due to the negation in the second bullet above. However, this is only superficially true, since in the sub-clause the satisfaction predicate is applied to a strictly smaller diagram; hence we can conduct proofs on the depth of the predicate diagram. (Actually, the above definition and most of the developments of this paper would still work for dags, and even for diagrams with cycles, as long as for any arrow in the diagram, the length of every path from the root to that arrow has the same parity, i.e., either all paths have odd length or all paths have even length. This implies that, in particular, all cycles must have even length. However, we restrict to tree-shaped diagrams in this paper.)

Alternatively, and perhaps more understandably, predicate satisfaction can be formulated in terms of two distinct satisfaction relations,  $\models_{\exists}$  and  $\models_{\forall}$ , as follows:

**Definition 2.** Existential and universal satisfaction are the smallest pair of binary relations  $\models_\exists$  and  $\models_\forall$  between graph predicates p and graph morphisms  $f: G \to H$  such that

- $p \models_\exists f$  whenever the following conditions hold:
  - $root_p = H$ ;
  - There are  $g: G \rightarrow K \in init_p$  and  $h: K \rightarrow H$  such that  $f = h \circ g$  and  $sub_p(K) \models_{\forall} h$ .
- $p \models_{\forall} f$  whenever the following conditions hold:
  - $root_p = H$ ;
  - For all  $g: G \rightarrow K \in init_p$  and all  $h: K \rightarrow H$  such that  $f = h \circ g$ ,  $sub_p(K) \models_{\exists} h$ .

Note that the concept of "smallest pair of binary relations" is indeed well-defined, under a pairwise ordering on sets. Also note that the problem due to the negation in the inductive definition of Def. 1 is no longer present in this formulation; instead, we can mark every arrow of a predicate diagram as  $\exists$  or  $\forall$ , depending on their distance from