

普通高等教育“十三五”规划教材

孙萌涛 李源作 编著

Sun Mengtao Li Yuanzuo

# One- and Two- Photon Absorptions:

Principles and Applications

## 单光子和双光子吸收： 原理和应用

清华大学出版社

One- and Two- Photon  
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## 内 容 简 介

本教材共分为9章,系统介绍了单光子吸收理论,单光子诱导电子空穴相关性,在生物、材料、SERS中的单光子过程,双光子吸收理论,非线性极化率理论,双光子诱导电子空穴相关性和双光子荧光分子应用等内容。本书内容深入浅出,通俗易懂。

本教材适用于物理学、光学、化学、材料学等专业科研院所和高校的研究人员、研究生及高年级本科生使用。

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## Sun Mengtao, Li Yuanzuo

**Sun Mengtao** obtained his Ph. D. in 2003 from the State Key Laboratory of Molecular Reaction Dynamics, Dalian Institute of Chemical Physics, Chinese Academy of Sciences (CAS). From 2003 to 2006, he worked as a postdoc at the Department of Chemical Physics, Lund University. Since 2006, as an associate professor, he has worked at the Beijing National Laboratory for Condensed Matter Physics, Institute of Physics, Chinese Academy of Sciences(CAS). In 2016, he became a full professor in University of Science and Technology Beijing, China. His current research interests focus on one- and two-photon absorptions in organic molecules, two-dimensional (2D) materials and plasmonics, as well as the exciton-plasmon coupling interaction for surface catalytic reaction. He has published more than 150 papers, including 10 invited review papers, three books and three book chapters in English, and citations are about 5 000 times. Researcher ID: B1131-2008. In 2016, He was awarded the second prize of Science and Technology in Liaoning province.



**Li Yuanzuo** earned his Ph. D. in the School of Physics, Dalian University of Technology (DLUT) in 2011. He became an associate professor in Northeast Forestry University in 2014. His current research interests include: experiment and first principle calculation on solar cells, excited state dynamics, energy conversion and nanomaterials. He has published more than 60 scientific publications, reviews and book chapters in the field of excited state properties of organic systems.

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## CHAPTER 1

### One-Photon Absorption Theory

It is known that there is a kind of electromagnetic (EM) interaction between light and matter, which determines the light absorption and the emission. Conjugated organic molecules have attracted considerable attention in the last decades due to their remarkable optoelectronic properties<sup>[1-6]</sup>, and their structural malleability allows tunable optical properties, which can be exploited for different applications, such as optoelectronic and photonic devices<sup>[7-11]</sup>. The time-independent perturbation theory is considered as a way to deal with the above problem, and there is a case in which we want to study how systems respond to the imposed perturbations<sup>[12-15]</sup>. Firstly, we assume that the Hamiltonian  $H$  of the system can be written in the form:

$$\hat{H} = \hat{H}_0 + \lambda V \quad (1-1)$$

where,  $\hat{H}_0$  is the Hamiltonian of the unperturbed system, and  $\lambda V$  is a perturbation term applied to the system. Since  $H_0$  is unperturbed, the Schrödinger equation is satisfied:

$$\hat{H}_0 \psi_n^0 = i \hbar \frac{\partial \psi_n^0}{\partial t} \quad (1-2)$$

The wave functions  $\psi_n^0$  are related to the time-dependent unperturbed wave-functions, as shown in form of  $\psi_n^0 = \psi_n \exp(-itE_n/\hbar)$ ; while the whole system wave-functions  $\psi(t)$  can be expressed as a linear combination of the  $\psi_n^0$ :

$$\psi = \sum_n C_n(t) \psi_n^0 \quad (1-3)$$

The time-dependent Schrödinger equation containing the perturbation term of EM interaction is expressed as

$$(\hat{H}_0 + \lambda V)\psi = i \hbar \frac{\partial \psi}{\partial t} \quad (1-4)$$

