



纳米科学与技术

# 生物纳米电子学

Bionanoelectronics  
Bioinquiring and Bioinspired Devices

Daniela Dragoman Mircea Dragoman

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北 京

图: 01-2014-4077

Reprint from English language edition:

Bionanoelectronics : Bioinquiring and Bioinspired Devices

by Daniela Dragoman and Mircea Dragoman

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#### 图书在版编目(CIP)数据

生物纳米电子学=Bionanoelectronics:bioinquiring and bioinspired devices :  
英文/(罗)弗拉格曼 (Dragoman,D.)主编. —影印本.—北京:科学出版社,  
2014.7

(纳米科学与技术)

ISBN 978-7-03-041427-4

I. ①生… II. ①弗… III. ①纳米材料-应用-生物-电子学-英文 IV. ①  
Q-331

中国版本图书馆CIP数据核字(2014)第166066号

丛书策划:杨震 / 责任编辑:王化冰

责任印制:钱玉芬 / 封面设计:陈敬

科学出版社出版

北京东黄城根北街16号

邮政编码:100717

<http://www.sciencep.com>

中国科学院印刷厂印制

科学出版社发行 各地新华书店经销

\*

2014年7月第一版 开本:720×1000 1/16

2014年7月第一次印刷 印张:16 3/4

字数:335 000

定价:138.00元

(如有印装质量问题,我社负责调换)



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在新兴前沿领域的快速发展过程中,及时整理、归纳、出版前沿科学的系统性专著,一直是发达国家在国家层面上推动科学技术发展的重要手段,是一个国家保持科学技术的领先权和引领作用的重要策略之一。

科学技术的发展和应用,离不开知识的传播:我们从事科学研究,得到了“数据”(论文),这只是“信息”。将相关的大量信息进行整理、分析,使之形成体系并付诸实践,才变成“知识”。信息和知识如果不能交流,就没有用处,所以需要“传播”(出版),这样才能被更多的人“应用”,被更有效地应用,被更准确地应用,知识才能产生更大的社会效益,国家才能在越来越高的水平上发展。所以,数据→信息→知识→传播→应用→效益→发展,这是科学技术推动社会发展的基本流程。其中,知识的传播,无疑具有桥梁的作用。

整个 20 世纪,我国在及时地编辑、归纳、出版各个领域的科学技术前沿的系列专著方面,已经大大地落后于科技发达国家,其中的原因有许多,我认为更主要的是缘于科学文化的习惯不同:中国科学家不习惯去花时间整理和梳理自己所从事的研究领域的知识,将其变成具有系统性的知识结构。所以,很多学科领域的第一本原创性“教科书”,大都来自欧美国家。当然,真正优秀的著作不仅需要花费时间和精力,更重要的是要有自己的学术思想以及对这个学科领域充分把握和高度概括的学术能力。

纳米科技已经成为 21 世纪前沿科学技术的代表领域之一,其对经济和社会展所产生的潜在影响,已经成为全球关注的焦点。国际纯粹与应用化学联合会(IUPAC)会刊在 2006 年 12 月评论:“现在的发达国家如果不发展纳米科技,今后必将沦为第三世界发展中国家。”因此,世界各国,尤其是科技强国,都将发展纳米科技作为国家战略。

兴起于 20 世纪后期的纳米科技,给我国提供了与科技发达国家同步发展的良好机遇。目前,各国政府都在加大力度出版纳米科技领域的教材、专著以及科普读物。在我国,纳米科技领域尚没有一套能够系统、科学地展现纳米科学技术各个方面前沿进展的系统性专著。因此,国家纳米科学中心与科学出版社共同发起并组织出版《纳米科学与技术》,力求体现本领域出版读物的科学性、准确性和系统性,全面科学地阐述纳米科学技术前沿、基础和应用。本套丛书的出版以高质量、科学性、准确性、系统性、实用性为目标,将涵盖纳米科学技术的所有领域,全面介绍国内外纳米科学技术发展的前沿知识;并长期组织专家撰写、编辑出版下去,为我国

