

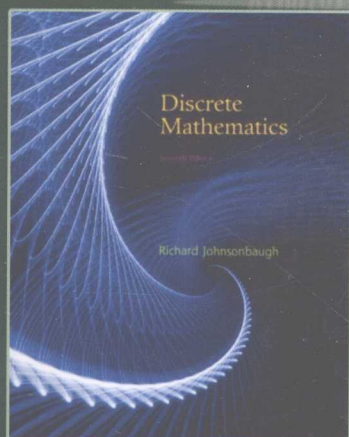
国外计算机科学教材系列

PEARSON

离散数学

(第七版)

Discrete Mathematics, Seventh Edition



英文版

[美] Richard Johnsonbaugh 著



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Publishing House of Electronics Industry

北京·BEIJING

内 容 简 介

本书从算法分析和问题求解的角度,全面系统地介绍了离散数学的基础概念及相关知识。书中通过大量实例,深入浅出地讲解了数理逻辑、组合算法、图论、布尔代数、网络模型、形式语言与自动机理论等与计算机科学密切相关的前沿课题,既着重于各部分内容之间的紧密联系,又深入探讨了相关的概念、理论、算法和实际应用。本书内容叙述严谨、推演详尽,各章配有相当数量的习题,并且在书后提供了相应的提示和答案,为读者迅速掌握有关知识提供了有效的帮助。

本书既可作为计算机科学及计算数学等专业的本科生和研究生教材,也可作为工程技术人员和相关人员的参考书。

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此外,我们还将与国外著名出版公司合作,提供一些教材的教学支持资料,希望能为授课老师提供帮助。今后,我们将继续加强与各高校教师的密切联系,为广大师生引进更多的国外优秀教材和参考书,为我国计算机科学教学体系与国际教学体系的接轨做出努力。

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PREFACE

This updated edition is intended for a one- or two-term introductory course in discrete mathematics, based on my experience in teaching this course over many years and requests from users of previous editions. Formal mathematics prerequisites are minimal; calculus is *not* required. There are no computer science prerequisites. The book includes examples, exercises, figures, tables, sections on problem-solving, sections containing problem-solving tips, section reviews, notes, chapter reviews, self-tests, and computer exercises to help the reader master introductory discrete mathematics. In addition, an *Instructor's Guide* and website are available.

In the early 1980s there were few textbooks appropriate for an introductory course in discrete mathematics. However, there was a need for a course that extended students' mathematical maturity and ability to deal with abstraction, which also included useful topics such as combinatorics, algorithms, and graphs. The original edition of this book (1984) addressed this need and significantly influenced the development of discrete mathematics courses. Subsequently, discrete mathematics courses were endorsed by many groups for several different audiences, including mathematics and computer science majors. A panel of the Mathematical Association of America (MAA) endorsed a year-long course in discrete mathematics. The Educational Activities Board of the Institute of Electrical and Electronics Engineers (IEEE) recommended a freshman discrete mathematics course. The Association for Computing Machinery (ACM) and IEEE accreditation guidelines mandated a discrete mathematics course. This edition, like its predecessors, includes topics such as algorithms, combinatorics, sets, functions, and mathematical induction endorsed by these groups. It also addresses understanding and constructing proofs and, generally, expanding mathematical maturity.

Logic and Proofs Changes

The changes in this book, the seventh edition, result from comments and requests from numerous users and reviewers of previous editions of the book. The biggest change from the sixth to the seventh edition occurs in Chapters 1–3. The first chapter in the sixth edition, Logic and Proofs, has been divided into two chapters in the seventh edition: Sets and Logic (Chapter 1) and Proofs (Chapter 2). Except for the section on sets, Chapters 2 (The Language of Mathematics) and 3 (Relations) in the sixth edition have been combined into Chapter 3 (Functions, Sequences, and Relations) in the seventh edition. Pre-publication reviews have been very enthusiastic about these changes.

The section on sets is now the first section of the book. This change permits the use of set terminology throughout the book. It makes sets available for proofs in examples and exercises, thus providing more interesting examples earlier than in the previous editions. We can even use sets to introduce proofs (e.g., proving that two sets are equal, proving that one set is a subset of another) before fully discussing proofs and proof techniques.