Inserting Eq. (1-3) into Eq. (1-4) gives

$$\lambda \sum_m C_m \langle \psi_n^0 | V | \psi_m^0 \rangle = i \hbar \frac{\partial C_n}{\partial t} \quad (1-5)$$

Given the dipole interaction between a system and an electric field can be viewed as a very small quantity in comparison with the Hamiltonian without perturbation, the wave function of the system has only a small change; therefore, the coefficient  $C_n$  was defined as the  $C_n = C_n^{(0)} + \lambda C_n^{(1)} + \lambda^2 C_n^{(2)} + \dots$ , where  $C_n^{(1)}$  and  $C_n^{(2)}$  were expansion coefficients of first- and second-order perturbations, respectively. And

$$\frac{dC_n^{(0)}}{dt} = 0 \quad (1-6)$$

$$i \hbar \frac{dC_n^{(1)}}{dt} = \sum_m C_m^{(0)} \langle \Psi_n^0 | V | \Psi_m^0 \rangle \quad (1-7)$$

$$i \hbar \frac{dC_n^{(2)}}{dt} = \sum_m C_m^{(1)} \langle \Psi_n^0 | V | \Psi_m^0 \rangle \quad (1-8)$$

Upon one electron is excited from initial state  $i$ , expanding coefficient  $C_i^{(0)} = 1$ . So

$$i \hbar \frac{dC_n^{(1)}}{dt} = \langle \Psi_n^0 | V | \Psi_i^0 \rangle \quad (1-9)$$

$$C_n^{(1)} = (V_{fi} / \hbar \omega_{fi}) (1 - e^{i\hbar\omega_{nk}t}) \quad (1-10)$$

where  $\omega_{fi} = (E_f - E_i) / \hbar$ .

For one-photon absorption (OPA) or 1-photon absorption (1PA), also called single-photon absorption, transition probability per unit time from  $i$  state to  $f$  state is then given by

$$W_{i \rightarrow f}^{(1)} = \frac{|C_n^{(1)}|^2}{t} = \left( \frac{|V_{fi}|}{\hbar \omega_{fi}} \right)^2 (2 - 2 \cos \omega_{fi} t) = \frac{2\pi}{\hbar} |V_{fi}|^2 \delta(E_f - E_i) \quad (1-11)$$

where  $V_{fi}$  is the perturbation matrix element. Considering the long interaction time between a system and an optical field, when  $t \rightarrow +\infty$ .

$$\delta(\omega_{fi}) = \frac{1}{\pi} \lim_{t \rightarrow \infty} \frac{1}{t} \frac{1 - \cos \omega t}{\omega_{nk}^2} \quad (1-12)$$

For calculating transition probability, each composite site, say initial state  $|I\rangle$ , is characterized by  $|\varepsilon_i, n_L \hbar \omega, n_1 \hbar \omega_2\rangle$ ;  $|F\rangle \equiv |\varepsilon_f, (n_L - 1) \hbar \omega_1\rangle$ , say final state. Furthermore, expanding the vector potential in terms of the creation and annihilation operator can be written as:

$$V = - \sum_k (\widehat{e}_k \cdot P) \frac{e}{m} \left( \frac{2\pi\hbar}{\omega_k L^3} \right)^{1/2} (\widehat{a}_k^+ + \widehat{a}_k) \quad (1-13)$$



$$\text{so } \omega_{if}^{(1)} = \frac{4\pi^2 \omega_L}{\hbar L} \sum_i \sum_f |\hat{e}_i \cdot \mu_{fi}|^2 \delta(\omega_{fi} - \omega_L) \quad (1-14)$$