表面分子组装》，是对相关工作的归纳总结。

多年来，本人的研究组开展固体表面分子组装研究，不但发展表面组装方法，还一直试图找到分子结构-固体种类-组装结构间的关系，也不放过发现组装结构中重要现象的机会并阐明原因，意欲探索表面分子组装规律，利用分子组装实现表面功能化。书中在介绍固体表面的结构特点和 STM 技术等表面分子组装基础知识之后，顺序介绍了简单烷烃/烷烃衍生物分子的组装结构、复杂配合物分子的组装、主客体组装以及功能化组装等，随后介绍结构转化研究、手性结构研究、电化学环境下的组装和相变化，最后是可能的表面功能化，内容安排尽量承上启下、先易后难且逻辑相关。

借此机会，我要感谢我研究组的研究生们，他们倾心科学，随我多年耕耘于固体表面分子组装研究领域，努力工作，夜以继日，他们终学有所成，也留下了丰富的科研结果。陈婷、严会娟、殷雅侠、陈庆、张旭、崔博、管翠中、郑轻娜等还参与了书稿内容整理、文献核对等工作。感谢科学出版社杨震、张淑晓和刘冉诸位编辑的悉心指导，感谢国家出版基金对本书的出版资助。感谢国家自然科学基金委员会、科技部和中国科学院，多年来，我的研究工作一直得到他们的支持，本书中的研究内容大多是在他们的资助下获得的科研成果。

还要感谢我的妻子姜红，她不厌其烦地整理我写下的零散片段，帮助打字输入我的手写书稿，保存相关资料，愿本书的出版给她带去一份快乐！

分子组装研究历史已久，内容丰富，且时有挑战课题出现，也有轰动性和里程碑性成果问世。限于水平和时间，书中不妥之处在所难免，恳请各位前辈和同行不吝赐教。出版本书意在抛砖引玉，以诱导、鼓励更多的科技工作者，尤其是青年科技工作者加入该研究行列，发展新技术，探索规律，攻坚克难；同时，发现新问题和解决新问题，推动分子组装研究不断发展。

姜红

# Preface

This is the first book on bionanoelectronics which deals with the applications of nanoelectronics in biology and medicine. Nanoelectronics is the most advanced area of nanotechnologies having huge applications in daily life. The mobile phones at which we are communicating every day as well as the desktop and laptop computers and iPhones are all results of the development of nanoelectronics, which is now able to fabricate with high reproducibility trillions of very large scale integrated circuits, integrating a huge number of transistors in a single chip. The nanoelectronics technologies are so effective that even 10 years ago the number of transistors contained in DRAM memories was greater than the number of grains of rice produced in the same year, and the price of a transistor was significantly lower than that of a grain of rice. These nanoscaled chips contain one billion transistors, which act as Boolean switches, connected in complicated paths, with a total length of 20 km, but confined and packed in an area of few  $\text{cm}^2$ . The nanoelectronics technology has developed so significantly according to the Moore law, which states that the dimensions of transistors reduce with 30% every 3 years, such that today the software of any iPhone is more powerful than that of the Apollo 11 lunar module, which landed on the Moon 30 years ago.

After publishing the second edition of the book *Nanoelectronics. Principles and Devices*, at Artech House, in 2009, which followed the first edition after only 3 years, we started to think that the last chapter of this book, called “Molecular and biological nanodevices,” must be extended into a separate book, taking into account the amazing applications of bionanoelectronics in rapid DNA sequencing, tissue engineering, controlled drug delivery, bioinspired devices, targeted cancer therapy, or even nanoelectronic artificial organs such as the nose, liver, or lung. More than 20 therapy products based on nanotechnologies are already in use, with very promising results, and other hundreds of nanomedicine-related devices are researched and are under clinical tests. However, we were a bit reluctant to start such an endeavor. We have known that nanoelectronic devices are governed by the rules of quantum mechanics, which prevail for any nanoscale device, and are accompanied by other fundamental laws of physics that cannot be easily adapted to the complex systems of biology. While physics uses a reductive approach to get relatively simple equations