The discussion about how to construct proofs has been greatly expanded. Sections 2.1 and 2.2 are new extended sections on mathematical systems and proof techniques. In addition, there are expanded subsections on proofs of equivalence and existence proofs (including constructive and nonconstructive existence proofs). Nearly every proof is preceded by a Discussion section and/or accompanied by a figure. The Problem-Solving Tips sections include expanded advice, examples, and so on, on how to do proofs, how to write up proofs, and common errors in proofs. There are two new Problem-Solving Corners, one on quantifiers, the other on proofs (see Proving Some Properties of Real Numbers).

The discussion of arguments and rules of inference for propositions has been moved to follow the discussion of propositions. The rules of inference for quantified statements are integrated within the quantifiers section.

The number of examples and exercises has been vastly expanded. In the sixth edition, there were approximately 1370 worked examples and exercises in the first three chapters. In the seventh edition, there are approximately 1640 worked examples and exercises in the first three chapters. Of course, not just the quantity of examples and exercises is important, it is also the quality. In most of the examples found in the sixth edition, the discussion has been expanded and additional motivation has been added.

Other Changes from the Sixth Edition

Other changes from the sixth edition are as follows:

- The description and notation for integers (\mathbf{Z} , \mathbf{Z}^+ , \mathbf{Z}^- , $\mathbf{Z}^{\text{nonneg}}$), rational numbers (with \mathbf{Z} replaced by \mathbf{Q}), and real numbers (with \mathbf{Z} replaced by \mathbf{R}) are introduced early (in Section 1.1, Sets).
- Proofs, rather than sketches of proofs as in the sixth edition, are provided for Theorems 5.1.17 and 5.1.22, which give the greatest common divisor and least common multiple of two integers given their prime factorizations.
- Recursive algorithms are given (Algorithms 5.3.9 and 5.3.10) to compute the greatest common divisor of two integers a and b , $\gcd(a, b)$, and to compute integers s and t satisfying $\gcd(a, b) = sa + tb$.
- The Inclusion-Exclusion Principle has been added to Section 6.1.
- Internet addressing is now included in Section 6.1.
- Several practice exercises have been added to Section 6.1 that specifically say to use either the Multiplication Principle or the Addition Principle. These exercises precede other exercises that require the reader to figure out which Principle to use or require using both Principles.
- The section on Generalized Permutations and Combinations (Section 6.6 in the sixth edition) now follows Sections 6.1 and 6.2 (Basic Principles, Permutations and Combinations) since generalized permutations and combinations are so closely related to the material in Sections 6.1 and 6.2.
- Several relatively straightforward “warm-up” exercises have been added before the main pigeonhole exercises (Section 6.8).
- More exercises on graph isomorphism have been added (Section 8.6). The exercises have been divided into those that ask for a proof that two given graphs are isomorphic, those that ask for a proof that two given graphs are not isomorphic, and those that ask the reader to determine, with a proof, whether two given graphs are isomorphic.

- In Section 9.3, there are several new backtracking exercises including the popular Sudoku puzzle.
- More examples and exercises are included to highlight common errors (for example, the subsection Some Common Errors that precedes the Section 2.1 Review Exercises discusses some common errors in proofs, and Example 6.2.24 illustrates a common counting error).
- A number of recent books and articles have been added to the list of references. Several book references have been updated to current editions.
- The number of worked examples has been increased to over 650. (There were approximately 600 in the sixth edition.)
- The number of exercises has been increased to nearly 4200. (There were approximately 4000 in the sixth edition.)