The OPA oscillator strength of an electronic transition from the ground state (0) to the final state ( $f$ ) can be obtained by

$$f_{0f} = \frac{8\pi^2}{3} \frac{m_e}{e^2 \hbar} \nu_{0f} |\mu_{0f}|^2 \quad (1-15)$$

where,  $m_e$  is the electron mass,  $e$  is the electron charge,  $\hbar$  is Planck's constant,  $\nu_{0f} = E_{0f}/\hbar$  is the frequency in  $\text{s}^{-1}$  corresponding to the transition energy ( $E_{0f}$ ) between the two states, and the transition dipole moments are given by

$$\mu_{0f} = \langle 0 | e\mathbf{r} | f \rangle \quad (1-16)$$

The computed oscillator strength is related to the experimental integrated intensity by

$$f_{0f} = 4.32 \times 10^{-9} \int \epsilon(\bar{\nu}) d\bar{\nu} \quad (1-17)$$

where,  $\epsilon$  is the extinction coefficient in unit  $\text{L} \cdot \text{mol}^{-1}$ , and  $\bar{\nu}$  is the frequency in  $\text{cm}^{-1}$ . Since the integration limits in Eq. (1-3) are generally not known, a single Gaussian (or Lorentzian) function is often used to represent an experimental spectral band, which gives rise to an approximate measure of the corresponding band intensity. Using a Gaussian line-shape

$$f_{0f} = 4.32 \times 10^{-9} \epsilon_{\max} \int e^{-(\Delta\bar{\nu}/\theta)^2} d\bar{\nu} = 4.32 \times 10^{-9} \sqrt{\pi} \epsilon_{\max} \theta \quad (1-18)$$

The  $\theta$  width parameter relates to the full width ( $W$ ) at half maximum ( $\epsilon_{\max}/2$ ) by  $W = 2(\ln 2)^{1/2} \theta$ , and the cross section (in  $\text{cm}^2$ ) at the band maximum relates to  $\epsilon_{\max}$  by  $\sigma_{\max} = 3.83 \times 10^{-21} \epsilon_{\max}$ . Thus,  $\epsilon_{\max}$  or  $\sigma_{\max}$  of a transition can be readily approximated, provided its bandwidth is known.

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## CHAPTER 2

### Charge Transfer and Electron-Hole Coherence in OPA

Photoinduced charge transfer (CT) from donor to acceptor is a primary step in photophysical, photochemical as well as photobiological processes<sup>[1-5]</sup>. The CT process can be intermolecular, in which an electron is transferred from electron-donating species (D) to electron-accepting species (A), producing the radical cation of donor and the radical anion of acceptor, or intramolecular CT, involving charge redistribution in the excited molecule which produces a very large excited state dipole moment. It is well known that photophysical properties of the organic molecules are determined predominantly by the low energy excited states. Knowledge of nature of excited states, and interplay of inter- and intra-molecular mechanism in the CT process, are becoming very important to develop the novel optoelectronic devices.

Quantum chemistry provides practical approaches for studies on excited states. Upon OPA, the singlet excited states  $|S_n\rangle$  are represented by vectors  $C_{n,ai}^{CI}$  based on configurations of unoccupied and occupied molecular orbitals  $a$  and  $i$ , respectively. The molecular orbitals are in turn given by linear combinations of atomic orbitals (LCAOs)  $\mu$  and  $\nu$  with coefficients  $c_{a\mu}^{LCAO}$  and  $c_{i\nu}^{LCAO}$ . In order to characterize the excited state by observables we define two matrices<sup>[6,7]</sup>:

$$\begin{cases} \mathbf{Q}_{\mu\nu}^{(n)} = \frac{1}{\sqrt{2}} \sum_{\substack{a \in \text{unocc} \\ i \in \text{occ}}} C_{n,ai}^{CI} (c_{a\mu}^{LCAO} c_{i\nu}^{LCAO} + c_{i\mu}^{LCAO} c_{a\nu}^{LCAO}) \\ \mathbf{P}_{\mu\nu}^{(n)} = \frac{i}{\sqrt{2}} \sum_{\substack{a \in \text{unocc} \\ i \in \text{occ}}} C_{n,ai}^{CI} (c_{a\mu}^{LCAO} c_{i\nu}^{LCAO} - c_{i\mu}^{LCAO} c_{a\nu}^{LCAO}) \end{cases} \quad (2-1)$$

which are (anti)symmetric for exchange of the atomic orbitals and normalized as

$$\sum_{\mu,\nu} |\mathbf{Q}_{\mu\nu}^{(n)}|^2 = \sum_{\mu,\nu} |\mathbf{P}_{\mu\nu}^{(n)}|^2 = 1 \quad (2-2)$$