with a universal character, also applicable in nanodevices, biology, and medicine are mainly observational science, since life manifestations are extremely complex. For example, in a human body, there are  $10^{14}$  cells and, due to cell divisions, 25 millions of new cells are generated every second; a cell has an average dimension of  $10\text{ }\mu\text{m}$  and weighs 1 ng; each cell contains the human genome having  $3 \times 10^9$  base pairs, which means 750 MB of information; the human genome is 1 m long but is folded and packed in few microns and weighs 3 pg. Indeed, our nanoelectronics chips are simple toys compared to what nature has created. We have to recognize that human body is in itself a universe having at least a similar complexity to the cosmological universe from which we originate.

So we have thought how to make accessible to the engineering and physical community the amazing accomplishments of nanoelectronic devices and nanotechnologies applied in various areas of biology and medicine. The reason of such important steps forward in bionanoelectronics are due to the fact that the size of nanodevices and nanomaterials are similar to that of cells, and even of the DNA. The result of our efforts is the present book. The book is not focused on complicated biological, medical, or chemical considerations, although we inevitably use terms from these sciences, briefly explained in the text.

The main idea of the book is to provide to the reader the basic knowledge of nanosciences, i.e., the theoretical concepts and the basic technologies, as well as their applications in biosensing, imaging, bioarchitectures, molecular devices, bioinspired devices, controlled drug delivery, implants, biochips, etc. Thus, the book has achieved an internal coherence reflecting the dual interaction between nanoelectronics on one side and biology and medicine on the other, manifested by bioinquiring devices, when nanotechnologies are used to sense, control, or heal biological systems, and by bioinspired devices, when innovative nanoelectronic devices mimic the function of biological systems.

The first chapter of the book contains the basic principles and theoretical concepts of nanosciences and nanotechnologies, which are further used in the entire book. The second chapter is dedicated to the sensing of biomolecules, including single biomolecules such as DNA, using various techniques, for example, nanoelectronic devices based on nanowires, carbon nanotubes, or graphene, nanocantilevers, or plamonic devices. An artificial nose, which is able to sense various gases in very small quantities, of even few molecules, and to detect the gases associated with diseases such as lung cancer ends this chapter. Chapter 3 is dealing with the imaging tools used in nanotechnologies, such as atomic force microscopy (AFM), which are applied to determine important parameters of various biological systems. The manipulation of biomolecules using optical tweezers and dielectrophoresis is also described in this chapter. These three chapters form the basis for understating the bioinquiring nanodevices. Chapter 4 is focused on the applications in medicine of nanoelectronic devices, which perform complex tasks such as controlled drug delivery monitored by external signals, targeted cancer cell therapy, and mimicking organs such as lung.

Chapters 5, 6, and 7 are dedicated, respectively, to biomolecular architectures, molecular devices, and biocomputing. These chapters present biological



devices that perform mechanical, optical, or electrical actions usually associated to nonbiological devices. On the contrary, Chap. 8 gathers examples of bioinspired devices, which refer to mechanical, optical, or electrical devices designed based on nature's lessons. The book ends with Chap. 9, which deals with nano-bio integration, a subject that could prove invaluable in the future innovative nanodevices. The applications of nanotechnologies in biology and medicine will produce soon a revolution similar to that of communications and computers, which made possible the occurrence of the internet, mobile phones, and laptops. In the case of bionanoelectronics and nanomedicine, we hope that the final result will be a better and healthier life, in a cleaner environment, the nanotechnologies contributing to the diagnosis and therapy of serious diseases as well as to the development of environmental-friendly technological processes.

Many thanks are addressed to Dr. Claus Ascheron from Springer Verlag, who has encouraged us during the writing of this book.