Contents and Structure

This book includes

- Sets and logic (including quantifiers). Practical examples such as using the Google search engine are included (Example 1.2.13). Translating between English and symbolic expressions is discussed as is logic in programming languages. A *logic game*, which offers an alternative way to determine whether a quantified propositional function is true or false, is discussed in Example 1.6.15.
- Proofs (Chapter 2). Proof techniques discussed include direct proofs, counterexamples, proof by contradiction, proof by contrapositive, proofs by cases, proofs of equivalence, existence proofs (constructive and nonconstructive), and mathematical induction. Loop invariants are presented as a practical application of mathematical induction. We also include a brief, optional section on resolution proofs (a proof technique that can be automated).
- Functions, sequences, sum and product notations, strings, and relations (Chapter 3), including motivating examples such as the new 13-character international standard book number (ISBN), an introduction to hash functions, and pseudorandom number generators (Section 3.1); an application of partial orders to task scheduling (Section 3.3); and relational databases (Section 3.6).
- A thorough discussion of algorithms, recursive algorithms, and the analysis of algorithms (Chapter 4). A number of examples of algorithms are presented before getting into big-oh and related notations (Sections 4.1 and 4.2), thus providing a gentle introduction and motivating the formalism that follows. An algorithmic approach is taken throughout this book. We mention that many modern algorithms do not have all the properties of classical algorithms (e.g., many modern algorithms are not general, deterministic, or even finite). To illustrate the point, an example is given of a randomized algorithm (Example 4.2.4). The algorithms are written in a flexible form of pseudocode, which resembles currently popular languages such as C, C++, and Java. (The book does not assume any computer science prerequisites; the description of the pseudocode used is given in Appendix C.) Among the algorithms presented are tiling (Section 4.4), the Euclidean algorithm for finding the greatest common divisor (Section 5.3), the RSA public-key encryption algorithm (Section 5.4), generating combinations and permutations (Section 6.4), merge sort (Section 7.3), Dijkstra's shortest-path algorithm (Section 8.4), backtracking algorithms (Section 9.3), breadth-first and depth-first search (Section 9.3), tree traversals (Section 9.6), evaluating a game tree (Section 9.9), finding a

maximal flow in a network (Section 10.2), finding a closest pair of points (Section 13.1), and computing the convex hull (Section 13.2).

- A full discussion of the “big oh,” omega, and theta notations for the growth of functions (Section 4.3). Having all of these notations available makes it possible to make precise statements about the growth of functions and the time and space required by algorithms.
- An introduction to number theory (Chapter 5). This chapter includes classical results (e.g., divisibility, the infinitude of primes, fundamental theorem of arithmetic), as well as algorithmic number theory (e.g., the Euclidean algorithm to find the greatest common divisor, exponentiation using repeated squaring, computing s and t such that $\text{gcd}(a, b) = sa + tb$, computing an inverse modulo an integer). The major application is the RSA public-key cryptosystem (Section 5.4). The calculations required by the RSA public-key cryptosystem can be performed using the algorithms previously developed in the chapter.
- Combinations, permutations, discrete probability, and the Pigeonhole Principle (Chapter 6). Two optional sections (Sections 6.5 and 6.6) treat discrete probability.
- Recurrence relations and their use in the analysis of algorithms (Chapter 7).
- Graphs, including coverage of graph models of parallel computers, the knight’s tour, Hamiltonian cycles, graph isomorphisms, and planar graphs (Chapter 8). Theorem 8.4.3 gives a simple, short, elegant proof of the correctness of Dijkstra’s algorithm.
- Trees, including binary trees, tree traversals, minimal spanning trees, decision trees, the minimum time for sorting, and tree isomorphisms (Chapter 9).
- Networks, the maximal flow algorithm, and matching (Chapter 10).
- A treatment of Boolean algebras that emphasizes the relation of Boolean algebras to combinatorial circuits (Chapter 11).
- An approach to automata emphasizing modeling and applications (Chapter 12). The *SR* flip-flop circuit is discussed in Example 12.1.11. Fractals, including the von Koch snowflake, are described by special kinds of grammars (Example 12.3.19).
- An introduction to computational geometry (Chapter 13).
- Appendixes on matrices, basic algebra, and pseudocode.
- A strong emphasis on the interplay among the various topics. As examples, mathematical induction is closely tied to recursive algorithms (Section 4.4); the Fibonacci sequence is used in the analysis of the Euclidean algorithm (Section 5.3); many exercises throughout the book require mathematical induction; we show how to characterize the components of a graph by defining an equivalence relation on the set of vertices (see the discussion following Example 8.2.13); and we count the number of nonisomorphic n -vertex binary trees (Theorem 9.8.12).
- A strong emphasis on reading and doing proofs. Most proofs of theorems are illustrated with annotated figures and/or motivated by special Discussion sections. Separate sections (Problem-Solving Corners) show students how to attack and solve problems and how to do proofs. Special end-of-section Problem-Solving Tips highlight the main problem-solving techniques of the section.
- A large number of applications, especially applications to computer science.
- Figures and tables to illustrate concepts, to show how algorithms work, to elucidate proofs, and to motivate the material. Several figures illustrate proofs of theorems. The captions of these figures provide additional explanation and insight into the proofs.