In the collective electron oscillator (CEO) model<sup>[8]</sup> the excited state  $|S_n\rangle$  is described by a harmonic oscillator with oscillating coordinate  $Q_{\mu\nu}^{(n)} \cos(\omega_n t)$  and momentum  $P_{\mu\nu}^{(n)} \sin(\omega_n t)$  for the transition frequency  $\omega_n$ . For visual characterization of the excited states we use two different representations of the matrices  $Q_{\mu\nu}^{(n)}$  and  $P_{\mu\nu}^{(n)}$ .

## 1. Real-space representation

In real space the oscillating CEO coordinate and momentum are given as<sup>[6, 7]</sup>

$$\begin{cases} Q_n(r, r'; t) = \sum_{\mu\nu} \phi_{\mu}^{AO}(r) Q_{\mu\nu}^{(n)} \phi_{\nu}^{AO}(r') \cos(\omega_n t) \\ P_n(r, r'; t) = \sum_{\mu\nu} \phi_{\mu}^{AO}(r) P_{\mu\nu}^{(n)} \phi_{\nu}^{AO}(r') \sin(\omega_n t) \end{cases} \quad (2-3)$$

The diagonal slice for  $r = r'$  results in

$$\begin{cases} Q_n(r, r; t) = \sqrt{2} \rho_{n0}(r) \cos(\omega_n t) \\ P_n(r, r; t) = 0 \end{cases} \quad (2-4)$$

The amplitude of the former is given by the so-called transition density (TD):

$$\rho_{n0}(r) = \frac{1}{\sqrt{2}} \sum_{\mu, \nu} \phi_{\mu}^{AO}(r) Q_{\mu\nu}^{(n)} \phi_{\nu}^{AO}(r) \quad (2-5)$$

The transition density contains information about the spatial location of the excitation<sup>[9]</sup> and is directly related to the transition dipole

$$\mu_{n0}(r) = e \int r \rho_{n0}(r) d^3 r \quad (2-6)$$

Furthermore, it is of particular relevance for excitonic interaction at shorter distances<sup>[10]</sup>. Besides the transition density, the charge difference density (CDD)

$$\Delta\rho_m(r) = 2i \sum_{\mu, \nu, k} \phi_{\mu}^{AO}(r) Q_{k\mu}^{(n)} P_{k\nu}^{(n)} \phi_{\nu}^{AO}(r) \quad (2-7)$$

is another useful quantity for real-space characterization of excitons. It represents the difference of electron distribution between the excited state  $|S_n\rangle$  and the ground state  $|S_0\rangle$ . In the present work, both transition and charge difference densities are represented by isosurfaces based on a 3D grid of approximately 100 000 cubes.

## 2. Site representation

For site representations of the CEO coordinate and momentum, we define them as:

$$\overline{Q_{AB}^{(n)2}} = \sum_{\substack{\mu \in A \\ \nu \in B}} |Q_{\mu\nu}^{(n)}|^2, \quad \overline{P_{AB}^{(n)2}} = \sum_{\substack{\mu \in A \\ \nu \in B}} |P_{\mu\nu}^{(n)}|^2 \quad (2-8)$$

respectively<sup>[8,11]</sup>. This means that the matrices  $Q_{\mu\nu}^{(n)}$  and  $P_{\mu\nu}^{(n)}$  are merged for atomic orbitals  $\mu$  and  $\nu$  belonging to atomic sites  $A$  and  $B$ , respectively. Thus  $\overline{P_{AB}^{(n)2}}$  gives the atomic sites  $A$  and  $B$  where electron and hole oscillate from and to, while  $\overline{Q_{AB}^{(n)2}}$  is a measure of the delocalization of the exciton as a whole. Note that for Frenkel excitons the occupation of  $\overline{Q_{AB}^{(n)2}}$  and  $\overline{P_{AB}^{(n)2}}$  is limited to pairs of atomic centers  $A$  and  $B$  belonging to the same monomeric unit.