Bucharest

*Mircea Dragoman  
Daniela Dragoman*

# Contents

<b>1</b>	<b>Fundamentals on Bionanotechnologies</b>	<b>1</b>
1.1	Transport Phenomena at the Nanoscale	1
1.2	Nanotechnologies for Bionanoelectronic Devices	18
1.2.1	Deposition Techniques for Bionanoelectronic Devices	18
1.2.2	Nanolithography	20
1.2.3	Nanomaterials	27
1.3	Conduction Properties of Biological Materials	35
1.4	Microfluidics and Nanofluidics	46
	References	54
<b>2</b>	<b>Sensing of Biomolecules</b>	<b>57</b>
2.1	Nanotransistors Based on Nanotubes, Nanowires, and Graphene for Biosensing	57
2.2	DNA Detection and Sequencing Using Nanopores	73
2.3	MEMS/NEMS Biodetection	80
2.4	Plasmonics Biodetection	87
2.5	Nanoelectronic Noses and Various Disease Detection	98
	References	102
<b>3</b>	<b>Imaging and Manipulation of Biomolecules</b>	<b>107</b>
3.1	Bioapplications of Atomic Force Microscopy	107
3.2	Bioapplications of Scanning Tunneling Microscopy	114
3.3	Manipulation of Biological Materials	117
	References	123
<b>4</b>	<b>Nanomedicine</b>	<b>127</b>
4.1	Drug Delivery and Healing Based on Nanomaterials	127
4.2	Biochips—DNA Arrays and Other Chips for Diagnosis	144
4.3	Artificial Tissues and Organs	146
	References	148

<b>5</b>	<b>Biomolecular Architecture for Nanotechnology</b> .....	151
5.1	DNA-Based Molecular Architectures .....	152
5.2	Self-Assembled DNA Nanowires .....	155
5.3	Two- and Three-Dimensional Bioarchitectures as Scaffolds.....	159
5.4	Nonperiodic Biological Scaffolds for Inorganic Structures .....	165
5.5	Inorganic Scaffolds for Biomolecules.....	169
	References .....	170
<b>6</b>	<b>Biomolecular Machines</b> .....	173
6.1	Biological Actuators and Switches.....	174
6.2	Biological Walkers .....	180
6.3	Biological Motors .....	183
	References .....	187
<b>7</b>	<b>Biomolecular Computing</b> .....	189
7.1	Principles of Biomolecular Computing .....	189
7.2	Boolean Biomolecular Computing .....	192
7.3	Self-Assembly Biomolecular Computing .....	198
7.4	Biomolecular Logical Deductions.....	200
7.5	Biomolecular Memory Devices .....	201
7.6	Logical Drug Delivery and In Vivo Computation .....	203
	References .....	205
<b>8</b>	<b>Bioinspired Devices</b> .....	207
8.1	Bioinspired Materials .....	208
8.2	Bioinspired Devices.....	215
8.3	Bioinspired Technological Processes .....	222
8.4	Devices Mimicking Biological Organs/Functionalities .....	224
	References .....	229
<b>9</b>	<b>Nano-Bio Integration</b> .....	233
9.1	Nano-bio Materials for Electronics and Optoelectronics.....	233
9.2	Nano-bio Mechanical Devices.....	236
9.3	Nanobioelectronics and Optoelectronics.....	239
	References .....	246
	<b>Index</b> .....	249
	<b>About the Authors</b> .....	253

# Chapter 1

## Fundamentals on Bionanotechnologies

**Abstract** This is the introductory chapter of the book. The basic theoretical and experimental facts regarding the application of electronics at the nanoscale and for biological systems are developed here. Transport phenomena at the nanoscale, the principles of nanotechnologies, the physical properties of biological materials, and micro/nanofluidics are reviewed and explained in this chapter. The knowledge gained in this chapter will then be used in the entire book.