- Section review exercises.
- Notes sections with suggestions for further reading.
- Chapter reviews.
- Chapter self-tests.
- Computer exercises.
- A reference section containing more than 160 references.
- Front and back endpapers that summarize the mathematical and algorithm notation used in the book.

Each chapter is organized as follows:

Overview
 Section
 Section Review Exercises
 Section Exercises
 Section
 Section Review Exercises
 Section Exercises
 ⋮
 Notes
 Chapter Review
 Chapter Self-Test
 Computer Exercises

Section review exercises review the key concepts, definitions, theorems, techniques, and so on of the section. All section review exercises have answers in the back of the book. Although intended for reviews of the sections, section review exercises can also be used for placement and pretesting.

Notes contain suggestions for further reading. Chapter reviews provide reference lists of the key concepts of the chapters. Chapter self-tests contain four exercises per section, with answers in the back of the book.

Computer exercises include projects, implementation of some of the algorithms, and other programming related activities. Although there is no programming prerequisite for this book and no programming is introduced in the book, these exercises are provided for those readers who want to explore discrete mathematics concepts with a computer.

In addition, most chapters have Problem-Solving Corners.

Exercises

The book contains nearly 4200 exercises, 145 of which are computer exercises. Exercises felt to be more challenging than average are indicated with a star, *. Exercise numbers in color (approximately one-third of the exercises) indicate that the exercise has a hint or solution in the back of the book. The solutions to most of the remaining exercises may be found in the *Instructor's Guide*. A handful of exercises are clearly identified as requiring calculus. No calculus concepts are used in the main body of the book and, except for these marked exercises, no calculus is needed to solve the exercises.

Examples

The book contains over 650 worked examples. These examples show students how to tackle problems in discrete mathematics, demonstrate applications of the theory, clarify proofs, and help motivate the material.

Problem-Solving Corners

The Problem-Solving Corner sections help students attack and solve problems and show them how to do proofs. Written in an informal style, each is a self-contained section following the discussion of the subject of the problem. Rather than simply presenting a proof or a solution to a problem, in these sections the intent is to show alternative ways of attacking a problem, to discuss what to look for in trying to obtain a solution to a problem, and to present problem-solving and proof techniques.

Each Problem-Solving Corner begins with a statement of a problem. After stating the problem, ways to attack the problem are discussed. This discussion is followed by techniques for finding a solution. After a solution is found, a formal solution is given to show how to correctly write up a formal solution. Finally, the problem-solving techniques used in the section are summarized. In addition, some of these sections include a Comments subsection, which discusses connections with other topics in mathematics and computer science, provides motivation for the problem, and lists references for further reading about the problem. Exercises conclude some Problem-Solving Corners.

Instructor Supplement

An *Instructor's Guide* is available at no cost from the publisher to instructors who adopt or sample this book. It should be requested from your local Prentice Hall representative. The *Instructor's Guide* contains solutions to most of the exercises not included in the book.

Website

The website

<http://condor.depaul.edu/~rjohnson/dm7th>

for the seventh edition contains



- Expanded explanations of difficult material and links to other sites for additional information about discrete mathematics topics. The icon shown signals that an expanded explanation or a link is at the book's website.
- Supplementary material
- Computer programs
- An errata list.

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Richard Johnsonbaugh

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