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## CHAPTER 3

### Application of OPA

#### 3.1 Biology

##### 3.1.1 Retinal proteins (rhodopsins)

Rhodopsins are located in cell membrane and eye retina, which naturally exist in protonated Schiff-base form and can convert EM energy into chemical one<sup>[1]</sup>. The absorption of visible light that strikes eyes can arouse in the molecule an ultrafast response. As a central issue in photobiology, understanding the intrinsic ultrafast response mechanism is a challenging work<sup>[2,3]</sup>. Because most experiments<sup>[4-6]</sup> were performed in liquid phases till the recent papers<sup>[2,3]</sup>, it is hard to decide if the ultrafast response is an intrinsic property of this class molecules or a consequence of an interaction between the molecule and environment<sup>[7,8]</sup>. Theoretically, Anfinrud<sup>[9]</sup> and co-workers have suggested a three-state ( $S_0$ ,  $S_1$  and  $S_2$ ) model to explain the ultrafast photophysics process in bacteriorhodopsin. Olivucci<sup>[10]</sup> and co-workers proposed another two-state ( $S_0$  and  $S_1$ ) model and studied the related isomerization pathways on the  $S_1$  and  $S_2$  states in solution phase<sup>[11]</sup> and concluded that  $S_1$  and  $S_2$  are nearly degenerate states, which is similar to the conclusion drawn by Yamamoto<sup>[12]</sup> et al. Moreover, the  $S_1$ - $S_2$  level spacing is sensitive to the external perturbations and the measurements in different conditions<sup>[4-6,13-15]</sup>, and the addition of solutions makes the situation more complicated. Therefore, the  $S_1$  and  $S_2$  excited states' behavior in the vacuum and unperturbed conditions are very important for extracting the ultrafast response mechanism hidden in the veil.

As a specific example of retinal protein, the photoisomerization from 11-*cis*

protonated Schiff base (PSB11) to its all *trans* protonated Schiff base (PSBT) isomer (see Fig. 3-1 for their structures) is one of the fastest chemical reactions observed so far<sup>[7,16]</sup>. Some experimental<sup>[4-6]</sup> and theoretical<sup>[11,17]</sup> studies have been reported in different solutions for understanding such a phenomenon. As a result of low target densities, few experiments were done in the gas phase. However, information related to this photoisomerization process without external perturbations is crucial for elucidating the mechanism, since it can provide us a simpler picture about the photophysical and photochemical processes than ones in solution phase<sup>[2,3]</sup>. In this work, the  $T_v$ ,  $f$  and  $\mu$  values of the PSB11 and PSBT for  $S_1$  and  $S_2$  excited states were calculated by time-dependent density functional theory (TD-DFT) methods in vacuum and compared with the experimental detected values<sup>[2]</sup>. The experimentally observed phenomenon that the  $S_2$   $\mu$  value is much smaller than the  $S_1$  one was interpreted by a 3D representation of transition densities. The different optical behaviors (linear and nonlinear optical responds) of the excited states were investigated by considering different strengths of external electric fields.