### 1.1 Transport Phenomena at the Nanoscale

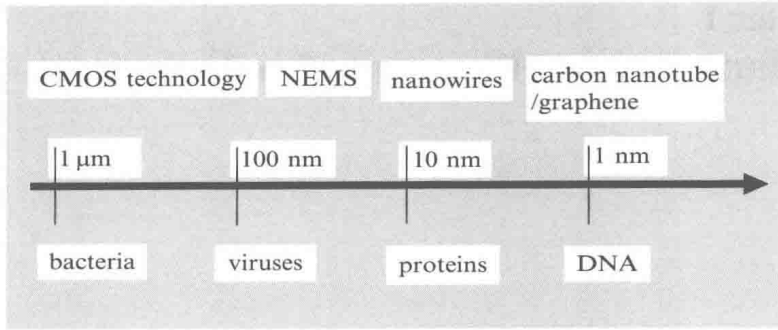
When electronic devices are scaled down from few microns up to nanoscale, they become comparable with living organisms, such as bacteria, viruses, or the dimensions of DNA bases. The nanoscale is represented in Fig. 1.1. This fact is of paramount importance for sensing, detecting, or manipulating microorganisms or biomolecules.

The reduced nanometer dimensions of electronic devices changes completely the transport properties. A nanoscale device is an electron device where one, two, or even all three spatial dimensions have few nm. If at a scale of few microns any electronic device can be described by macroscopic physical equations such as Ohm's law, at the nanoscale, microscopic equations are replaced by equations based on quantum mechanics. Quantum mechanical effects manifest at the nanoscale even at room temperature.

A homogenous semiconductor has a conduction band (the first empty band), a valence band (the last occupied band), and a bandgap that separates them. The distribution function of charge carriers in these bands is described by the Fermi-Dirac function

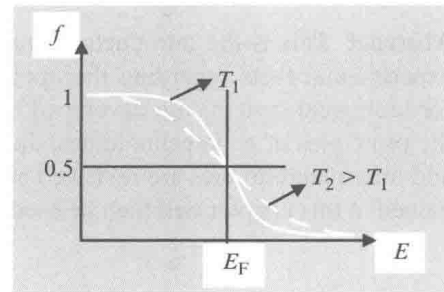
$$f(E) = 1/\{1 + \exp[(E - E_F)/k_B T]\}, \quad (1.1)$$

where  $E_F$  is the Fermi energy level. In semiconductors, the Fermi level is located inside the energy bandgap. In Fig. 1.2, we have displayed the Fermi function at two temperatures.



**Fig. 1.1** Dimension scale of biological systems and electron devices, where NEMS stands for nanoelectromechanical systems

**Fig. 1.2** The Fermi–Dirac distribution function



In the case of nanoscale devices, the confinement of carrier wavefunctions produces a discretization of the energy spectrum of charge carriers as well as discontinuities in the density of states. These effects cause further important changes in the transport properties of charge carriers depending on the number of dimensions along which the motion of carriers is restricted.

In bulk materials with dimensions of few millimeters, the transported carriers move randomly due to repeated scatterings with impurities and phonons. The carrier transport is thus of a diffusive type, which is modeled in general by a stochastic Boltzmann equation. The Boltzmann equation loses its validity as soon as the dimensions of the material shrink to nanoscale. The nanoscale is often termed as mesoscale since it is intermediate between the macroscopic scale and the atomic scale, where the atoms and molecules with sizes of the order of  $1 \text{ \AA} = 10^{-10} \text{ m}$  are described by quantum mechanical laws.

At the nanoscale, the electron transport is dictated by the relation between the dimensions of the sample and three parameters (Datta 1997):

1. The mean-free path  $L_{fp}$ , which is the average distance between two electron collisions with phonons or impurities that cancel the initial momentum of a charge carrier.
2. The phase relaxation length  $L_{ph}$ , which represents the propagation distance after which the electron coherence, i.e., the phase memory of electrons, vanishes as a result of time-reversal breaking. Examples of such processes are

electron–electron collisions, dynamic scatterings, or certain impurity scattering processes in which an internal degree of freedom changes; the phase relaxation length is often called the coherence length.

3. The electron Fermi wavelength, denoted as  $\lambda_F$ .

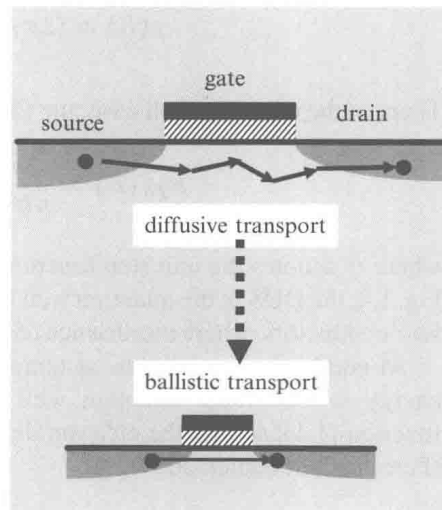
When one or more dimensions of a device are smaller than the mean-free path and the phase relaxation length, the number of scatterings reduces dramatically, and the transport in the device is termed ballistic. In this case, the electrons behave no longer as particles but as waves that follow all the reflection and refraction rules of common light or acoustic waves. As will be seen later, the ballistic transport manifests over distances of few hundreds of nanometers in carbon nanotubes (CNTs), graphene, or high-mobility transistors at room temperature.

In Fig. 1.3, we have schematically displayed a transistor with scaled down dimensions. The transport is diffusive when the transistor has gate lengths of  $1\ \mu\text{m}$  or greater and ballistic as soon as the gate channel shrinks to tens of nanometers. In the ballistic transport regime, the carriers traverse the gate channel in a much shorter time and with higher speeds.

The transport of ballistic charge carriers with electron effective mass  $m$  and constant energy  $E$  can be modeled by the time-independent Schrödinger equation

$$-\frac{\hbar^2}{2}\{m^\alpha \nabla [m^\beta \nabla (m^\alpha \Psi)]\} + V\Psi = E\Psi, \quad (1.2)$$

when the coupling phenomena between different electron bands can be neglected (Dragoman and Dragoman 1999). In (1.2),  $\Psi$  denotes the envelope electron wavefunction, which has a slow variation over the unit cell of the crystalline lattice and  $V$  is the potential energy. The material-dependent parameters  $\alpha$  and  $\beta$  are



**Fig. 1.3** The scaling down of a transistor

related by  $2\alpha + \beta = -1$  and are equal to  $\alpha = 0$  and  $\beta = -1$  in AlGaAs compounds, which were the first semiconductors that displayed ballistic transport.

The spatial restrictions on electron motion are expressed in the specific form of the boundary conditions imposed on the Schrödinger equation. A structure in which electrons are confined at the nanoscale by potential barriers along the, say,  $z$  direction but are free to travel along the transverse  $x$  and  $y$  directions is referred to as quantum well (QW). In a quantum well with infinite-height potential barriers, the Schrödinger equation is accompanied by the boundary conditions  $\Psi(x, y, 0) = \Psi(x, y, L_z) = 0$ , where  $L_z$  is the width of the quantum well.

If  $V = 0$ , the solution of the Schrödinger equation can be written as  $\Psi(x, y, z) = (2/L_x L_y)^{1/2} \sin(k_z z) \exp(ik_x x) \exp(ik_y y)$ , where  $L_x$  and  $L_y$  are, respectively, the dimensions of the structure along  $x$  and  $y$ . In ballistic devices,  $L_z$  is comparable to the Fermi wavelength  $\lambda_F$  and  $L_z < L_x, L_y \ll L_{fp}, L_{ph}$ . Another effect of the boundary conditions is a discrete spectrum for the  $z$  component of the electron momentum  $k_z = p\pi/L_z$ , which induces a discretization of the energy levels along the direction of spatial restriction. The energy dispersion relation in the quantum well in which the bottom of the conduction band  $E_c$  is considered as reference is given by

$$E(k_x, k_y, k_z) = E_c + \frac{\hbar^2}{2m} \left( \frac{p\pi}{L_z} \right)^2 + \frac{\hbar^2}{2m} (k_x^2 + k_y^2) = E_{s,p} + \frac{\hbar^2}{2m} (k_x^2 + k_y^2), \quad (1.3)$$

where  $E_{s,p}$  is the cutoff energy of the discrete subband labeled by the integer  $p$ ; the subbands are also referred to as transverse modes. The difference in energy between adjacent subbands is greater for more confined electrons, i.e., for smaller  $L_z$ .