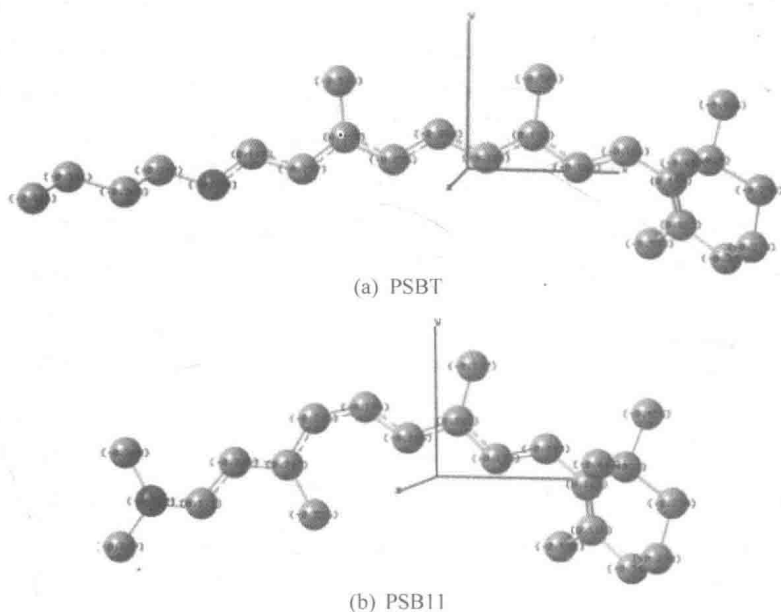


Figure 3-1 The schematic structure of (a) PSBT and (b) PSB11 retinal chromophores without H atoms together with the coordinate systems



The PSB11 ground state geometry was optimized by the B3LYP method with 6-31G(d), 6-31+G(d) and 6-311++G(d) basis sets. The results indicated that the size of the basis sets hardly affect the geometric parameters. Then PSBT ground-state geometry was just optimized by B3LYP/6-31G(d) and B3LYP/6-31+G(d), which also showed that the basis set size hardly influences the optimization results. Hereafter, the property calculations of PSB11 and PSBT were performed under their B3LYP/6-31G(d) optimized ground-state geometries. The subsequent B3LYP/6-31G(d) and B3LYP/6-31+G(d) frequency analyses indicated that the optimized geometries are the total minima on the potential energy surface of PSB11 and PSBT, respectively.

Table 3-1 shows  $S_1$  and  $S_2$  vertical excitation energies and oscillator strengths. The  $T_v$  and  $f$  values of the PSBT and PSB11 for  $S_1$  and  $S_2$  states were calculated by TD-B3LYP, TD-BPW91 and TDSVWN along with 6-31G(d), 6-31+G(d) and 6-311++G(d) basis sets, respectively. The calculated results were compared with the experimental detected values. For both PSBT and PSB11, the basis set size has very little affect on the calculated  $T_v$  and  $f$  values. However, the different functionals of the TD-DFT method do affect the calculated  $T_v$  and  $f$  values. For the PSBT  $S_1$  and  $S_2$  states, the TD-B3LYP, TD-BPW91 and TD-SVWN with 6-31G(d) basis set calculated  $T_v(f)$  values to be 536.1(1.561) nm and 393.7(0.669) nm, 590.5(0.835) nm, 451.9(0.891) nm, 592.3(1.003) nm and 451.1(1.058) nm, respectively.

**Table 3-1 TD-B3LYP and TDA calculated transition energies (in nm) of the first two excited states of PSBT and PSB11, compared with the corresponding experimental values**

Method	PSBT		PSB11	
	$S_1$	$S_2$	$S_3$	$S_4$
Exp.	620	385	610	390
TD-B3LYP/6-31G(d)	536.1	393.7	539.5	396.8
	(1.561)	(0.669)	(1.228)	(0.577)
TD-B3LYP/6-31+G(d)	543.1	397.3	546.6	400.0
	(1.580)	(0.647)	(1.295)	(0.564)
TD-B3LYP/6311++G(d)	543.9	398.1	548.1	401.3
	(1.579)	(0.646)	(1.291)	(0.561)
TD-BPW91/6-31G(d)	590.5	451.9	590.5	451.9
	(0.835)	(0.891)	(0.835)	(0.891)