For an arbitrary energy distribution in the  $\mathbf{k}$  space, which takes  $E(\mathbf{k})$  constant values on a  $\mathbf{k}$ -space surface  $\Sigma$ , a spin-degenerate density of states (DOS) can be defined as

$$\rho(E) = (2\pi)^{-3} \int_{\Sigma} \frac{dS}{|\nabla_{\mathbf{k}} E|_{E=\text{const.}}} \quad (1.4)$$

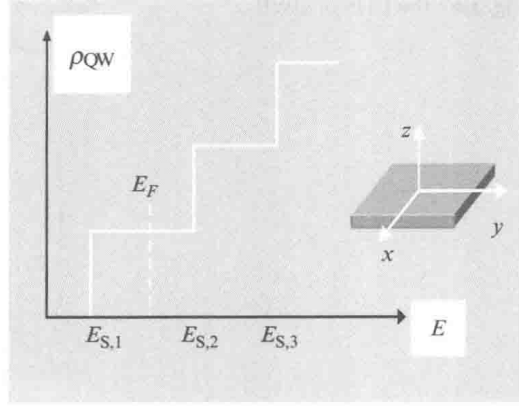
Then, in the quantum well case, the DOS particularizes to

$$\rho_{\text{QW}}(E) = \frac{m}{\pi \hbar^2 L_z} \sum_p \vartheta(E - E_{s,p}), \quad (1.5)$$

where  $\vartheta$  denotes the unit step function. As follows from (1.5), and as illustrated in Fig. 1.4, the DOS in the quantum well is discontinuous, in contrast to the case of bulk semiconductors, where the absence of spatial constraints leads to a continuous DOS.

At equilibrium conditions at temperature  $T$ , the electrons occupy the discrete energy levels of the quantum well according to the Fermi–Dirac distribution function (1.1), so that the electron density per unit area at equilibrium is given by (Ferry and Goodnick 2009)

**Fig. 1.4** Density of states in a quantum well



$$n = L_z \int_0^{\infty} \rho_{\text{QW}}(E) f(E) dE = k_B T \frac{m}{\pi \hbar^2} \sum_p \ln[1 + \exp(E_F - E_{s,p})/k_B T]. \quad (1.6)$$

In the degenerate limit or at low temperatures, when  $k_B T \ll E_F$ , the Fermi–Dirac distribution function is proportional to  $\vartheta(E_F - E)$ , so that all electron subbands below the Fermi energy are filled with electrons, and all subbands above it are empty. At low temperatures, the electrons with energy  $E$  reside in a number of subbands  $M(E)$ , which can be determined by counting the transverse modes with cutoff energies below  $E$ .

When the Fermi energy level in a quantum well is positioned between the first and the second energy subband, as displayed in Fig. 1.4, we have a two-dimensional electron gas (2DEG), which has a metallic behavior because  $E_F$  is inside the conduction band. In this case, the Fermi wavenumber  $k_F$ , determined from the electron kinetic energy as  $E_{\text{kin}} = E_F - E_{s,1} = \hbar^2 k_F^2 / 2m$ , is correlated to the electron density per unit area  $n = (m/\pi \hbar^2)(E_F - E_{s,1})$  through the formula (Ferry and Goodnick 2009)

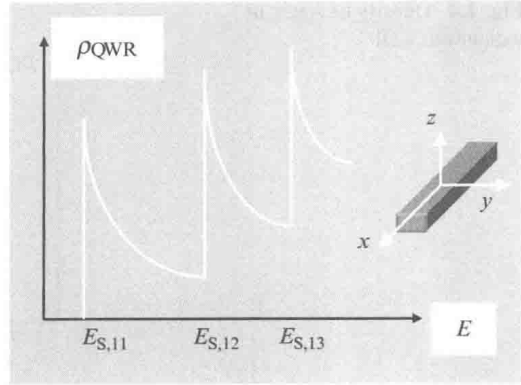
$$k_F = (2\pi n)^{1/2}. \quad (1.7)$$

The Fermi wavelength is defined as  $\lambda_F = 2\pi/k_F$ .

A nanoscale structure is called quantum wire (QWR) if the electron motion is spatially restricted by energy potentials in regions of widths  $L_y$  and  $L_z$  along two directions:  $y$  and  $z$ , but the electron can move freely along  $x$ . If the constraining potentials have infinite heights, the electron wavefunction has the expression  $\Psi(x, y, z) = [2/(L_y L_z L_x)^{1/2}] \sin(k_y L_y) \sin(k_z L_z) \exp(i k_x x)$ , and boundary conditions similar to those in the quantum well case imply that  $k_y = p\pi/L_y$ ,  $k_z = q\pi/L_z$ , with  $p, q$  integer numbers. The energy dispersion relation in QWR is then given by

$$E(k_x, k_y, k_z) = E_c + \frac{\hbar^2}{2m} \left( \frac{p\pi}{L_y} \right)^2 + \frac{\hbar^2}{2m} \left( \frac{q\pi}{L_z} \right)^2 + \frac{\hbar^2 k_x^2}{2m} = E_{s,pq} + \frac{\hbar^2 k_x^2}{2m}, \quad (1.8)$$



**Fig. 1.5** The DOS of QWR

so that the DOS becomes

$$\rho_{\text{QWR}}(E) = \frac{(2m)^{1/2}}{\pi \hbar L_y L_z} \sum_{p,q} (E - E_{s,pq})^{-1/2}. \quad (1.9)$$

The DOS of QWR is represented in Fig. 1.5.

Similar to the optical waveguides, the QWRs with  $L_y, L_z < L_x \ll L_{\text{fp}}, L_{\text{ph}}$  and  $L_y, L_z \cong \lambda_F$  are called electron waveguides if the energy difference between adjacent subbands is higher than the thermal energy  $k_B T$  and the possible potential drop along the waveguide,  $eV$ , where  $V$  is the applied bias (Dragoman and Dragoman 2004). At temperatures around 4 K, this condition is satisfied in modulation-doped AlGaAs/GaAs heterostructures for  $L_y, L_z \cong 0.1\text{--}0.5 \mu\text{m}$  and  $V < 1 \text{ mV}$ .

In a quantum dot (QD), the motion of charge carriers is spatially constrained along all three directions in regions much smaller than the mean-free path and the phase relaxation length. In this case, the discrete energy dispersion is given by

$$E(k_x, k_y, k_z) = E_c + \frac{\hbar^2}{2m} \left( \frac{p\pi}{L_x} \right)^2 + \frac{\hbar^2}{2m} \left( \frac{q\pi}{L_y} \right)^2 + \frac{\hbar^2}{2m} \left( \frac{r\pi}{L_z} \right)^2 = E_{s,pqr}, \quad (1.10)$$

and the DOS is proportional to the Dirac function

$$\rho_{\text{QD}} \propto \delta(E - E_{s,pqr}). \quad (1.11)$$

The DOS of QD is shown in Fig. 1.6. The discrete energy spectrum of quantum dots is similar to that of atoms or molecules, and therefore, sometimes, QDs are referred to as artificial atoms.

In the ballistic regime, only electrons with energies around  $E_F$  take part at transport, whereas in the diffusive regime, electrons with a wide energy spectrum contribute to electrical transport.